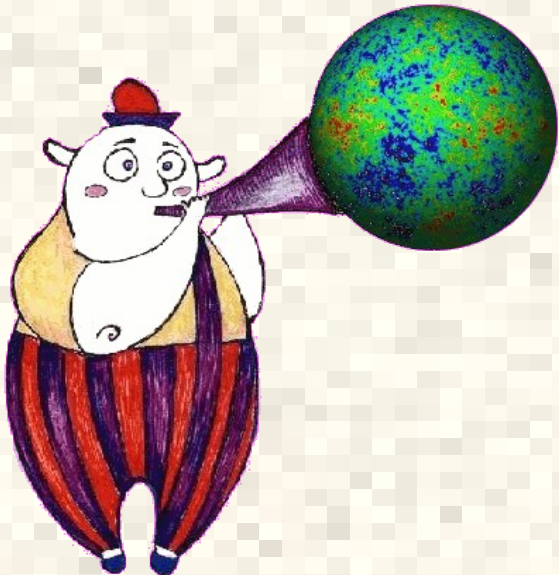


# Lecture 2.

## Cosmic microwave background observations and data processing

*Oleg Verkhodanov*

*Special astrophysical observatory, Russia*



# Cosmological tests

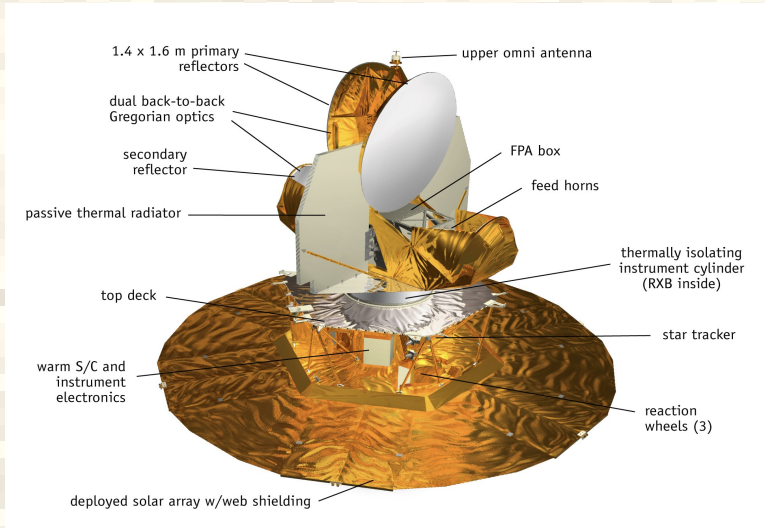
- ***Cosmic microwave background***
  - a) Angular power spectrum
  - b) Statistical properties (gaussianity)

cosmological  
tests

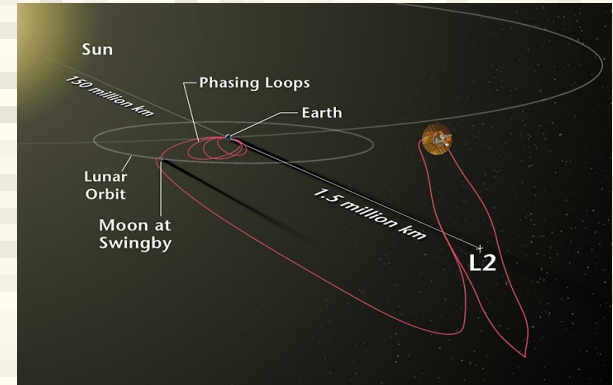


To solve problems, cosmic missions had launched  
and probably they are not the last

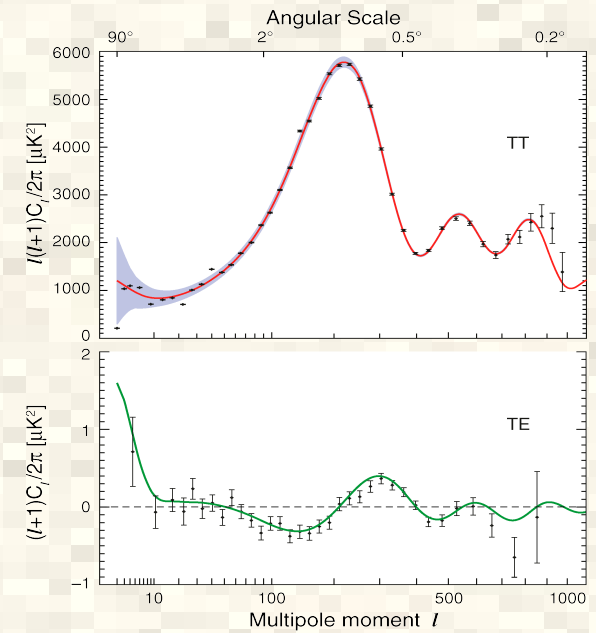
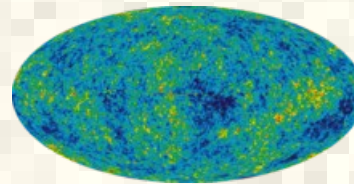
# Wilkinson Microwave Anisotropy Probe (WMAP, NASA)



2001-2011

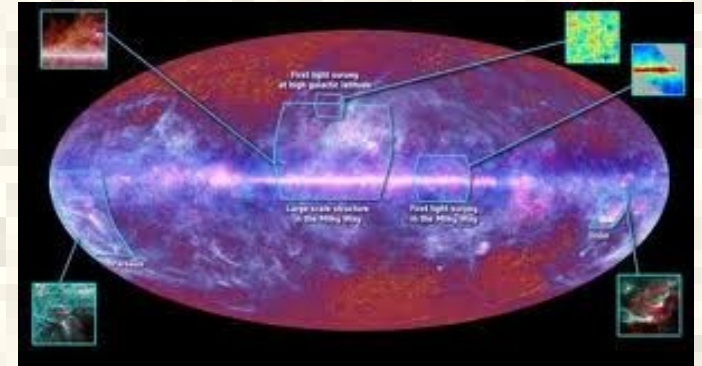
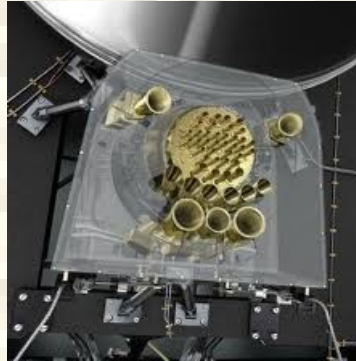


5 frequencies:  
23, 33, 41, 61, 94 GHz



Best determination of cosmological parameters till 2011 !

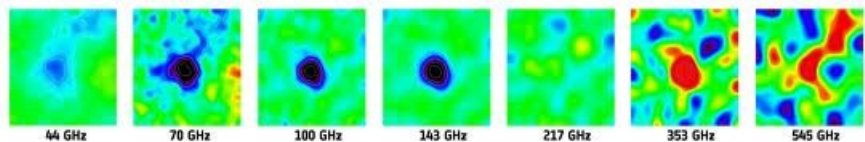
# Planck mission, ESA



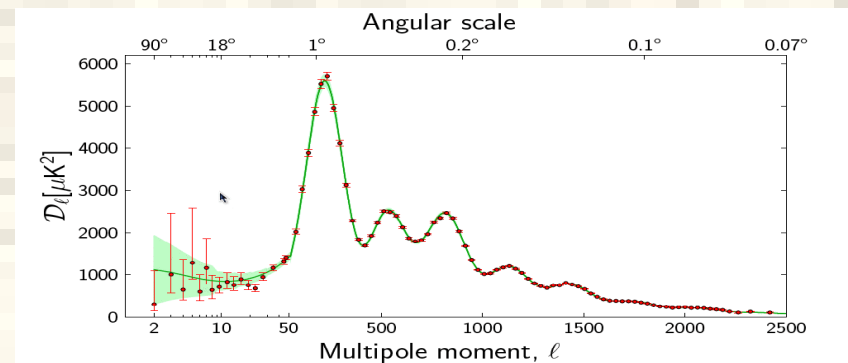
2010-2013

Low Frequency Instrument: 30,44,70  
HFI: 100, 143, 217, 353, 545, 857 GHz

2) Zeldovich-Sunyaev effect



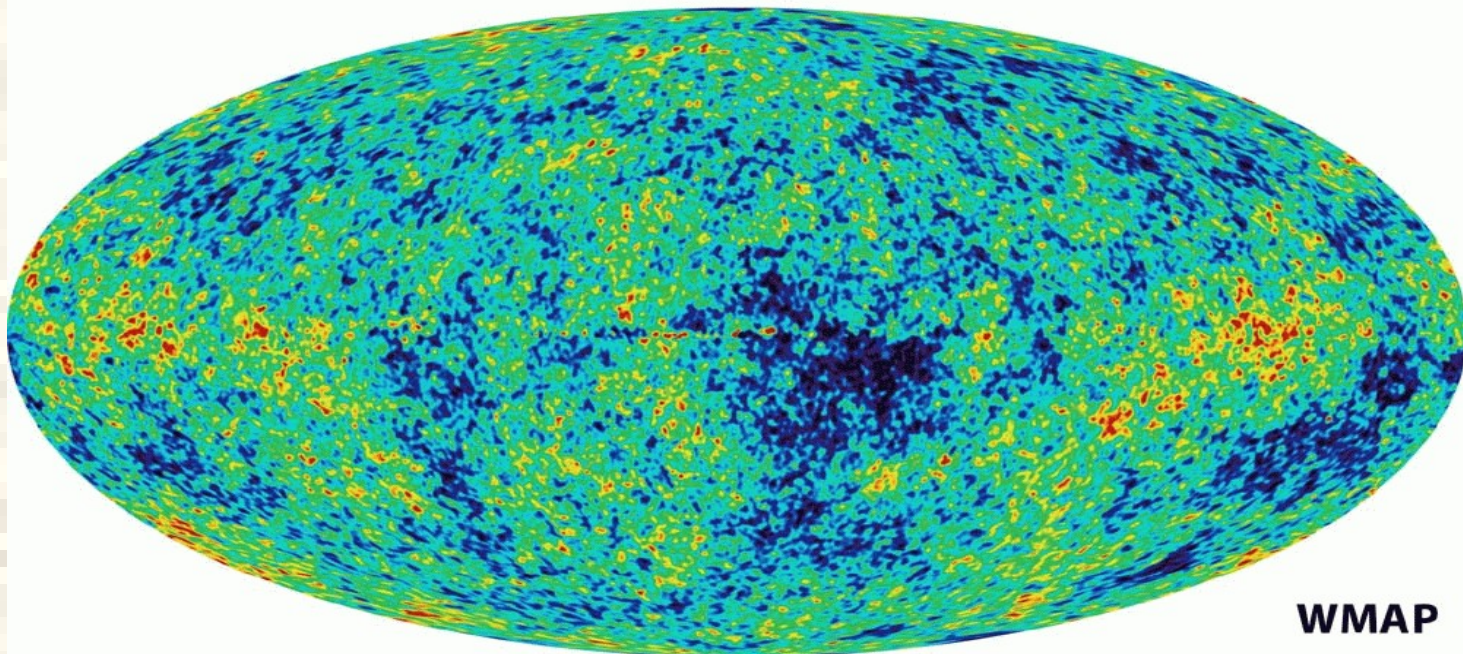
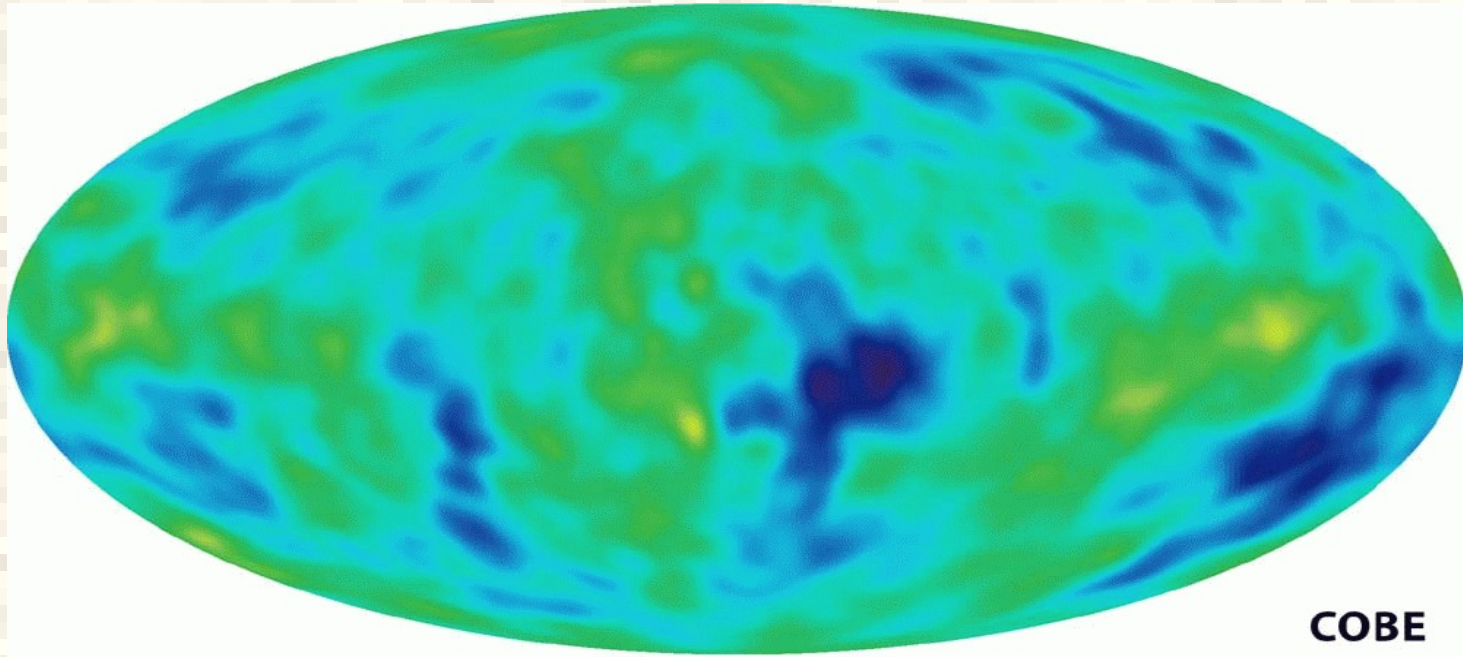
1)



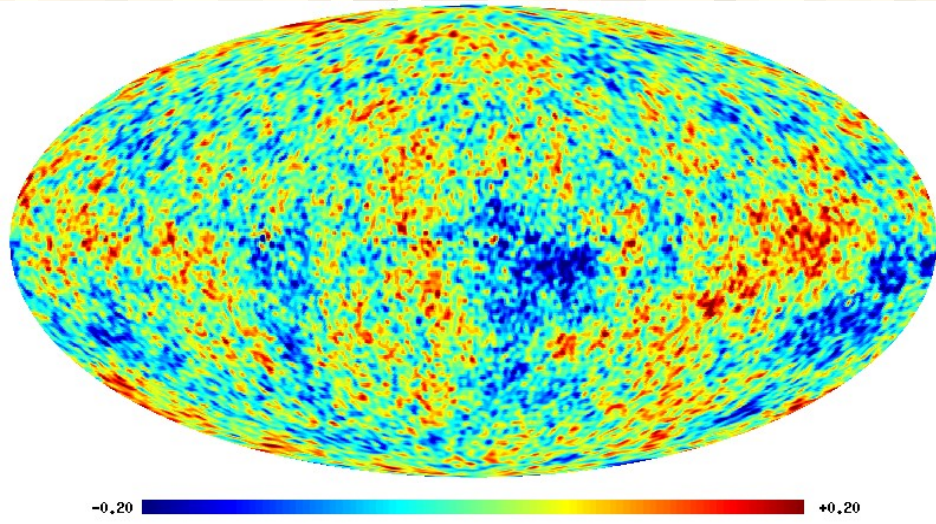
3) Gravitational waves in the B-mode of polarization ?

What do we analyze ?

# Maps

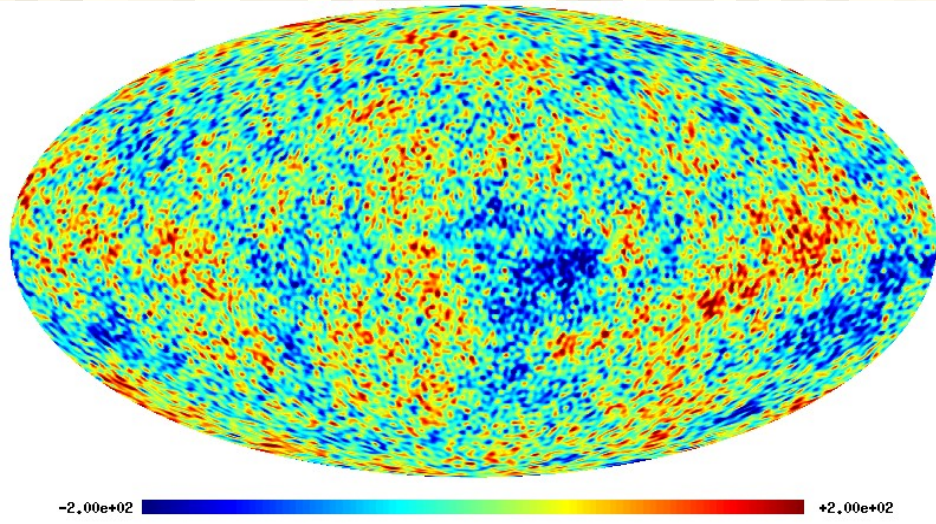


# And more maps

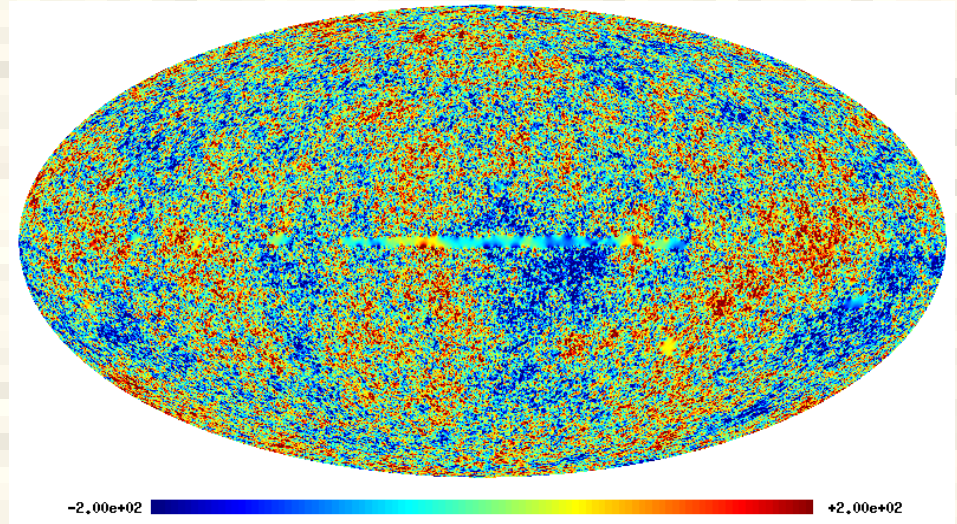


WMAP 9,  $L_{\text{max}}=100$   
(Hinshaw et al., 2012)

Planck collaboration, 2013



Planck,  $L_{\text{max}}=100$

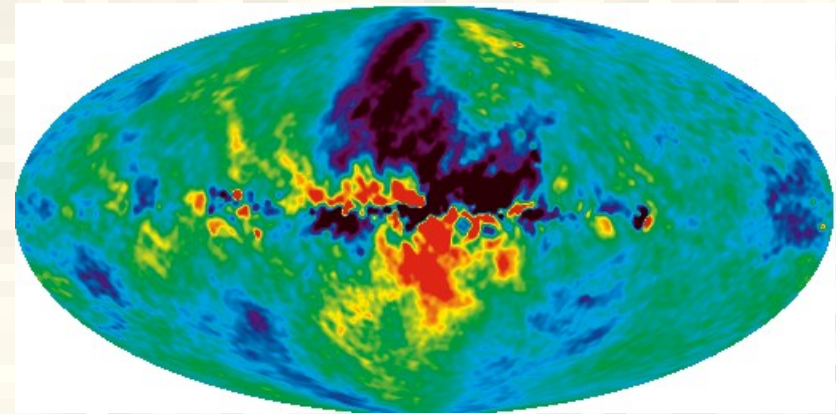
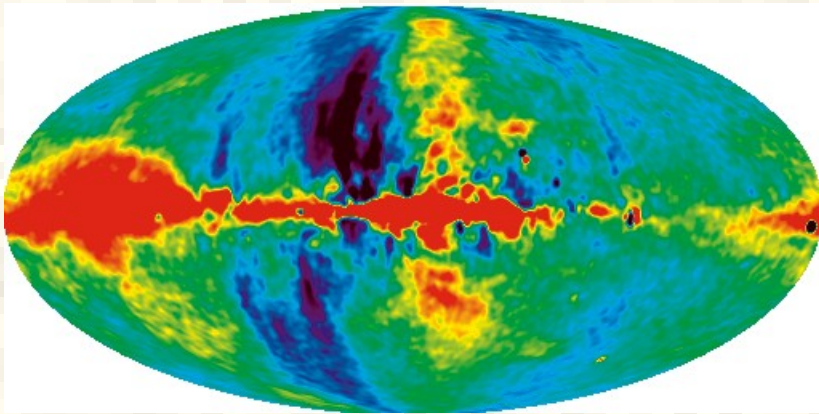


SMICA,  
 $L_{\text{max}} = 2500$



# And polarization WMAP maps too

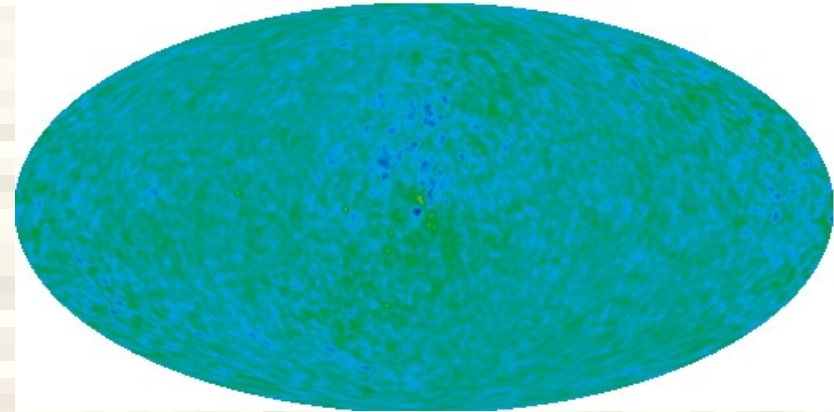
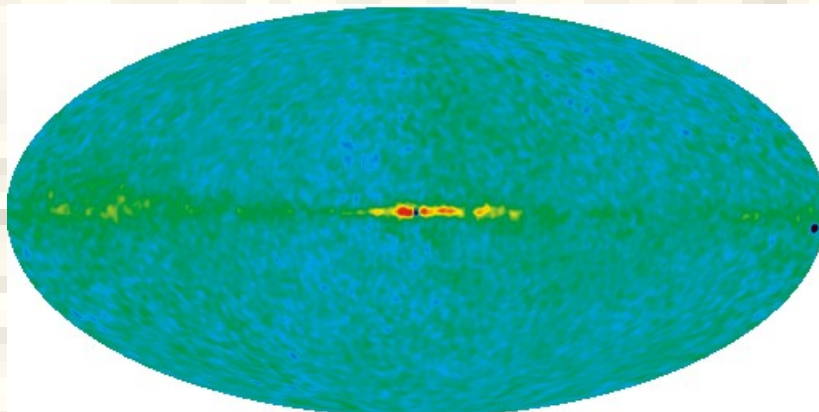
K-band (23 GHz)



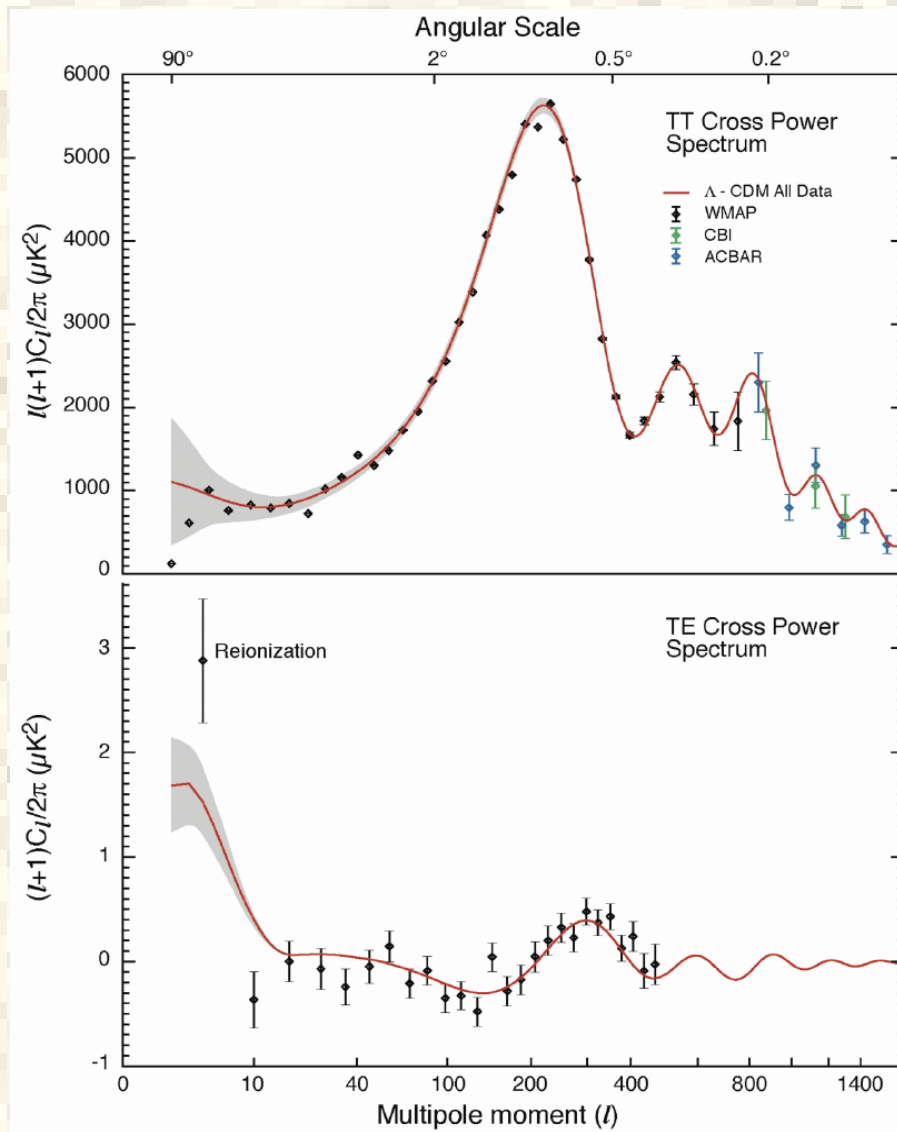
Q

U

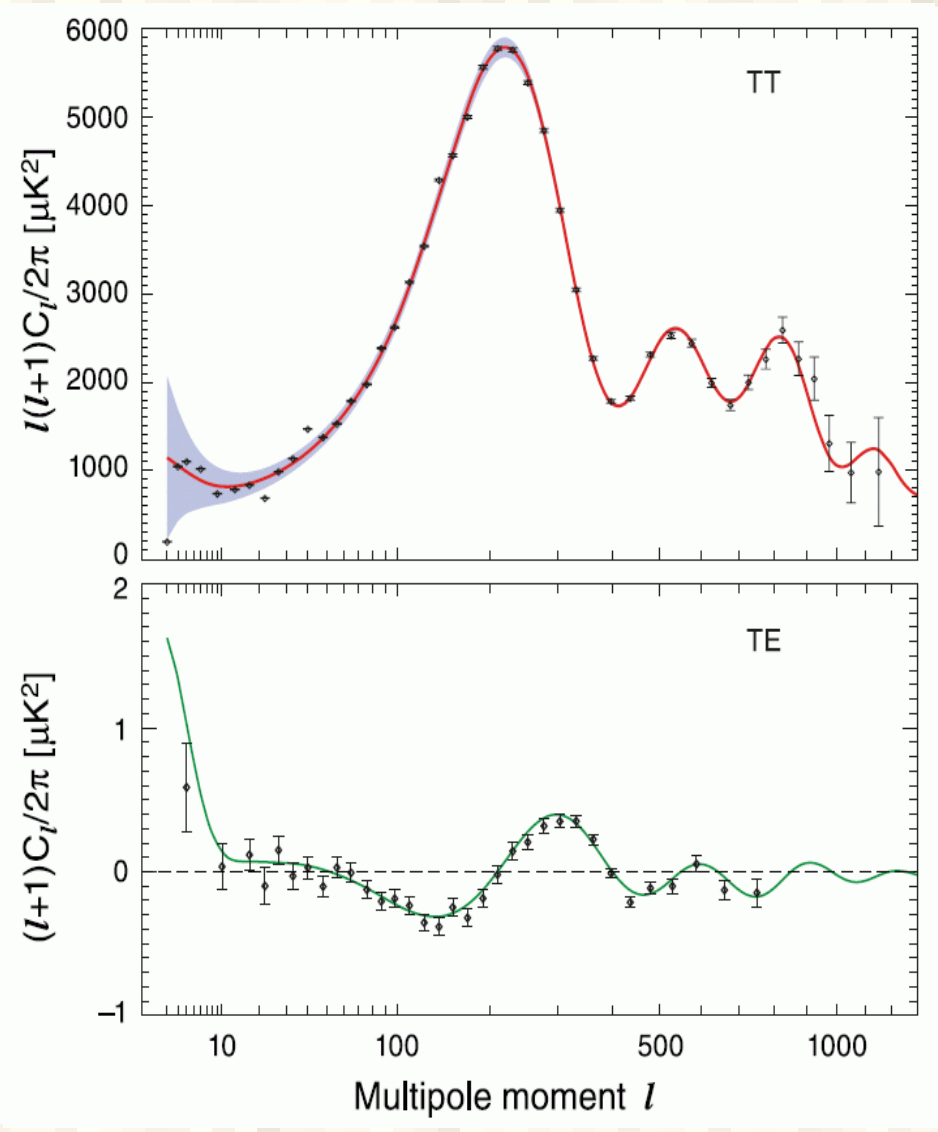
V-band (61 GHz):



# Angular power spectrum of CMB

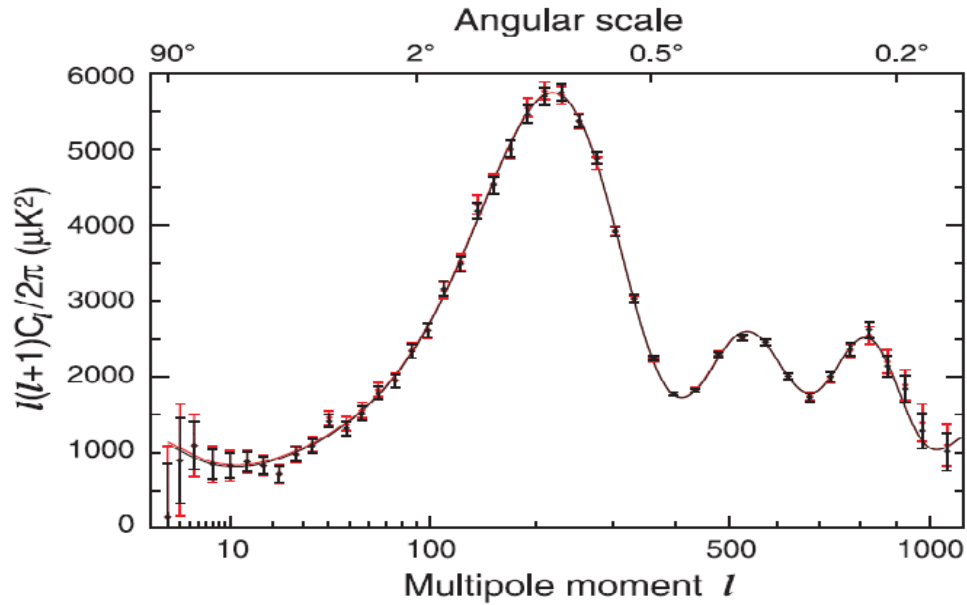


1st year

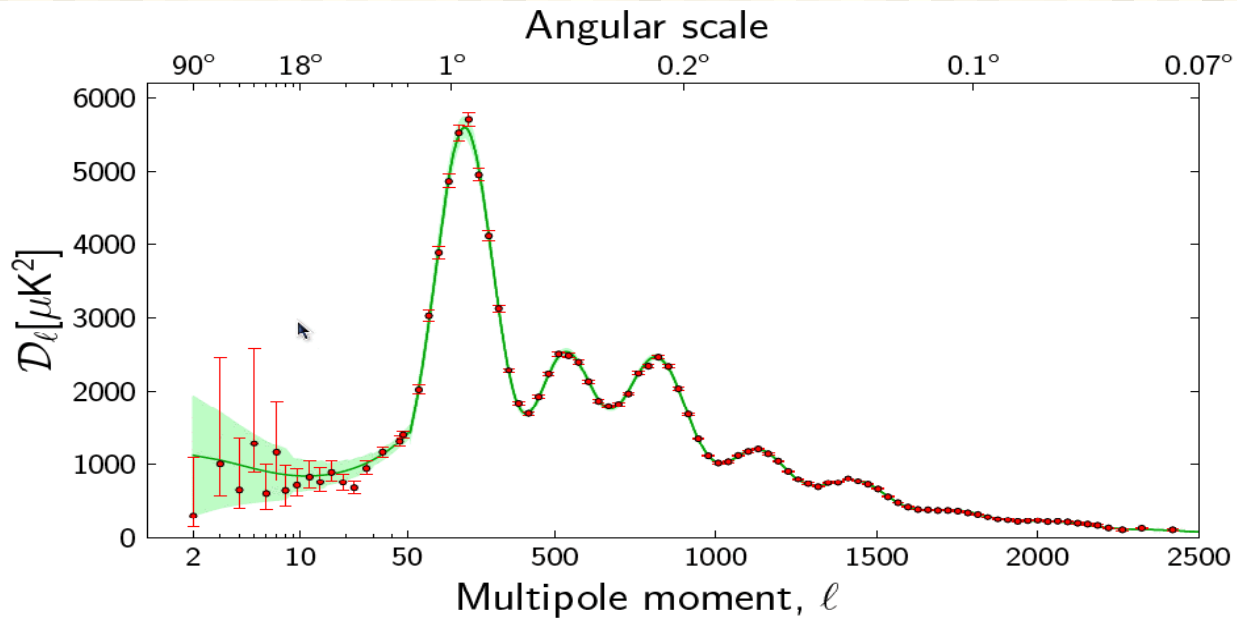


7 years

# And more spectra



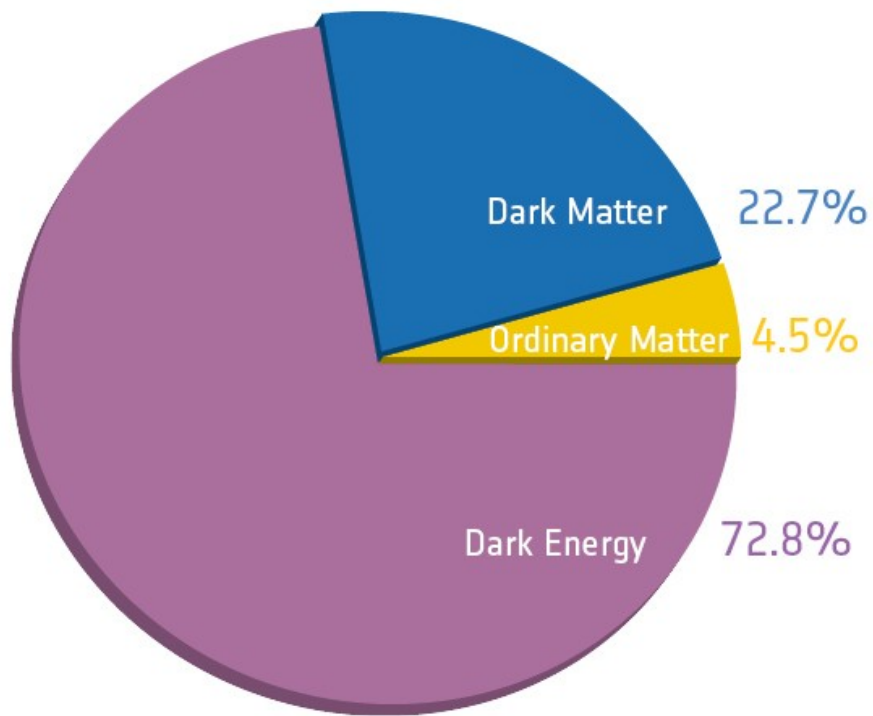
WMAP 9,  
2012



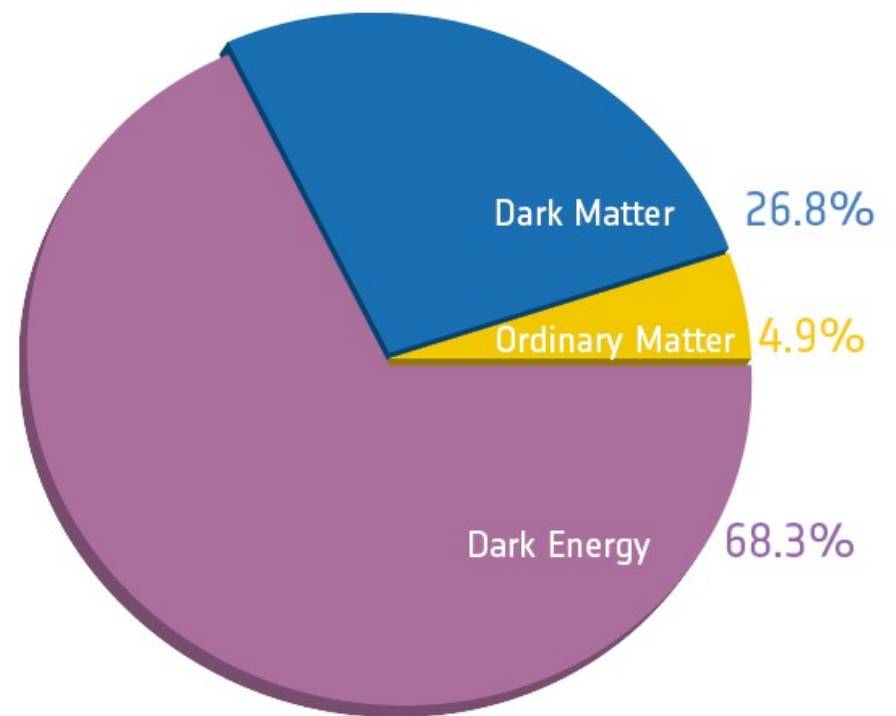
Planck  
2013



Description	Symbol	WMAP -only	WMAP +BAO+ $H_0$
Parameters for Standard $\Lambda$ CDM Model <sup>a</sup>			
Age of universe	$t_0$	$13.75 \pm 0.13$ Gyr	$13.75 \pm 0.11$ Gyr
Hubble constant	$H_0$	$71.0 \pm 2.5$ km/s/Mpc	$70.4_{-1.4}^{+1.3}$ km/s/Mpc
Baryon density	$\Omega_b$	$0.0449 \pm 0.0028$	$0.0456 \pm 0.0016$
Physical baryon density	$\Omega_b h^2$	$0.02258_{-0.00056}^{+0.00057}$	$0.02260 \pm 0.00053$
Dark matter density	$\Omega_c$	$0.222 \pm 0.026$	$0.227 \pm 0.014$
Physical dark matter density	$\Omega_c h^2$	$0.1109 \pm 0.0056$	$0.1123 \pm 0.0035$
Dark energy density	$\Omega_\Lambda$	$0.734 \pm 0.029$	$0.728_{-0.016}^{+0.015}$
Curvature fluctuation amplitude, $k_0 = 0.002$ Mpc <sup>-1</sup> <sup>b</sup>	$\Delta_{\mathcal{R}}^2$	$(2.43 \pm 0.11) \times 10^{-9}$	$(2.441_{-0.092}^{+0.088}) \times 10^{-9}$
Fluctuation amplitude at $8h^{-1}$ Mpc	$\sigma_8$	$0.801 \pm 0.030$	$0.809 \pm 0.024$
Scalar spectral index	$n_s$	$0.963 \pm 0.014$	$0.963 \pm 0.012$
Redshift of matter-radiation equality	$z_{\text{eq}}$	$3196_{-133}^{+134}$	$3232 \pm 87$
Angular diameter distance to matter-radiation eq. <sup>c</sup>	$d_A(z_{\text{eq}})$	$14281_{-161}^{+158}$ Mpc	$14238_{-129}^{+128}$ Mpc
Redshift of decoupling	$z_*$	$1090.79_{-0.92}^{+0.94}$	$1090.89_{-0.69}^{+0.68}$
Age at decoupling	$t_*$	$379164_{-5243}^{+5187}$ yr	$377730_{-3200}^{+3205}$ yr
Angular diameter distance to decoupling <sup>c,d</sup>	$d_A(z_*)$	$14116_{-163}^{+160}$ Mpc	$14073_{-130}^{+129}$ Mpc
Sound horizon at decoupling <sup>d</sup>	$r_s(z_*)$	$146.6_{-1.6}^{+1.5}$ Mpc	$146.2 \pm 1.1$ Mpc
Acoustic scale at decoupling <sup>d</sup>	$l_A(z_*)$	$302.44 \pm 0.80$	$302.40 \pm 0.73$
Reionization optical depth	$\tau$	$0.088 \pm 0.015$	$0.087 \pm 0.014$
Redshift of reionization	$z_{\text{reion}}$	$10.5 \pm 1.2$	$10.4 \pm 1.2$
Parameters for Extended Models <sup>e</sup>			
Total density <sup>f</sup>	$\Omega_{\text{tot}}$	$1.080_{-0.071}^{+0.093}$	$1.0023_{-0.0054}^{+0.0056}$
Equation of state <sup>g</sup>	$w$	$-1.12_{-0.43}^{+0.42}$	$-0.980 \pm 0.053$
Tensor to scalar ratio, $k_0 = 0.002$ Mpc <sup>-1</sup> <sup>b,h</sup>	$r$	$< 0.36$ (95% CL)	$< 0.24$ (95% CL)
Running of spectral index, $k_0 = 0.002$ Mpc <sup>-1</sup> <sup>b,i</sup>	$dn_s/d \ln k$	$-0.034 \pm 0.026$	$-0.022 \pm 0.020$
Neutrino density <sup>j</sup>	$\Omega_\nu h^2$	$< 0.014$ (95% CL)	$< 0.0062$ (95% CL)
Neutrino mass <sup>j</sup>	$\sum m_\nu$	$< 1.3$ eV (95% CL)	$< 0.58$ eV (95% CL)
Number of light neutrino families <sup>k</sup>	$N_{\text{eff}}$	$> 2.7$ (95% CL)	$4.34_{-0.88}^{+0.86}$



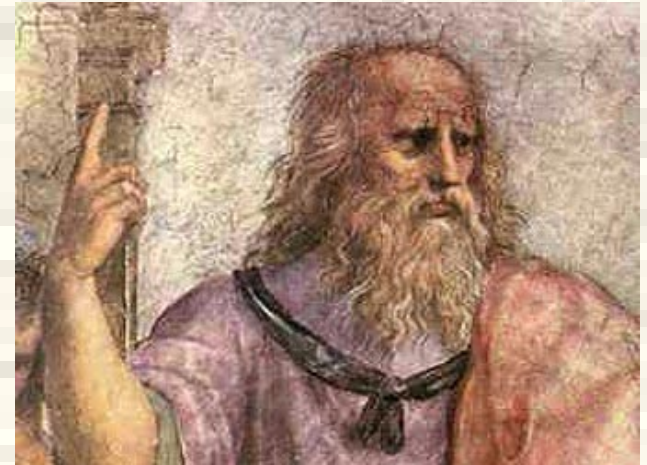
Before Planck



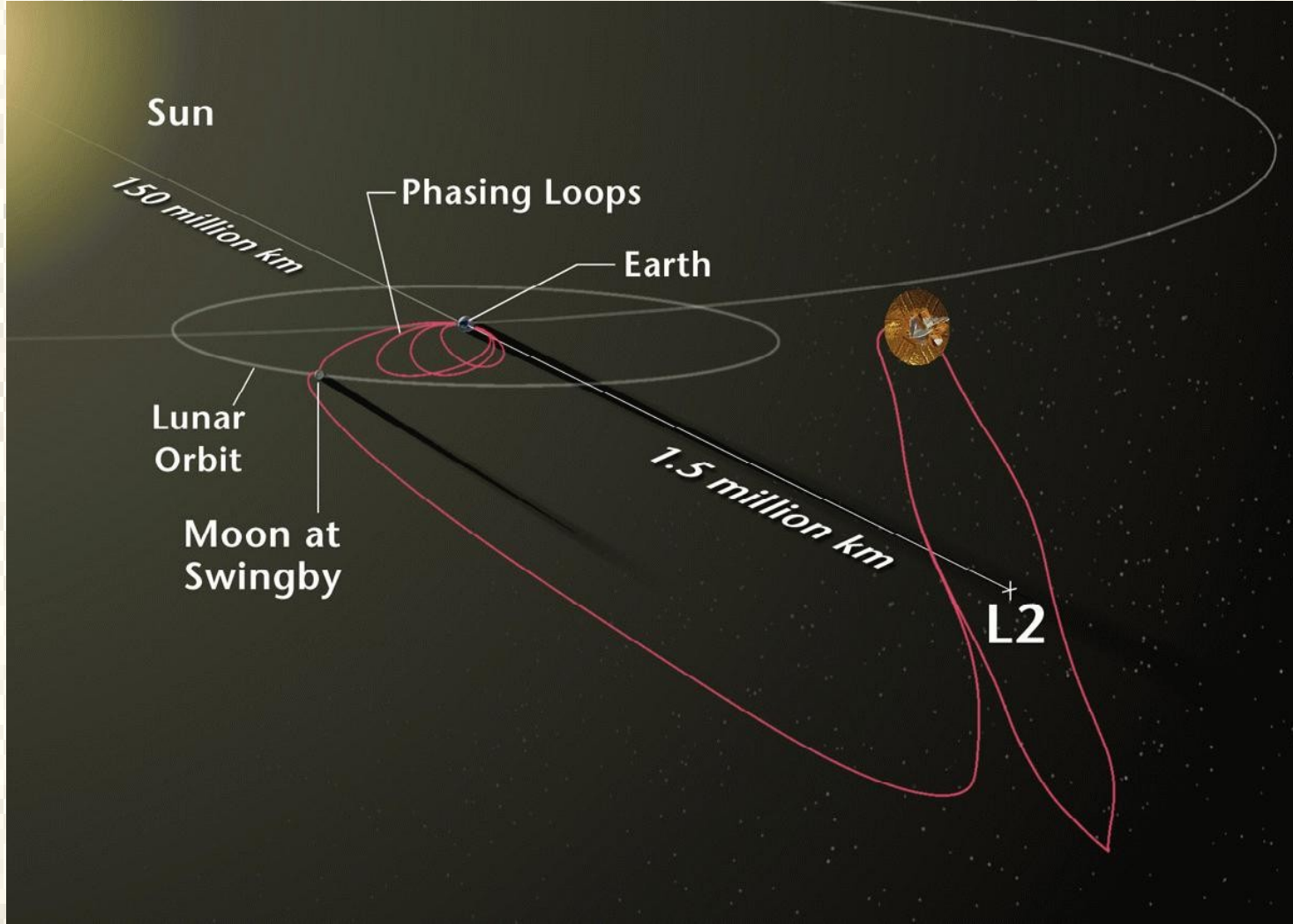
After Planck

# How to investigate ?

- 1) Theory
- 2) Observations
- 3) Simulation



How to observe ?





# Data analysis of CMB

- Registration: time ordered data:  $T(t)=T(l,b)$
- Pixelization: map-making and restoration data in pixels
- Component separation
- Multipole analysis
- Pixel statistics of the CMB map
- Angular power spectrum analysis and determination of cosmological parameters

## Map-making procedure

$$\mathbf{d} = P\mathbf{m} + \mathbf{n}$$

$\mathbf{d}$  is the TOD,  $\mathbf{m}$  is the map of pixels

$P$  is the pointinx matrix of  $(Nd, Np)$  elements

To estimate  $\mathbf{m}$ , the GLS method is used

$$\chi^2 = \mathbf{n}^T V \mathbf{n} = (\mathbf{d}^T - \mathbf{m}^T P^T) V (\mathbf{d} - P\mathbf{m})$$

$V$  minimizes variance of estimation of  $\mathbf{m}$ ,  
taking noise inverse covariance matrix:

$$V^{-1} = N \equiv \langle \mathbf{nn}^T \rangle$$

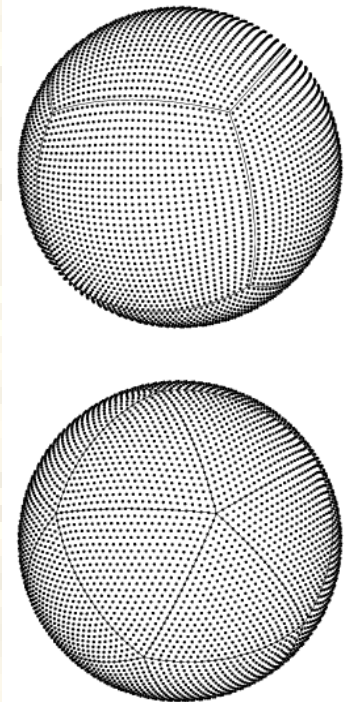
# Pixelization

Integration on a sphere: S.L.Sobolev (1974)

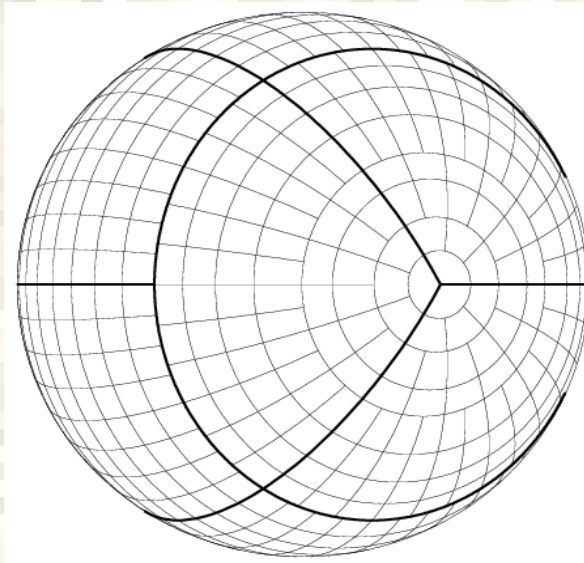
Some pixelization schemes:

- 1) Icosahedron (Tegmark, 1996)
- 2) Igloo (Crittenden, Turok, 1998)
- 3) HEALPix (Gorski et al., 1999)

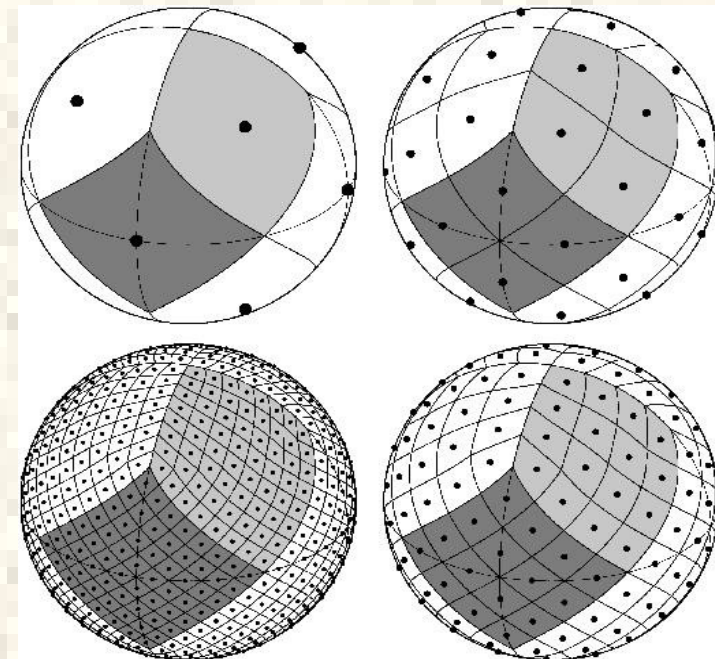
(1)



(2)

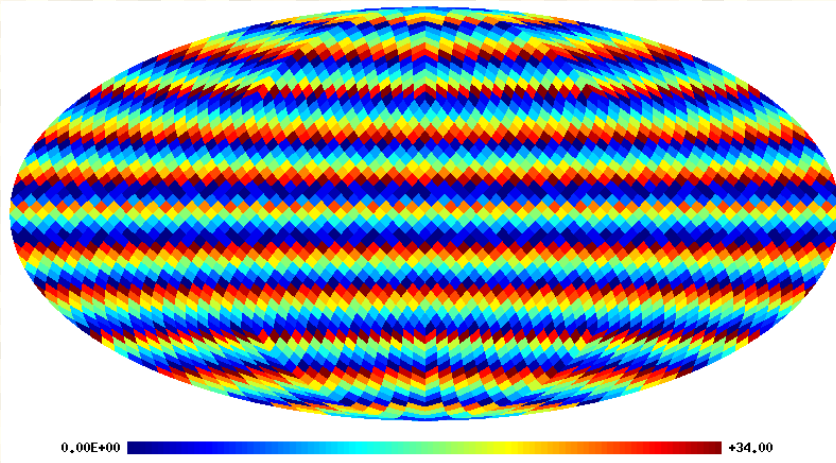


(3)



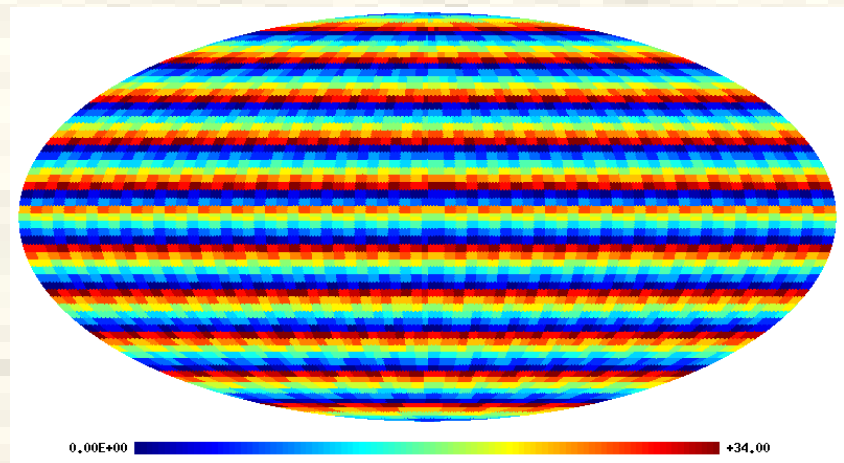
# Packages for 2 schemes

HEALPix



Hierarchical scheme  
pixel calculations  
Based on  $12 \cdot 2^n$  equal pixels  
(Gorski et al., 1993, 2005)

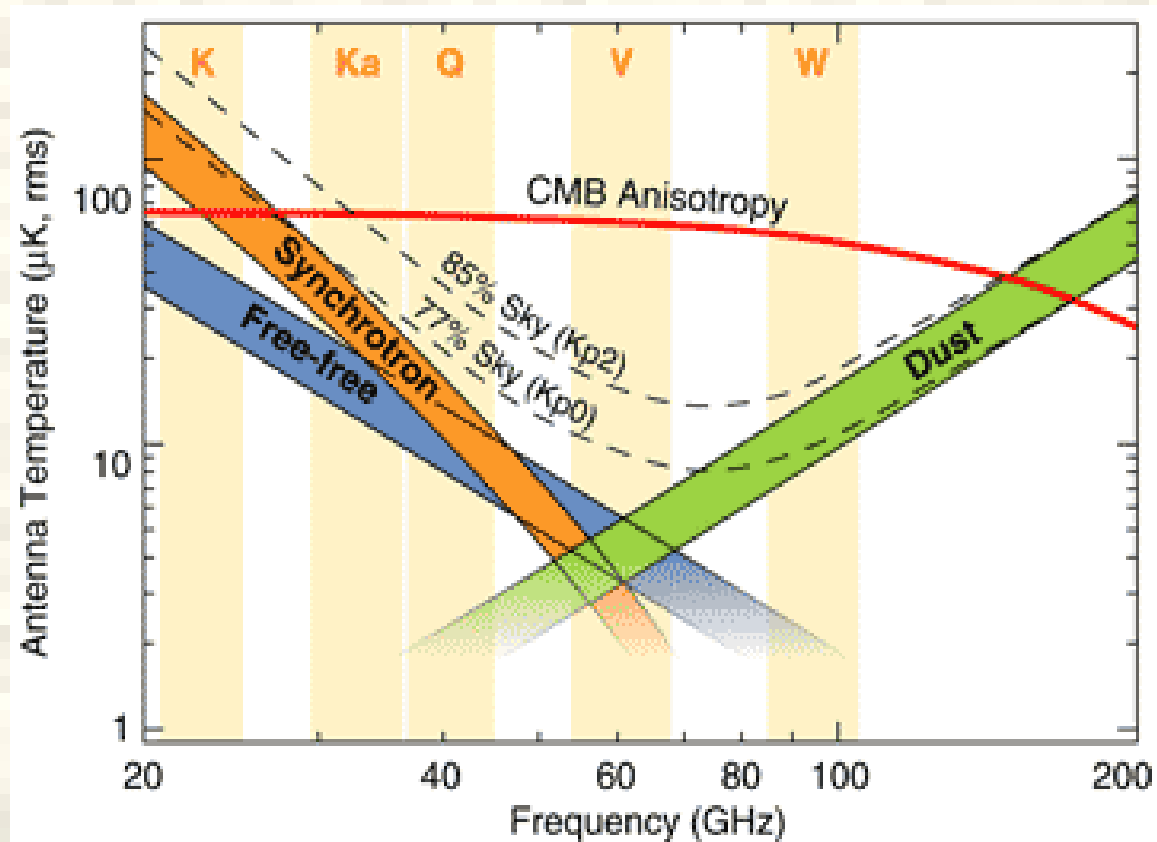
GLESP



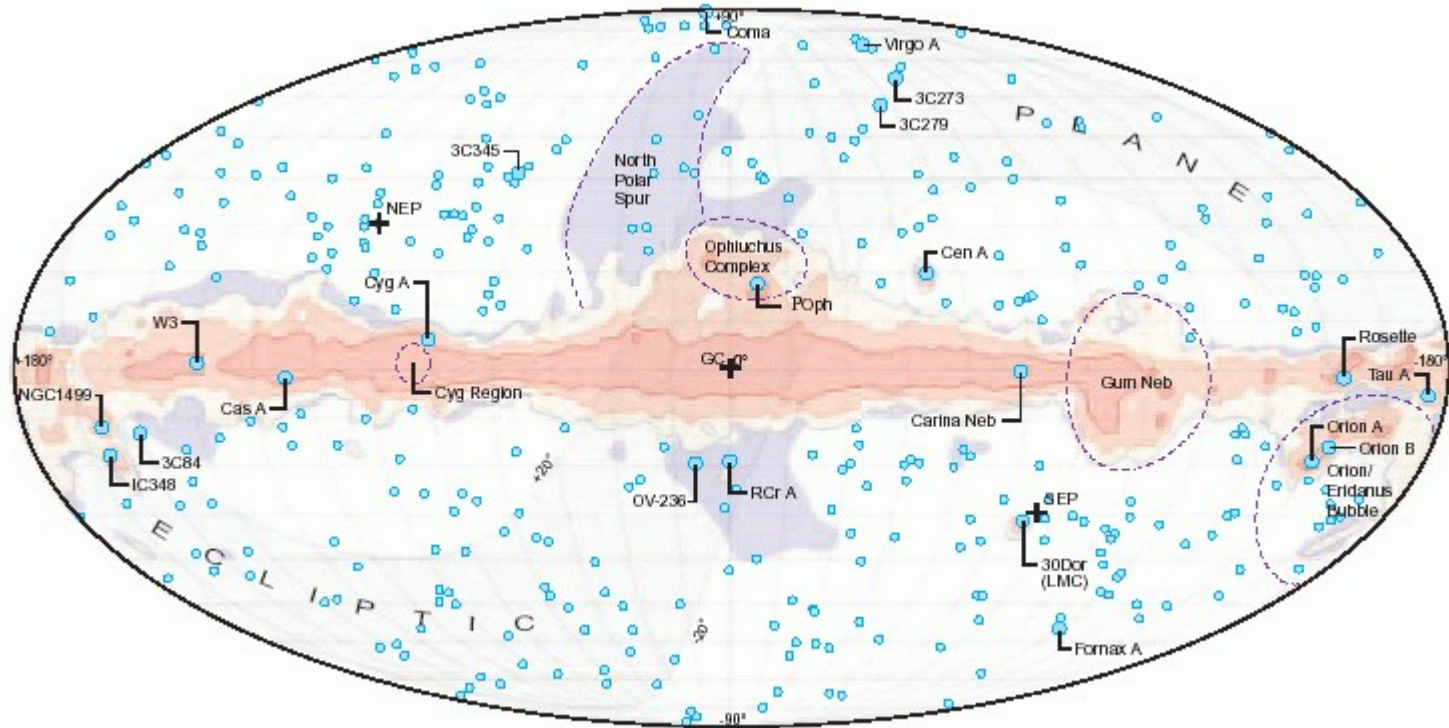
Non-hierarchical scheme  
harmonic calculations  
Based on gaussian quadrature  
(Doroshkevich et al., 2005)

# Component separation

# Emission components (WMAP)

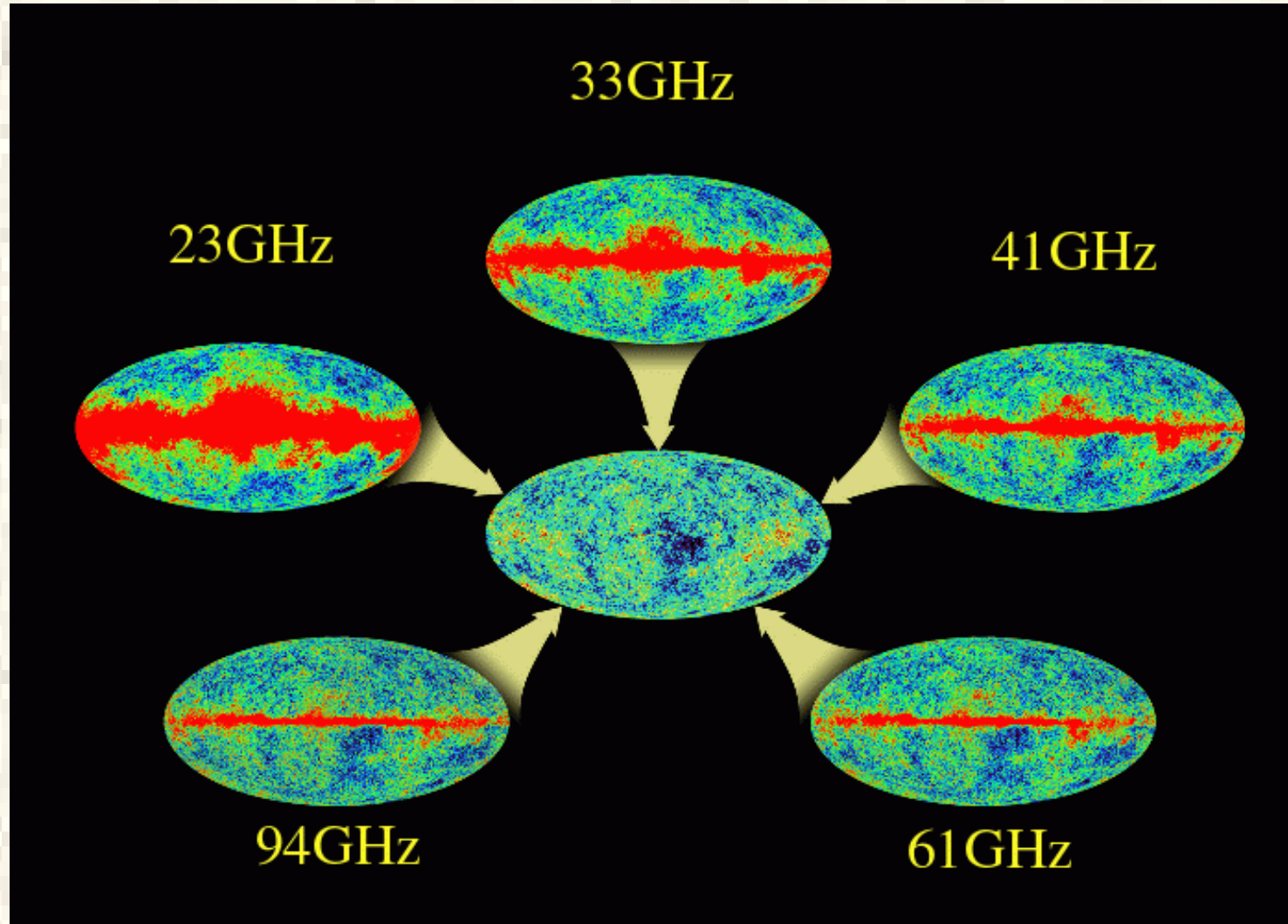


# Radio sources



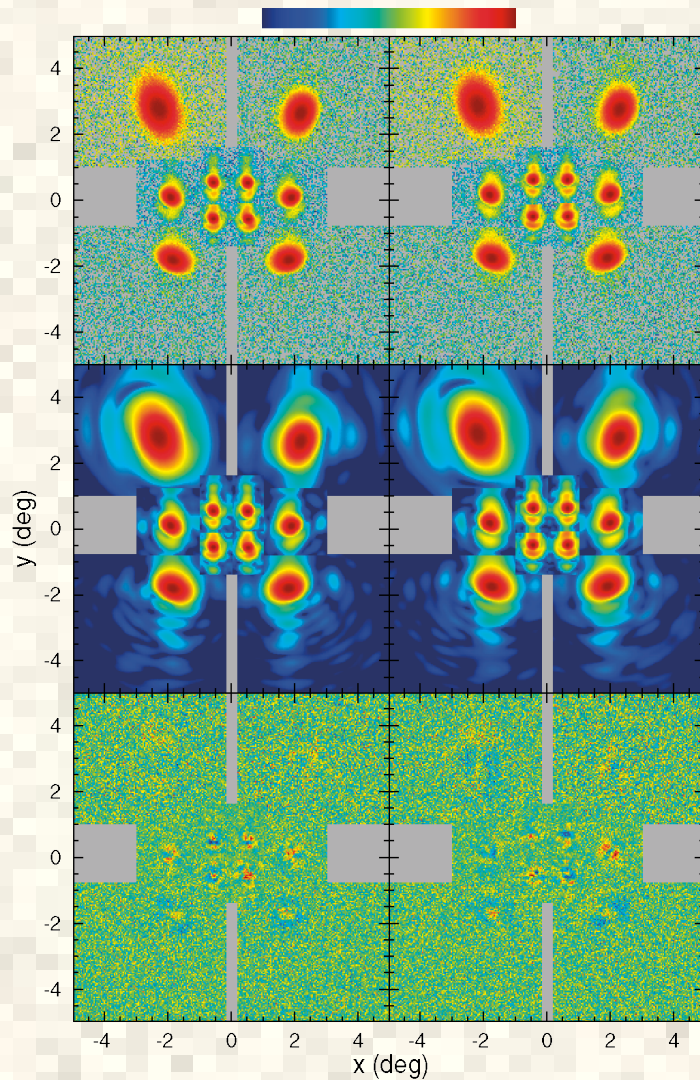
# Component separation:

Signal = (CMB + Synchrotron + dust + FreeFree + CO + radiosources) \* Beam + Noise





# WMAP beams



Degrees:  
0.88 (K),  
0.66 (Ka),  
0.51 (Q),  
0.35 (V),  
0.22 (W)

# CMB restoration

## **Two basic properties of CMB:**

- 1) Black body emission — same temperature at all wavelengthes;
- 2) Correlation of CMB and foregrounds should be close to zero: because CMB is a random gaussian process



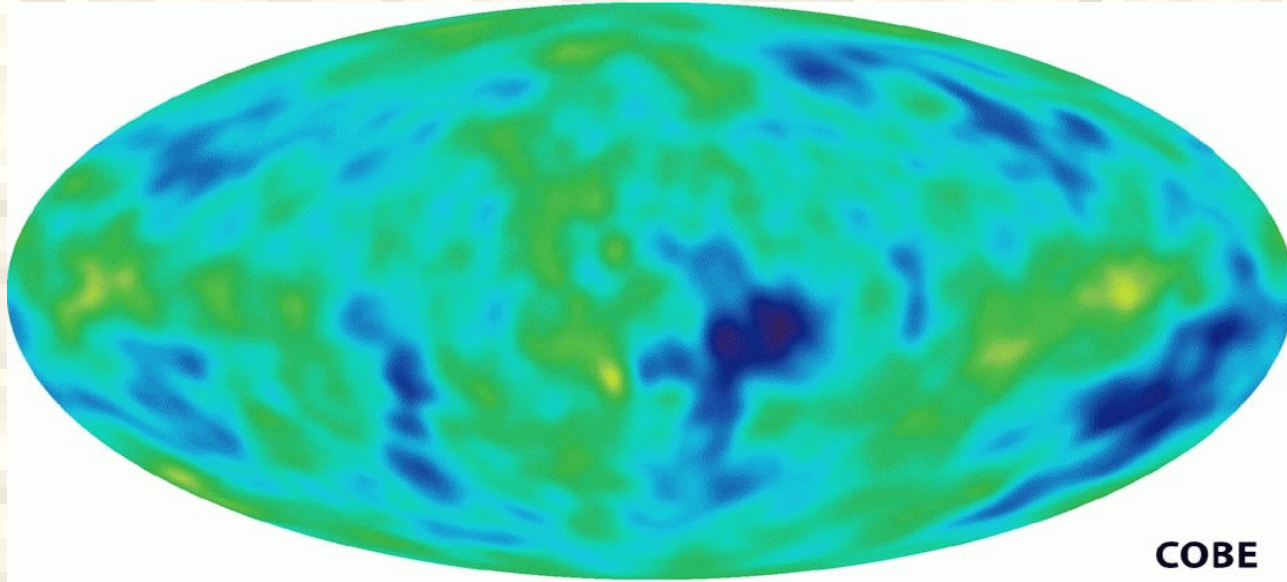
What is the CMB (ILC) map ?

$$\sum_k w_k = 1 \text{ and } Var(c_j) \rightarrow \min(w_k).$$

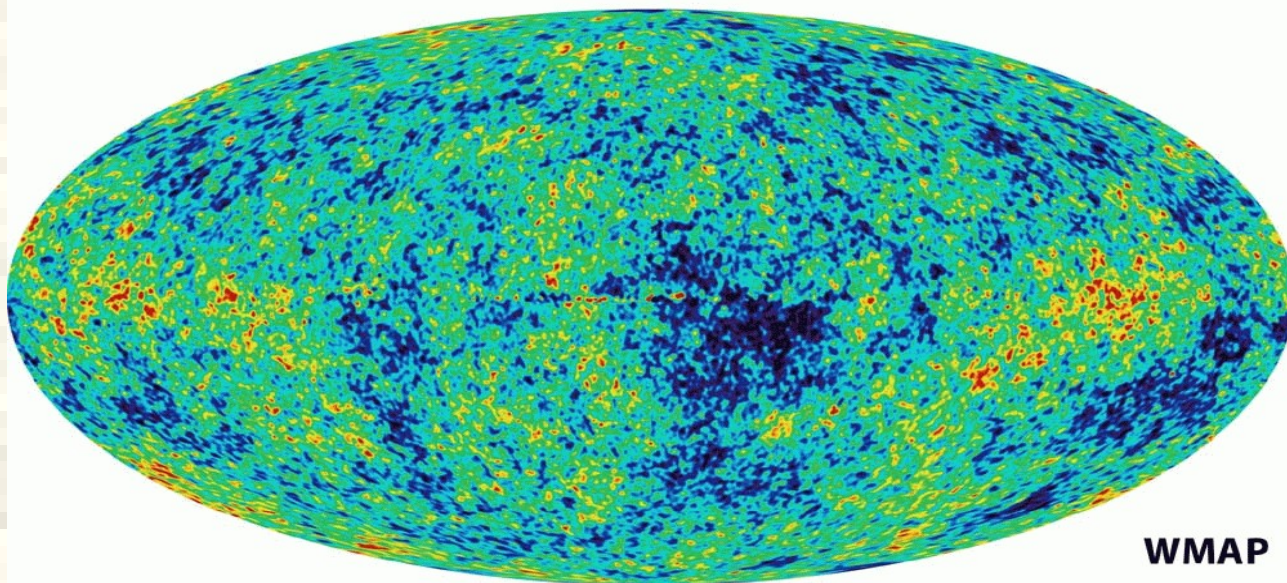
$$c_p = T(\theta_j, \phi_p, \nu_k) - \sum_{i=1}^{J-1} w_p (T(\theta_p, \phi_p, \nu_k) - T(\theta_p, \phi_p, \nu_i)),$$

$$Var(c_p) = \frac{1}{N_{tot}} \sum_{p \in \mathfrak{R}} [c_p - \langle c_p \rangle]^2, \quad \frac{\delta Var(c_p)}{\delta w_j} = 0$$

# NASA maps



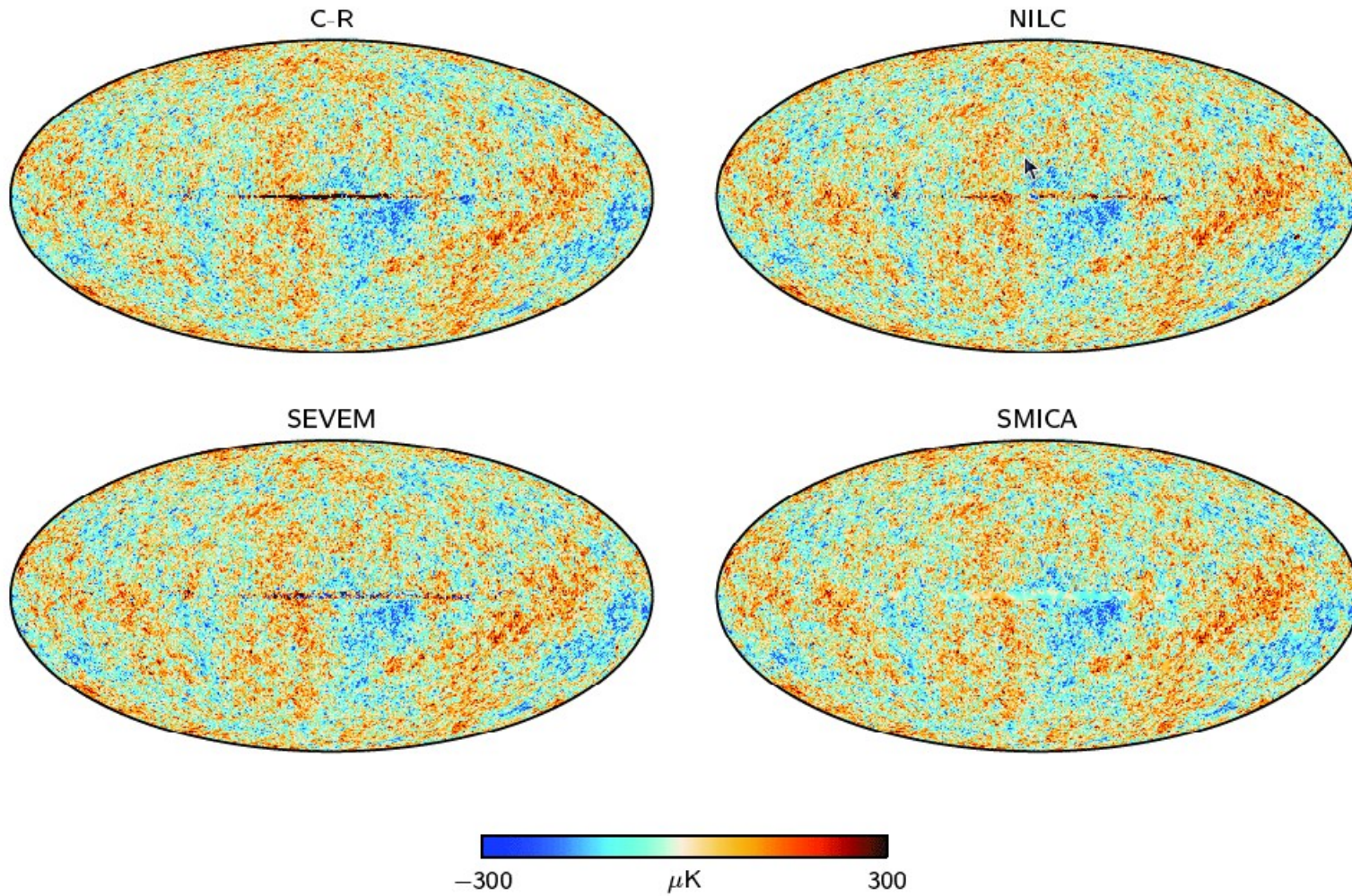
**COBE**



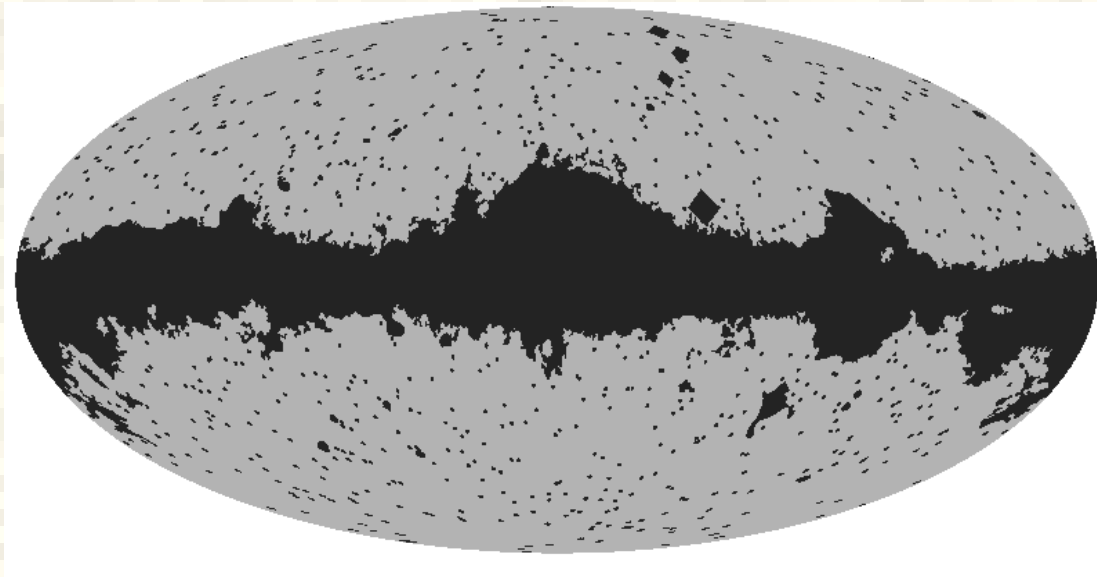
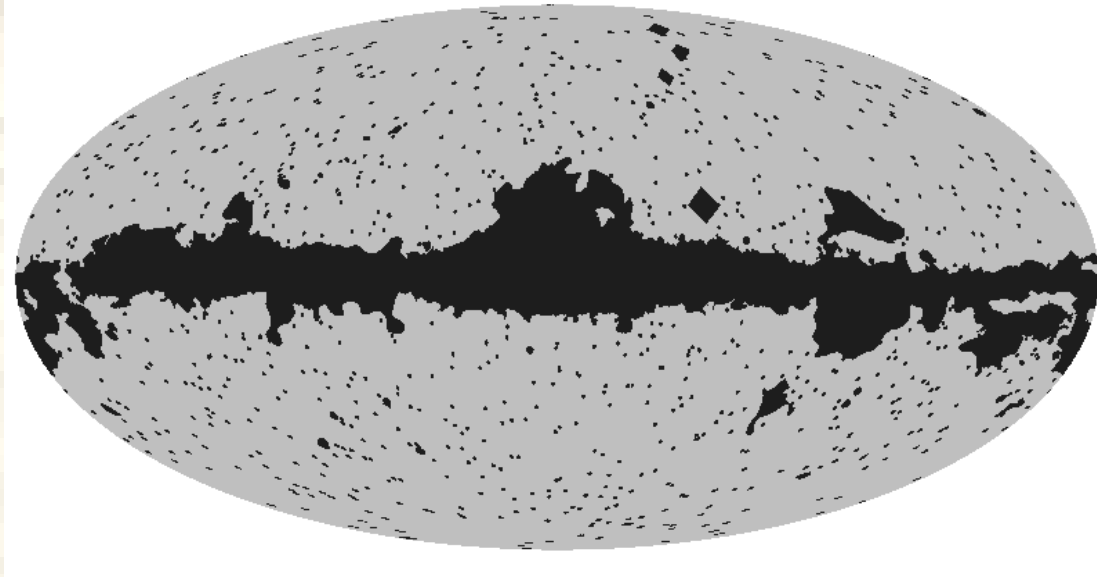
**WMAP**

# And Planck maps

*Planck* Collaboration: *Planck* 2013 results. XII. Component separation



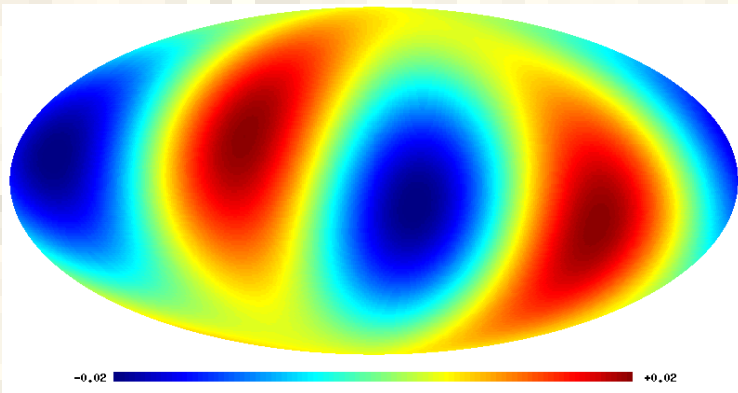
# Masks



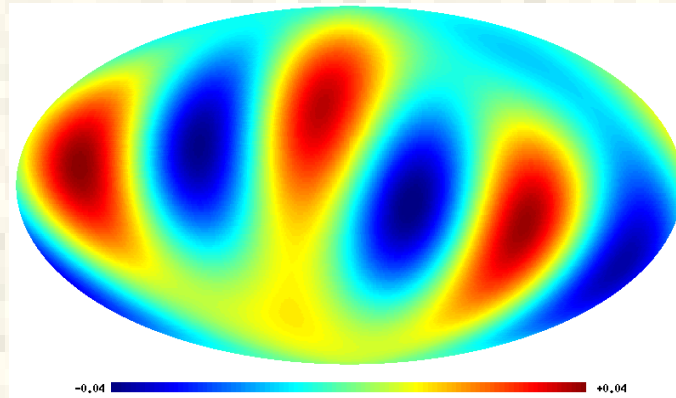
# Multipole expansion

# Multipole expansion

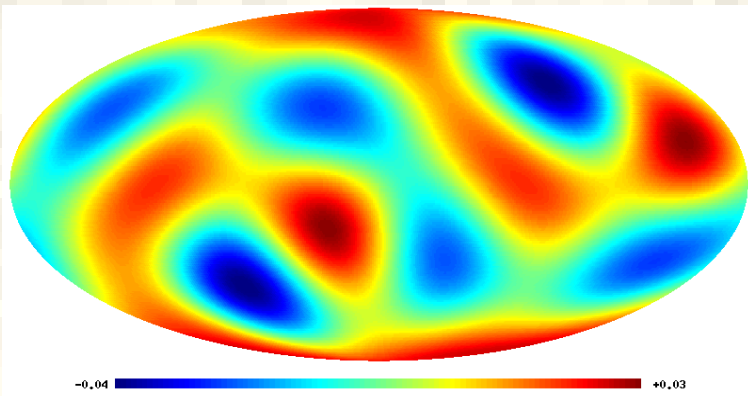
$$\Delta T(\theta, \phi) = \sum_{l=2}^{\infty} \sum_{m=-l}^{m=l} a_{l,m} Y_{l,m}(\theta, \phi)$$



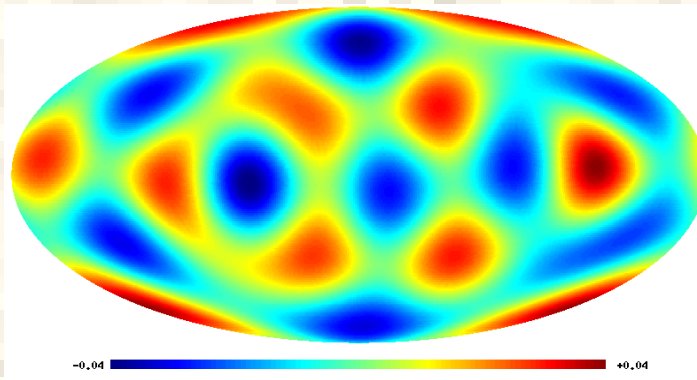
L = 2 (quadrupole)



L = 3 (octupole)



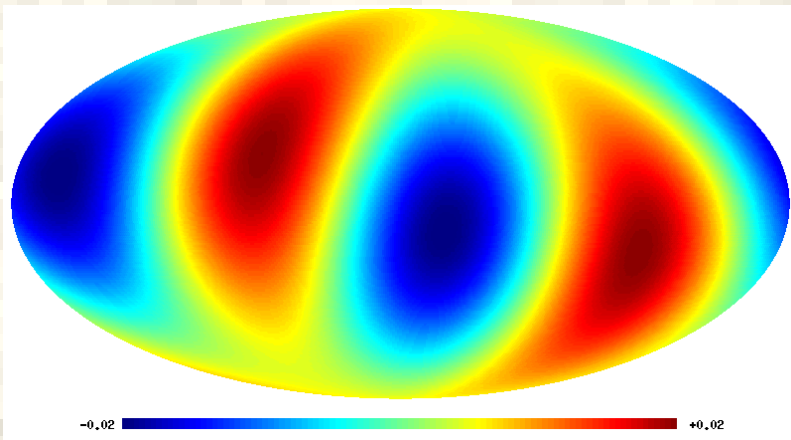
L = 4



L = 5

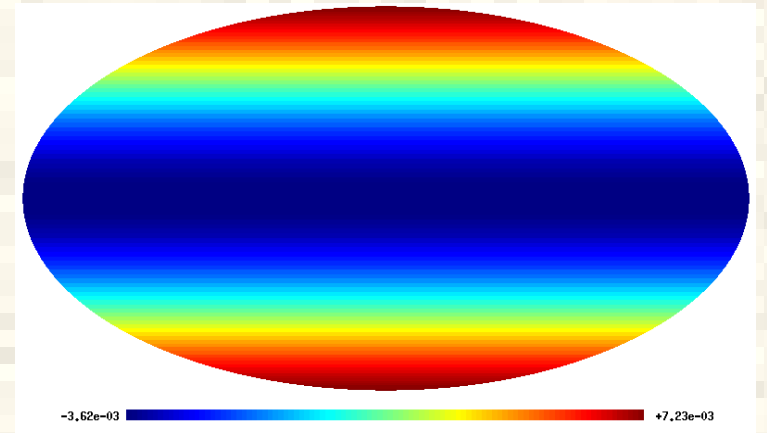


# Quadrupole



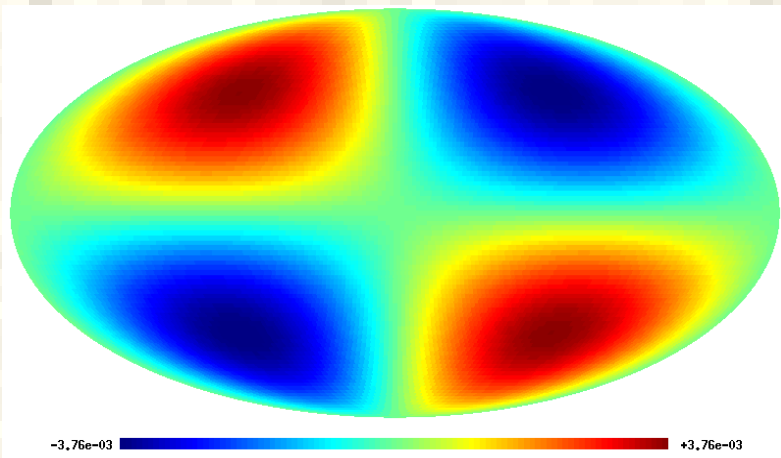
$L=2$

$= a_{20}$



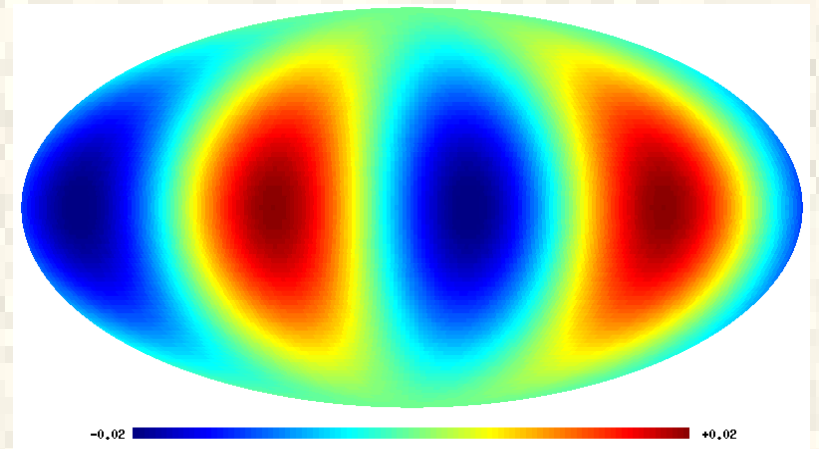
$(2,0)$

$+ a_{21}$



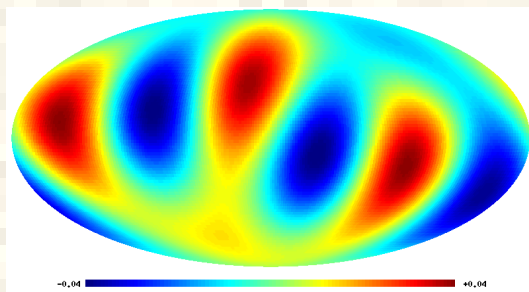
$(2,1)$

$+ a_{22}$



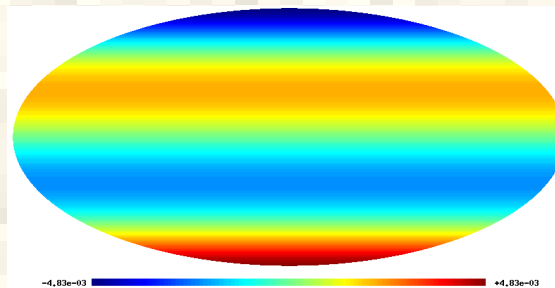
$(2,2)$

# Octupole



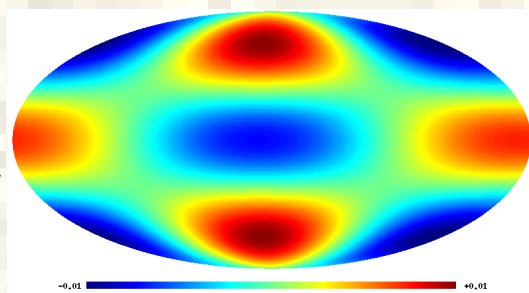
$L=3$

$= a_{30}$



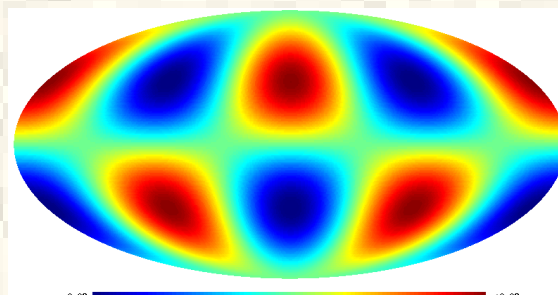
$(3,0)$

$+$



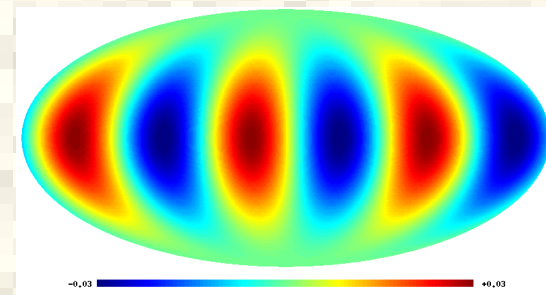
$(3,1)$

$+$   $a_{32}$



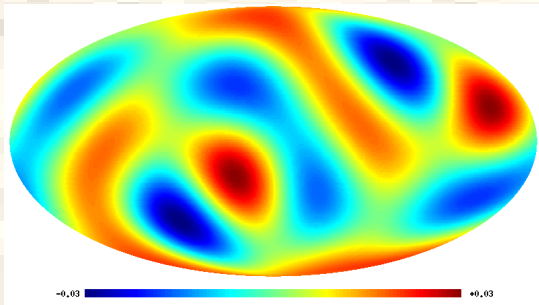
$(3,2)$

$+$   $a_{33}$



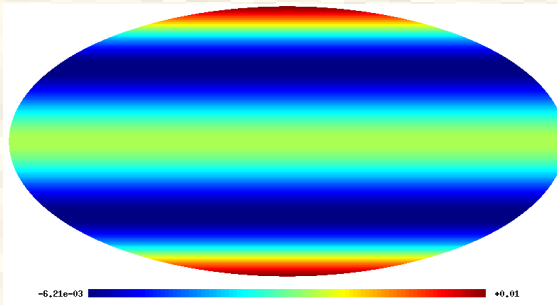
$(3,3)$

$L=4$



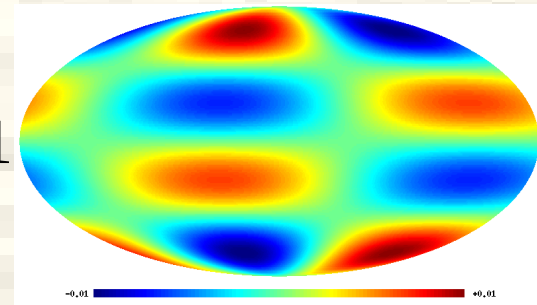
$L=4$

$= a_{40}$

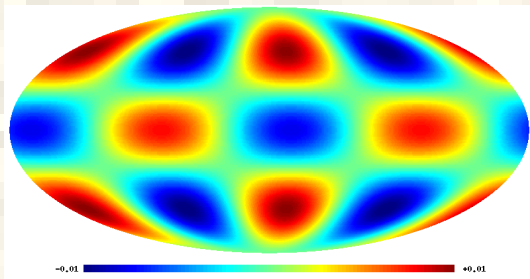


$(4,0)$

$+ a_{41}$

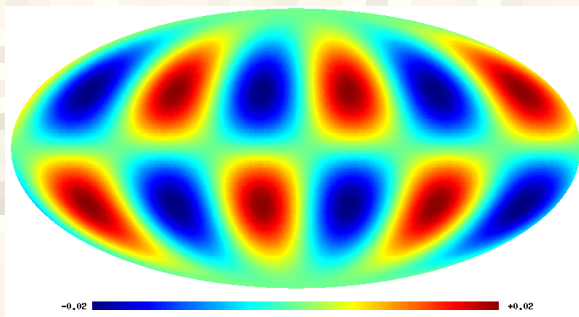


$(4,1)$



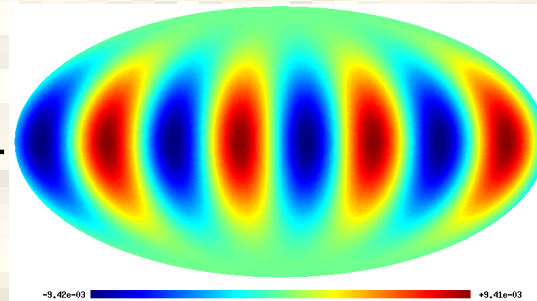
$(4,2)$

$+ a_{43}$



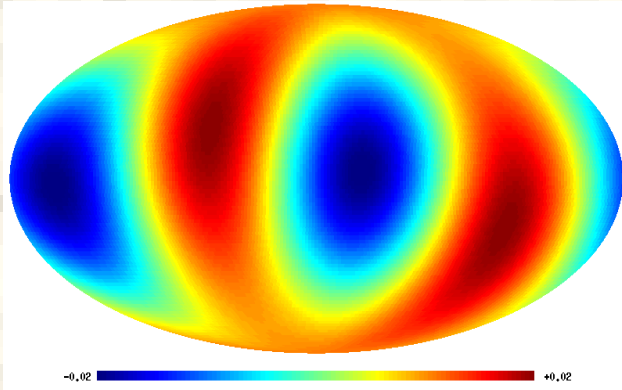
$(4,3)$

$+ a_{44}$

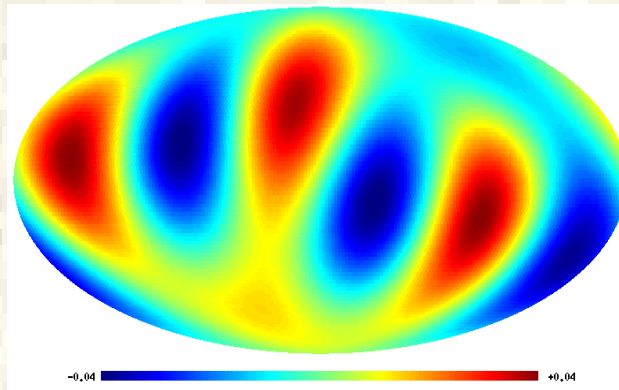


$(4,4)$

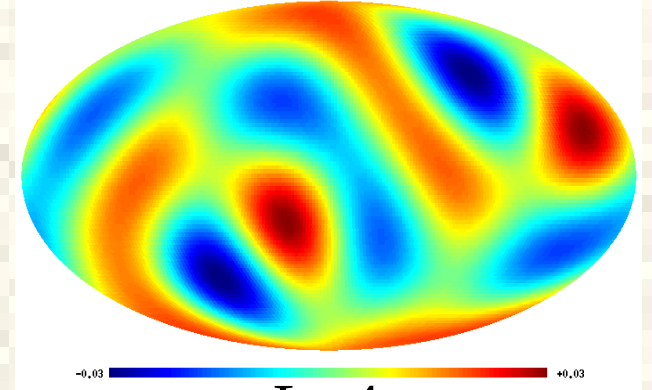
# Low multipoles



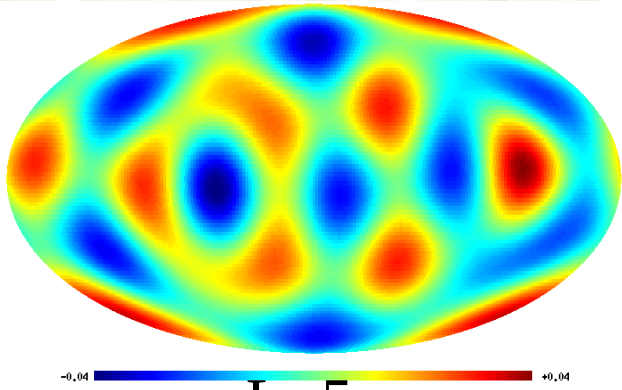
L=2



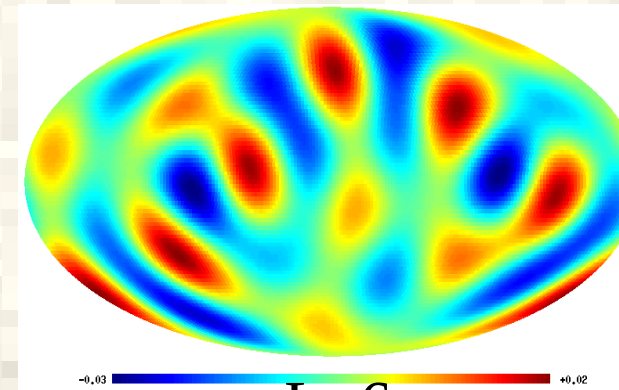
L=3



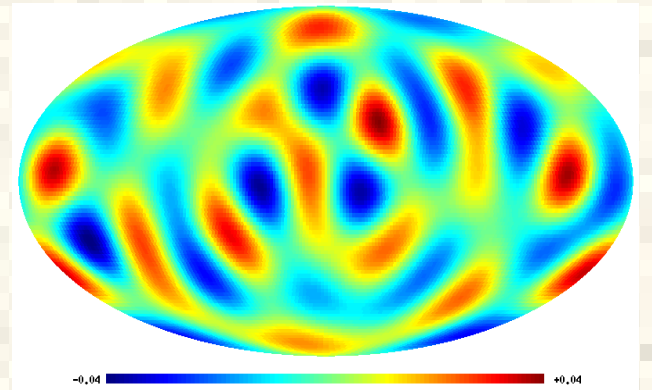
L=4



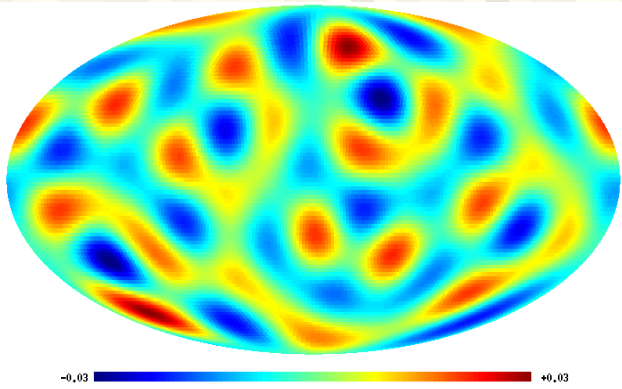
L=5



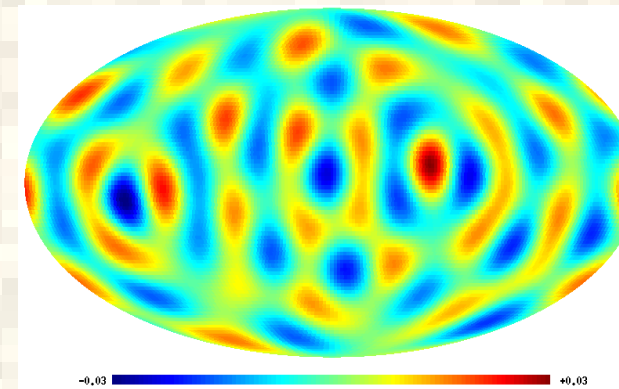
L=6



L=7



L=8



L=9

# Formation of anisotropy:

Density perturbations arised in form of sound waves  
(*A. Sakharov, 1965*)

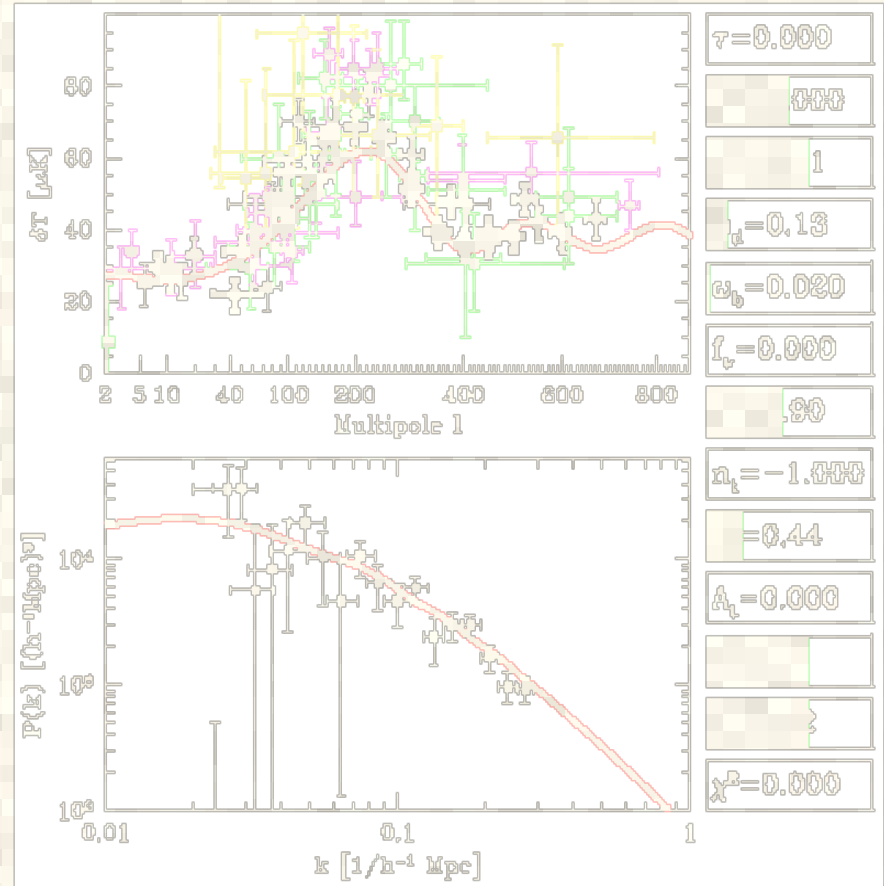
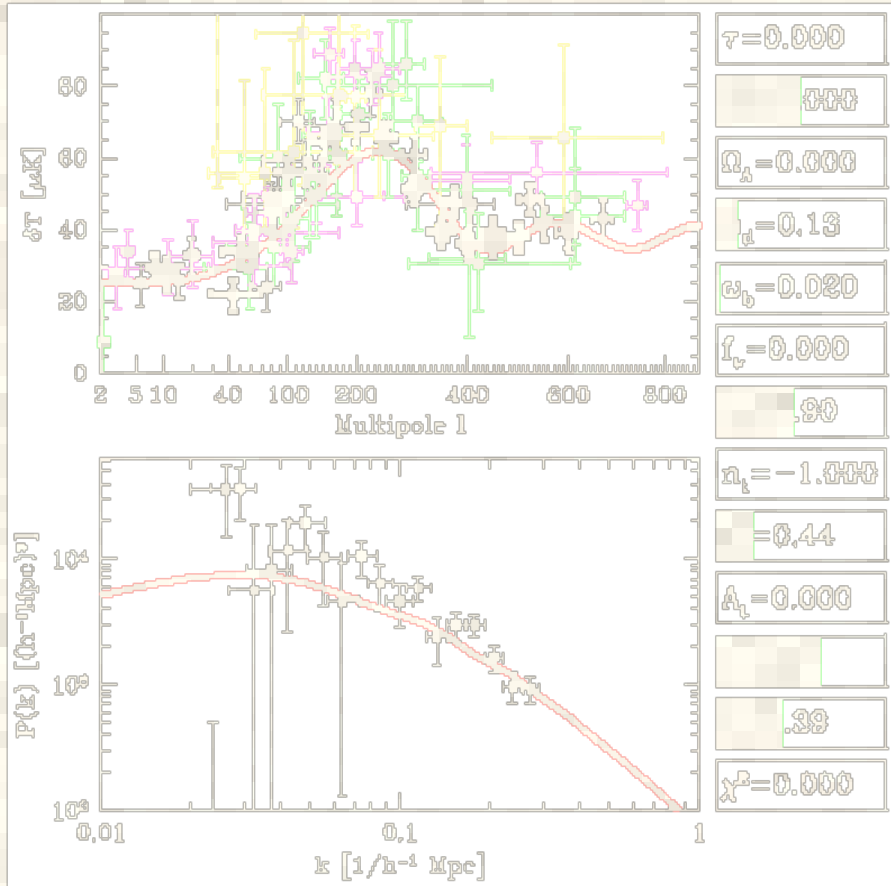
$$a_{\ell m} = 4(-i)^\ell \int \frac{d^3\mathbf{k}}{(2\pi)^3} \Phi(\mathbf{k}) g_{T\ell}(\mathbf{k}) Y_{\ell}^* m(\hat{\mathbf{k}})$$

# Angular power spectrum of CMB anisotropy

$$C_\ell \equiv C_\ell(h, \Omega_b h^2, \Omega_{CDM} h^2, \Omega_\Lambda, \Omega_\nu, n, \dots)$$

CMBfast: *Seljak & Zaltariaga, 1997*

CAMB: *Lewis, Challinor, Lasenby, 2000*



# Angular power spectrum of CMB anisotropy

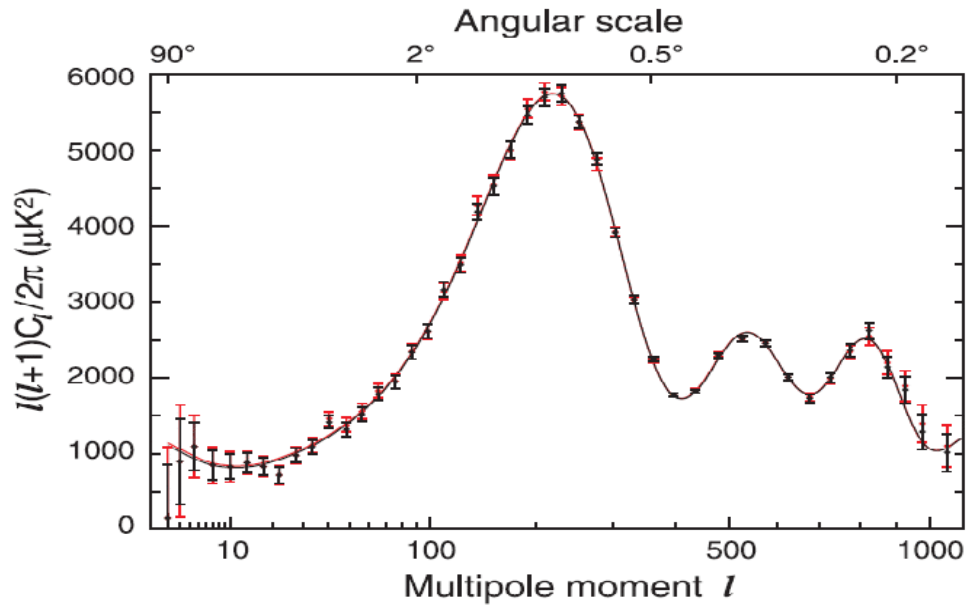
$$C(l) = \frac{1}{2l + 1} \left[ |a_{l0}|^2 + 2 \sum_{m=1}^l |a_{l,m}|^2 \right]$$

$$a_{l,m} = \int_{-1}^1 dx \int_0^{2\pi} d\phi \Delta T(\theta, \phi) Y_{l,m}^*(x, \phi)$$

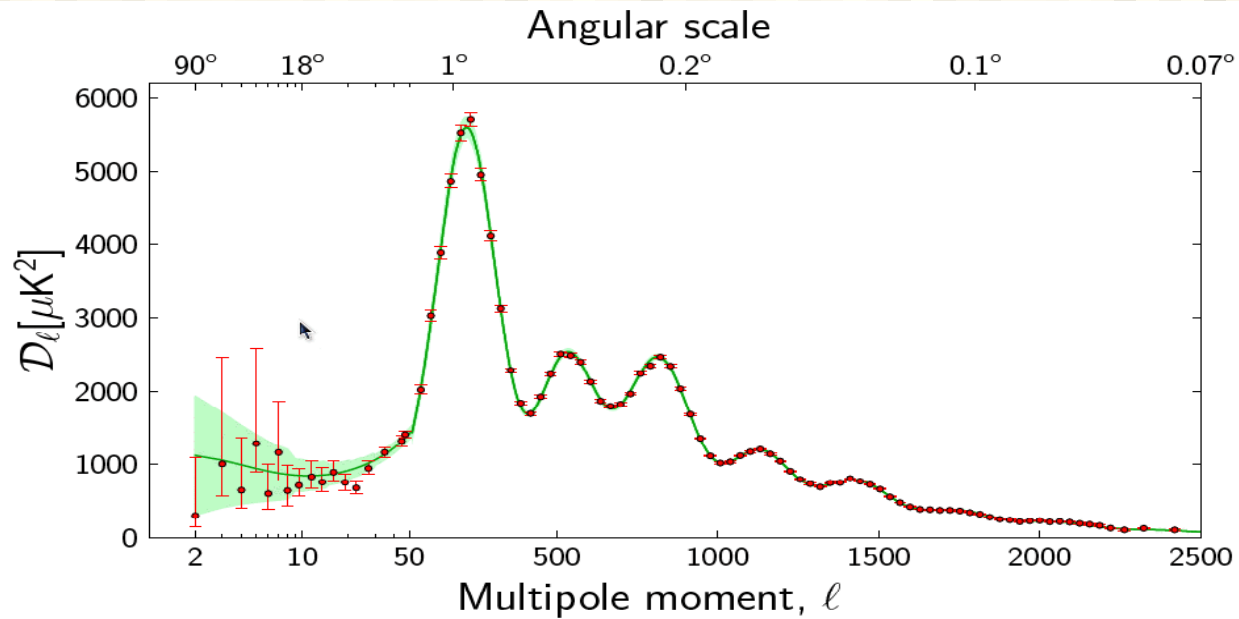
$$\Delta T(\theta, \phi) = \sum_{l=2}^{\infty} \sum_{m=-l}^{m=l} a_{l,m} Y_{l,m}(\theta, \phi)$$



# Angular power spectrum



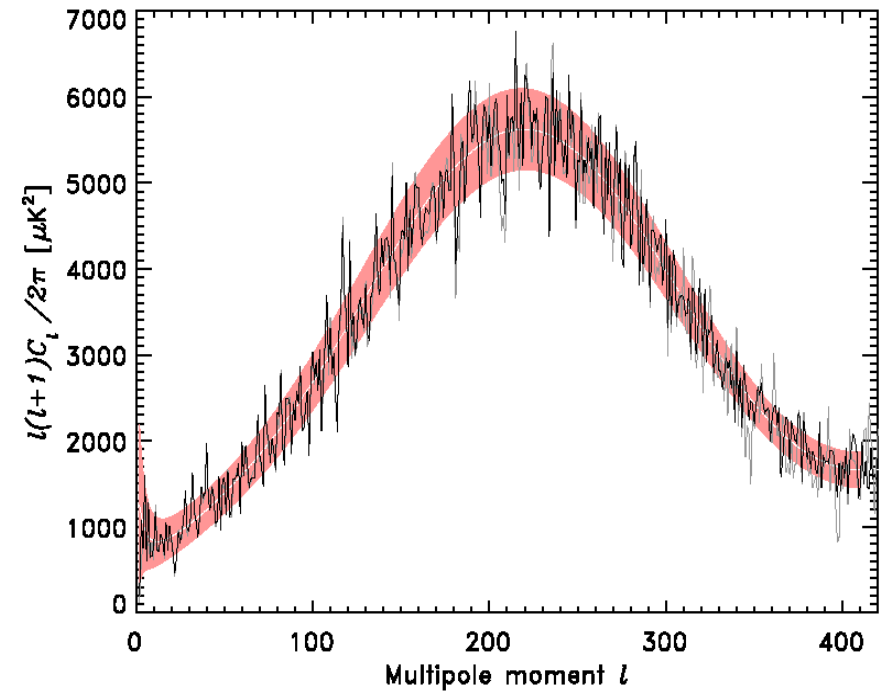
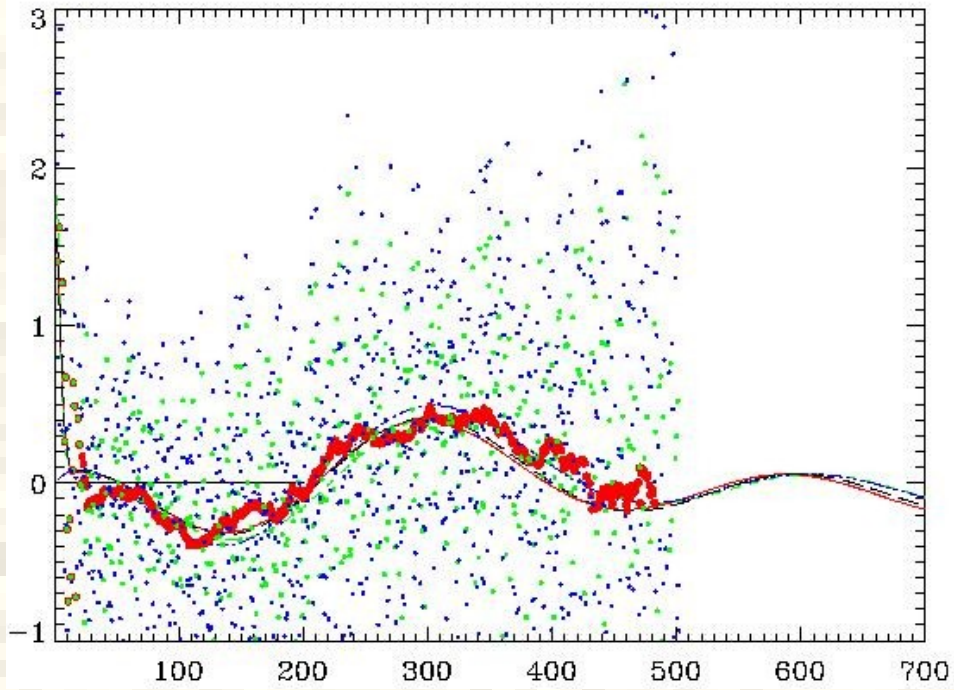
WMAP 9,  
2012



Planck  
2013



# Binning



# Estimation of parameters

# Data analysis of CMB

- Registration: time ordered data:  $T(t)=T(l,b)$
- Pixelization: map-making and restoration data in pixels
- Component separation
- Multipole analysis
- Pixel statistics of the CMB map
- Angular power spectrum analysis and determination of cosmological parameters

# Angular power spectrum of CMB

$$C_\ell \equiv C_\ell(h, \Omega_b h^2, \Omega_{CDM} h^2, \Omega_\Lambda, \Omega_\nu, n, \dots)$$

CAMB: *Lewis, Challinor, Lasenby, 2000*

# CAMB On-line: <http://lambda.gsfc.nasa.gov>

LAMBDA - CAMB Web Interface - Mozilla Firefox

File Edit View History Bookmarks Tools Help

http://lambda.gsfc.nasa.gov/toolbox/tb\_camb\_form.cfm

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## CAMB Web Interface

Supports the January 2011 Release

Most of the [configuration documentation](#) is provided in the sample parameter file provided with the application

This form uses JavaScript to enable certain layout features, and it uses Cascading Style Sheets to control the layout of all the form components. If either of these features are not supported or enabled by your browser, this form will NOT display correctly.

*Actions to Perform*

Scalar C<sub>l</sub>'s       Do Lensing       Linear  
 Vector C<sub>l</sub>'s       Transfer Functions       Non-linear Matter Power (IALOFIT)  
 Tensor C<sub>l</sub>'s       Non-linear CMB Lensing (HALOFIT)

Sky Map Output:

Vector C<sub>l</sub>'s are incompatible with Scalar and Tensor C<sub>l</sub>'s. The Transfer functions require Scalar and/or Tensor C<sub>l</sub>'s. The HEALpix synfast program is used to generate maps from the resultant spectra. The random number seed governs the phase of the a<sub>lm</sub>'s generated by synfast. The default of zero causes synfast to generate a new seed from the system time with each run. Specifying a fixed nonzero value will return fixed phases with successive runs.

*Maximum Multipoles and k\*eta*

Scalar	Tensor
<input type="text" value="2000"/> l <sub>max</sub>	<input type="text" value="1500"/> l <sub>max</sub>
<input type="text" value="4000"/> k*eta <sub>max</sub>	<input type="text" value="3000"/> k*eta <sub>max</sub>

Tensor limits should be less than or equal to the scalar limits.

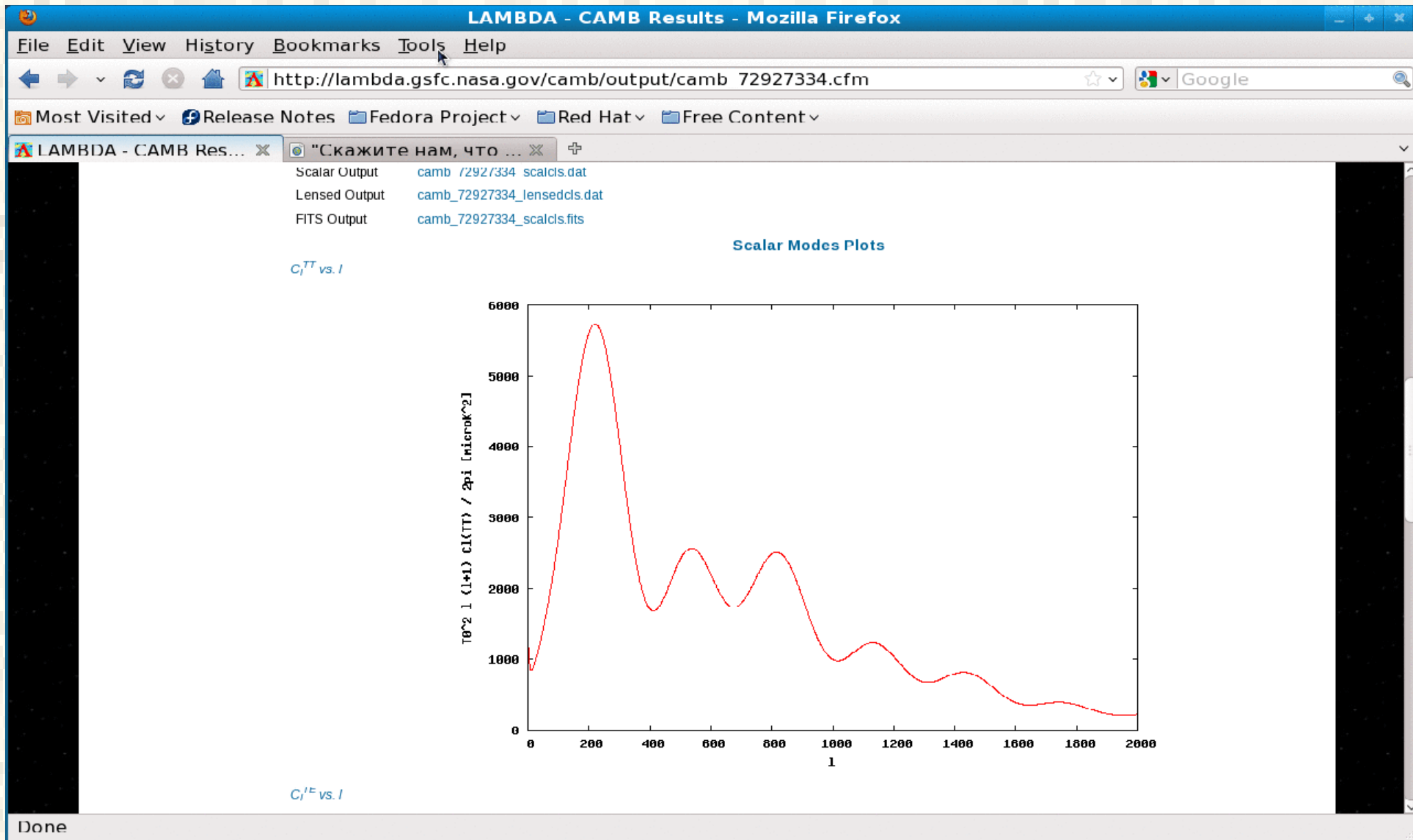
*Cosmological Parameters*

Use Physical Parameters?

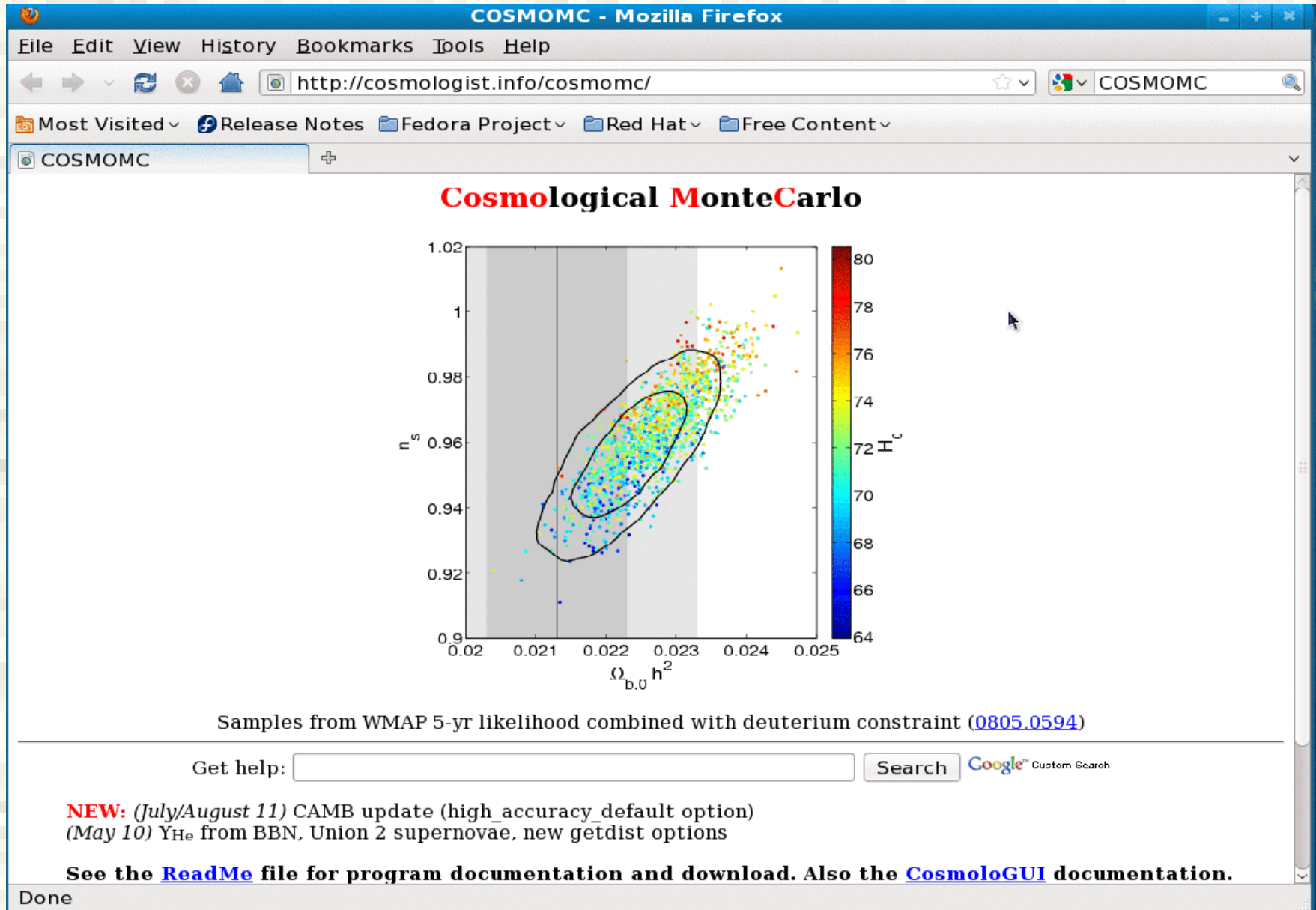
<input type="text" value="70"/> Hubble Constant	<input type="text" value="0.0226"/> Ω <sub>b</sub> h <sup>2</sup>	<input type="text" value="0.114"/> Ω <sub>c</sub> h <sup>2</sup>	<input type="text" value="0.24"/> Helium Fraction
<input type="text" value="2.725"/> T <sub>cmb</sub>	<input type="text" value="0"/> Ω <sub>v</sub> h <sup>2</sup>	<input type="text" value="0"/> Massive Neutrinos	<input type="text" value="3.04"/> Massless Neutrinos
	<input type="text" value="0"/> Ω <sub>k</sub>	<input type="text" value="-1"/> Eqn. of State	

Done

# CAMB On-line: <http://lambda.gsfc.nasa.gov>



# COSMOMC: COSMOlogical Monte Carlo





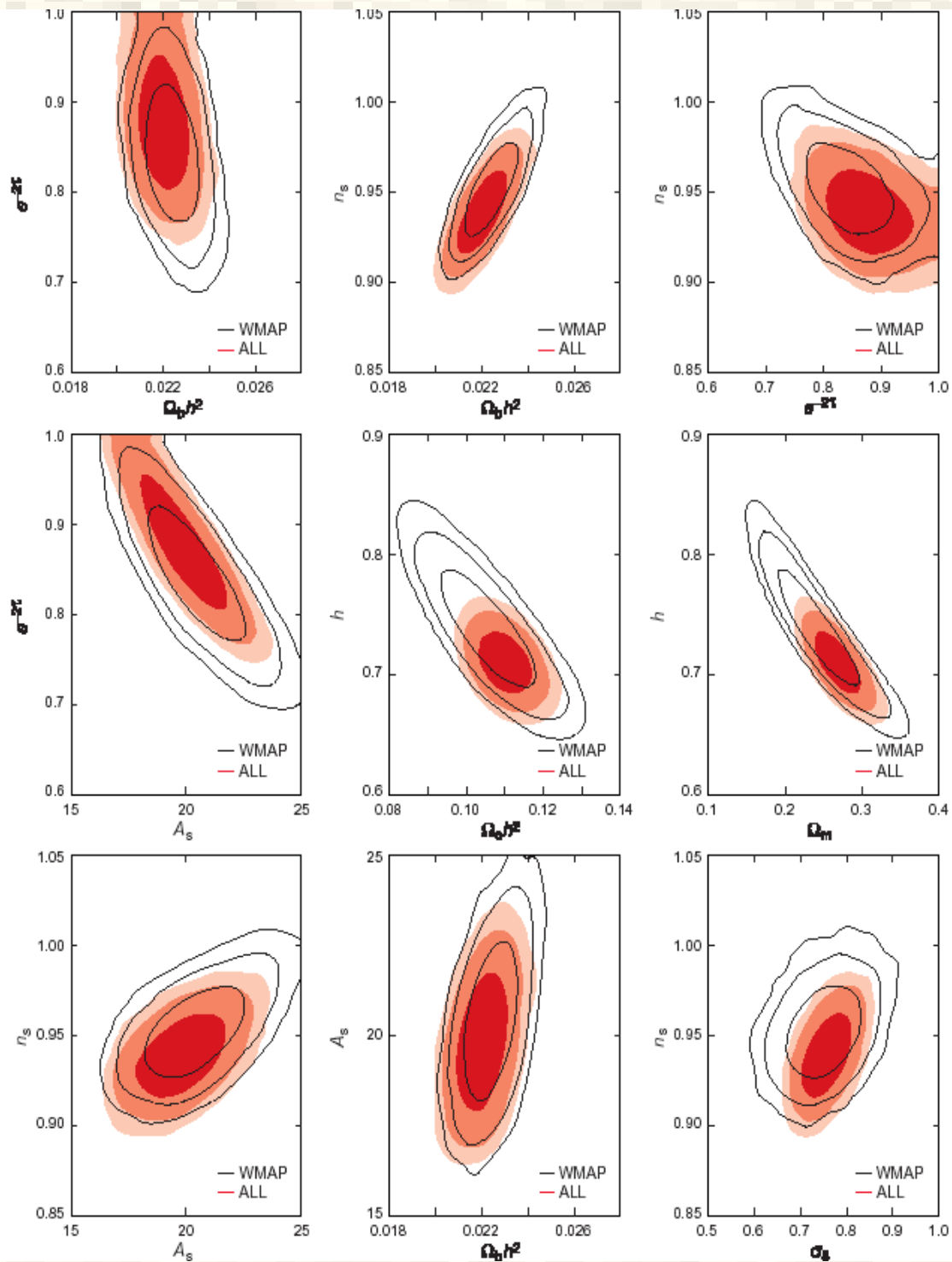
## **Basic input data:**

1. CMB  $C(l)$  data (CAMB)
2. SDSS Ly-alpha
3. SN Ia
4. Lensing
5. ...

## **Calculated parameters:**

1.  $\Omega_b h^2$  – density of barionic matter
2.  $\Omega_c h^2$  – density of DM
3.  $\theta$  ( $\Omega_L, H_0$ ) – sound horizon/angular distance
4.  $\tau$  – optical depth of reionization
5.  $\Omega_k$  - curvatore
6.  $f_{\nu}$  – amount of DM in heavy neutrino
7.  $w$  – equation of state
8.  $n_s$  – scalar spectral index
9.  $n_t$  – tenzor spectral index
- 10, 11, 12, 13, ....

# Diagrams of parameters



# Семейство LCDM-моделей

LAMBDA - WMAP Parameters Matrix - Mozilla Firefox

File Edit View History Bookmarks Tools Help

http://lambda.gsfc.nasa.gov/product/map/dr4/parameters.cfm

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LAMBDA - WMAP Par... Summer School for ...

## WMAP Cosmological Parameters Model/Dataset Matrix

The parameter constraints recommended by the WMAP team may be found [here](#).

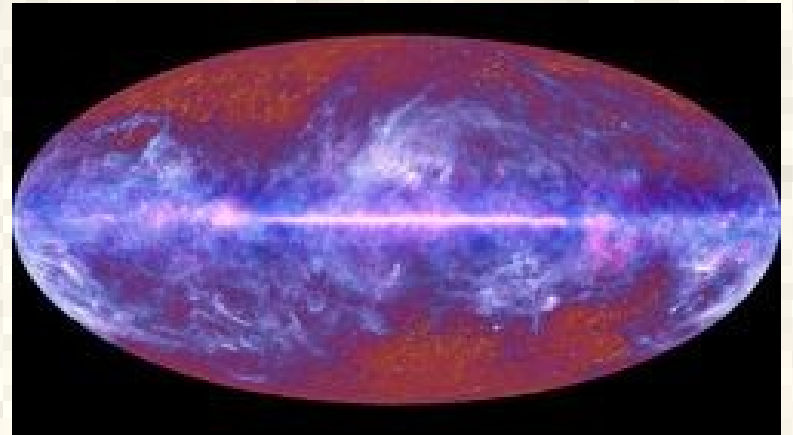
Model [all are +SZ+LENS]	WMAP7	WMAP7+													
		WMAP7.2	BAO+ H0	BAO+ SNSALT	SNCONST	BAO+ SNCONST	BAO+ H0+ TDEL	LRG+ H0	LRG+ H0+ SNCONST	LRG+ H0+ CMB	CMB	BAO	LRG	H0	WMAP7.2+ H0
$\Lambda$ CDM	●		●	◆							●	●	●	●	
$\Lambda$ CDM+DELZ	●														
$\Lambda$ CDM+RUN	●		●			◆					●				
$\Lambda$ CDM+TENS	●		●	◆		◆					●				
$\Lambda$ CDM+RUN+TENS	●		●												
$\Lambda$ CDM+ISO1	●		●			◆									
$\Lambda$ CDM+ISO2	●		●			◆									
$\Lambda$ CDM+MNU	●	▲	●			◆		●	◆						▲
$\Lambda$ CDM+YHE	●							●		●					
WCDM+MNU	●		●			●		●	●						
$\Lambda$ CDM+NREL	●	▲	●					●	◆						▲
$\Lambda$ CDM+NREL>3	◆		◆					◆							
O $\Lambda$ CDM	●		●	◆		◆									
WCDM	●	▲	◆		●	◆	●								▲
OWCDM	●		◆			●	●								

The icons indicate what data is available for a model/dataset pair:

- ▲ Filled Red Triangles Parameters with Markov chains (WMAP version 4.1, RECFAST version 1.5)
- ◆ Filled Green Diamonds Post Processed Parameters with spectra and/or Markov chains (WMAP version 4.0, RECFAST version 1.4.2)
- Filled Green Circles Parameters with spectra and/or Markov chains (WMAP version 4.0, RECFAST version 1.4.2)

Done

# We were waiting for Planck results



# Cosmological results: WMAP9 and Planck data

<http://lambda.gsfc.nasa.gov>

Comparison of *Planck*-only and *WMAP*-only Six-Parameter  $\Lambda$ CDM Fits<sup>a</sup>

Parameter	<i>Planck</i> ("CMB+Lens")	<i>WMAP</i> (9-year)	Difference	
			value	<i>WMAP</i> $\sigma$
$\Omega_b h^2$	$0.02217 \pm 0.00033$	$0.02264 \pm 0.00050$	$-0.00047$	0.9
$\Omega_c h^2$	$0.1186 \pm 0.0031$	$0.1138 \pm 0.0045$	$0.0048$	1.1
$\Omega_\Lambda$	$0.693 \pm 0.019$	$0.721 \pm 0.025$	$-0.028$	1.1
$\tau$	$0.089 \pm 0.032$	$0.089 \pm 0.014$	0	0
$t_0$ (Gyr)	$13.796 \pm 0.058$	$13.74 \pm 0.11$	56 Myr	0.5
$H_0$ (km s <sup>-1</sup> Mpc <sup>-1</sup> )	$67.9 \pm 1.5$	$70.0 \pm 2.2$	$-2.1$	1.0
$\sigma_8$	$0.823 \pm 0.018$	$0.821 \pm 0.023$	$0.002$	0.1
$\Omega_b$	$0.0481^b$	$0.0463 \pm 0.0024$	$0.0018$	0.7
$\Omega_c$	$0.257^b$	$0.233 \pm 0.023$	$0.024$	1.0

No revolution...

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No revolution... *But there are some strangeness...*

# Cosmological results: WMAP9 and Planck data

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No revolution... *But there are some strangeness,*  
*which we can see in the next lecture*

