

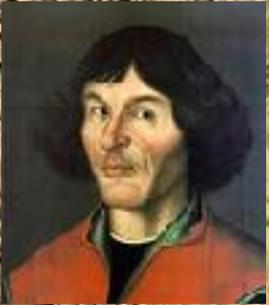
# Small Scale Structures in Lambda Cold Dark Matter

Julio F. Navarro



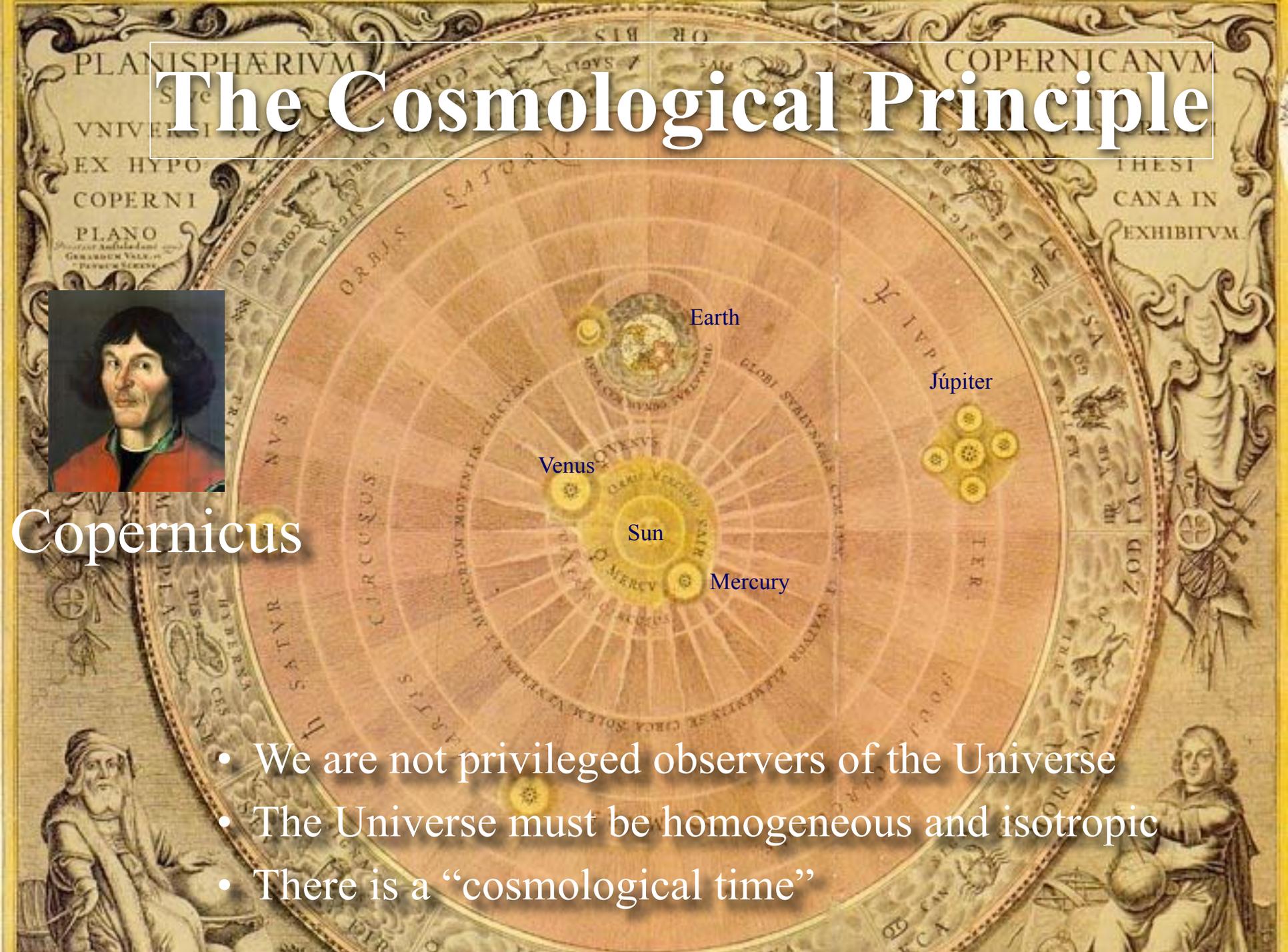
- Lecture 1: Basic Cosmological Facts
- Lecture 2: Non-Linear Structures in LCDM
- Lecture 3: Galaxy Structure and LCDM
- Lecture 4: Small Scale Constraints to LCDM

# The Cosmological Principle



Copernicus

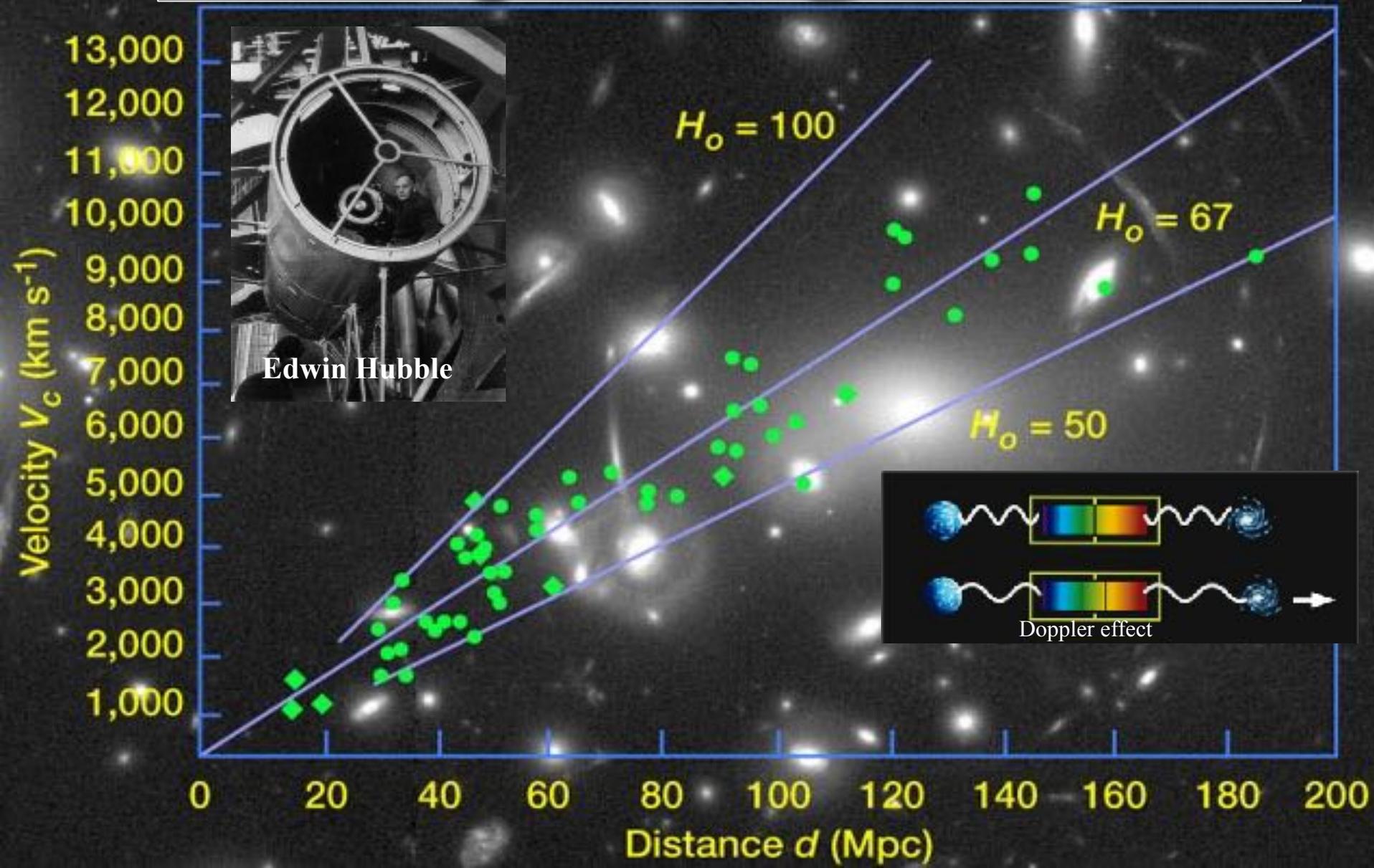
- We are not privileged observers of the Universe
- The Universe must be homogeneous and isotropic
- There is a “cosmological time”



# A finite Universe

- The night sky is dark
- The Universe cannot be infinite in time and space

# The expanding Universe



# Universal expansion

- On cosmological scales the Universe is homogeneous and isotropic
- A possible visualization is to think of galaxies as populating a uniform grid in space
- As the Universe **expands**, the **grid stretches without changing shape**
- There is no centre. Every point in the grid is equivalent to any other



# The expansion of the Universe

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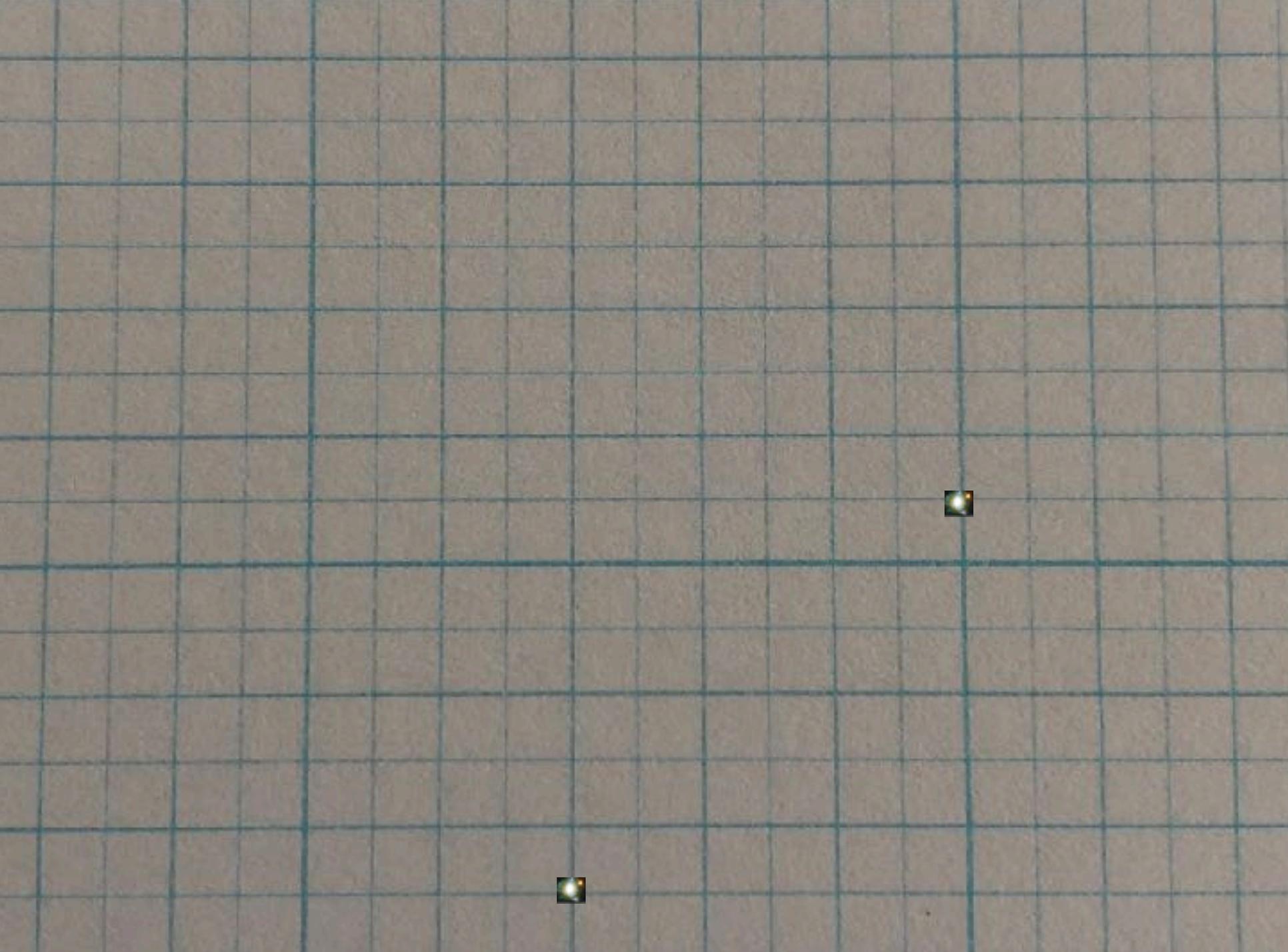
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Universal Expansion + Theory of Relativity:  
what happens if we look back in time?







# The Big Bang

- The “Big Bang” is the moment when the grid size approaches zero
- Looking back in time, the Universe compresses and heats up
- The early Universe was **hot and dense**



# The Big Bang

## Total confirmed COVID-19 cases

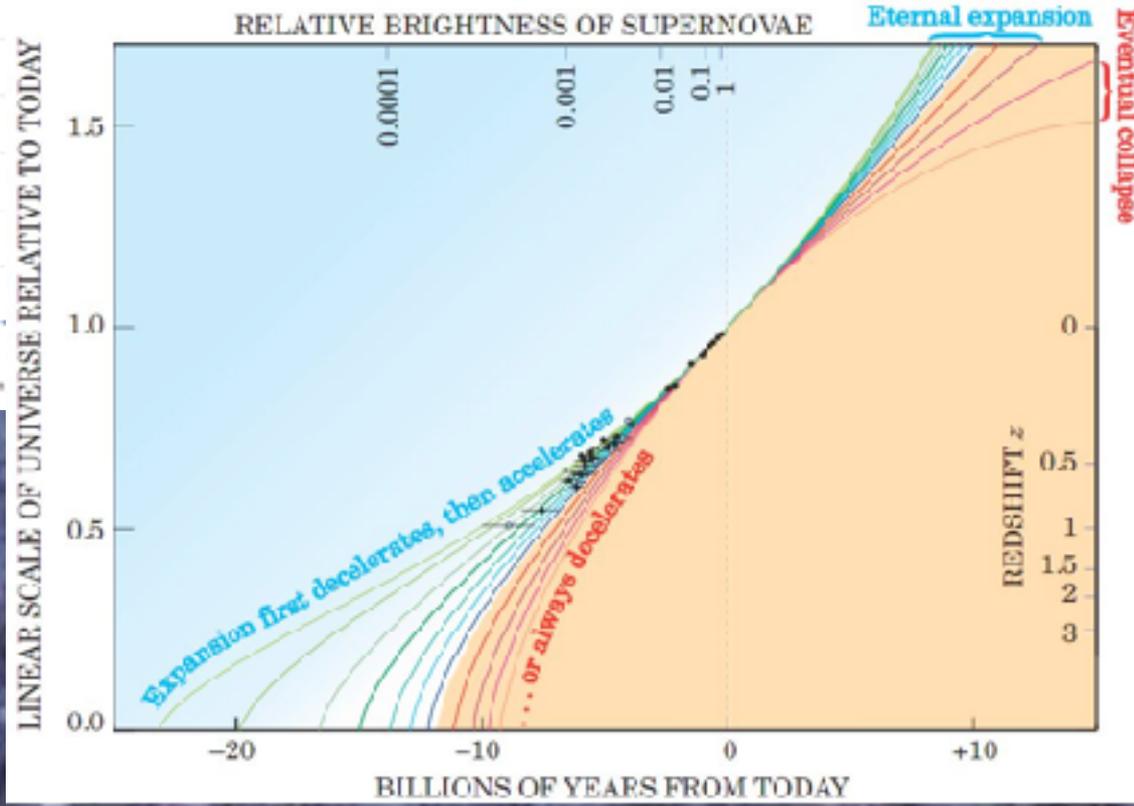
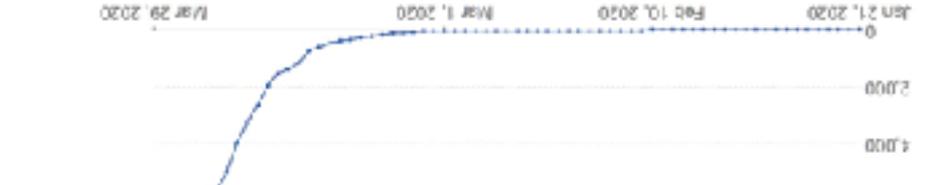
The number of confirmed cases is lower than the number of total cases. The main reason for this is limited testing.

Our Work in Data



Source: European CDC - Latest Situation Update Worldwide  
Note: the large increase in the number of cases globally and in the UK is due to a change in testing methodology.

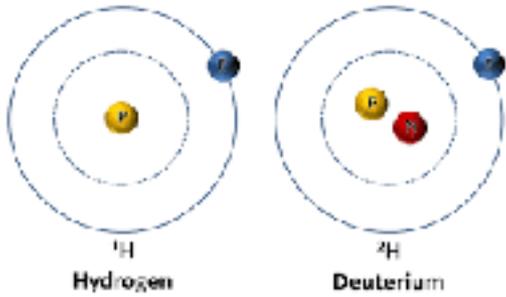
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Note: the large increase in the number of cases globally and in the UK is due to a change in testing methodology.



Total confirmed COVID-19 cases is lower than the number of total cases.

Universal Expansion + Theory of Relativity  
The Universe has a **finite age**

# Hydrogen Isotopes



# The matter content of the Universe

What is the world made of?

H (hydrogen)  
1 proton

Na (sodium)  
11 protons  
12 neutrons

He (helium)  
2 protons  
2 neutrons

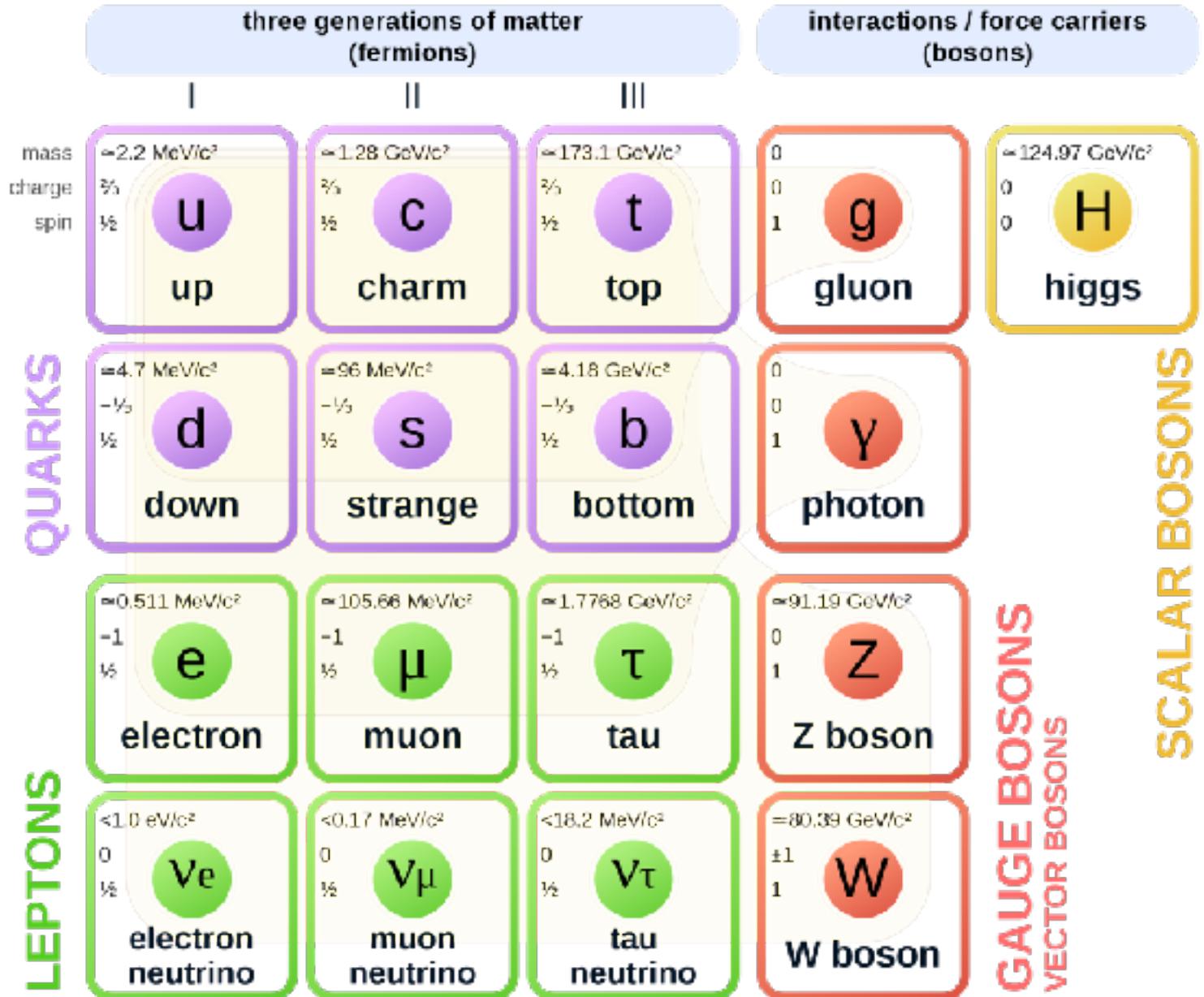
		Periodic table																				
		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18			
		Alkali metals	Alkaline earth metals																			
Group	Period	Hydrogen																		Helium		
1	1	1 H 1.008																			2 He 4.008	
2	2	3 Li 6.94	4 Be 9.0122											5 B 10.81	6 C 12.011	7 N 14.007	8 O 15.999	9 F 18.998			10 Ne 20.180	
3	3	11 Na 22.990	12 Mg 24.305												13 Al 26.982		14 Si 28.086	15 P 30.974	16 S 32.06	17 Cl 35.45	18 Ar 36.96	
4	4	19 K 39.098	20 Ca 40.078	21 Sc 44.956	22 Ti 47.867	23 V 50.942	24 Cr 51.996	25 Mn 54.938	26 Fe 55.845	27 Co 58.933	28 Ni 58.693	29 Cu 63.546	30 Zn 65.38	31 Ga 69.723	32 Ge 72.631	33 As 74.922	34 Se 78.971	35 Br 79.904	36 Kr 83.798			
5	5	37 Rb 85.468	38 Sr 87.62	39 Y 88.906	40 Zr 91.224	41 Nb 92.906	42 Mo 95.94	43 Tc [98]	44 Ru 101.07	45 Rh 102.91	46 Pd 106.32	47 Ag 107.87	48 Cd 112.41	49 In 114.82	50 Sn 118.71	51 Sb 121.76	52 Te 127.6	53 I 126.90	54 Xe 131.29			
6	6	55 Cs 132.91	56 Ba 137.33	57 La 138.91	58 Ce 140.12	59 Pr 140.91	60 Nd 144.24	61 Pm [145]	62 Sm 150.36	63 Eu 151.96	64 Gd 157.25	65 Tb 158.93	66 Dy 162.50	67 Ho 164.93	68 Er 167.26	69 Tm 168.93	70 Yb 173.05	71 Lu 174.97				
7	7	87 Fr [223]	88 Ra [226]	89 Ac [227]	90 Th 232.04	91 Pa 231.04	92 U 238.03	93 Np [237]	94 Pu [244]	95 Am [243]	96 Cm [247]	97 Bk [247]	98 Cf [251]	99 Es [252]	100 Fm [257]	101 Md [258]	102 No [259]	103 Lr [260]				
	8																					
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Heavier elements need neutrons

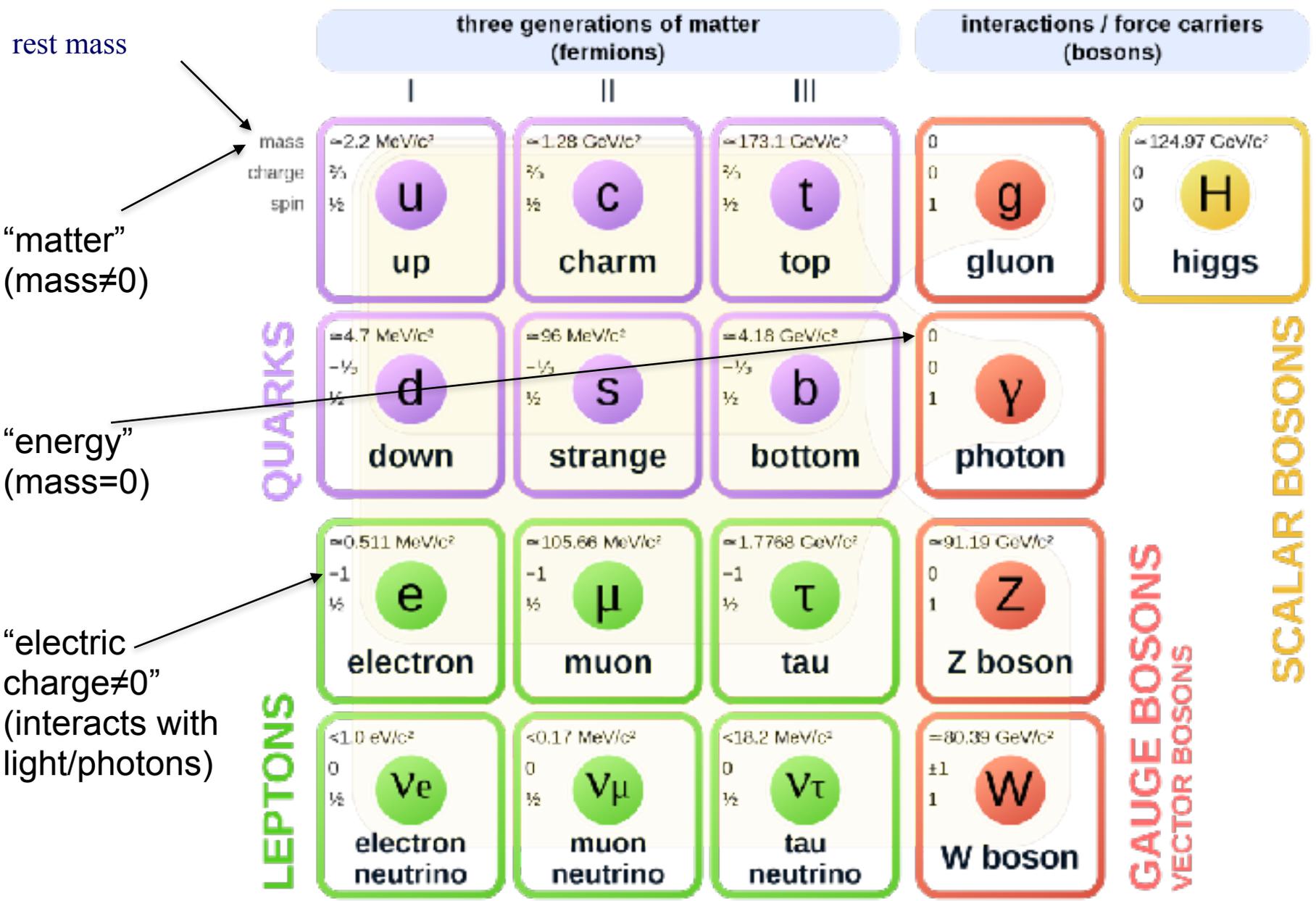
# Standard Model of Elementary Particles

And their anti-particles!

Example: positron is same as electron, but with positive charge. They “annihilate” each other...



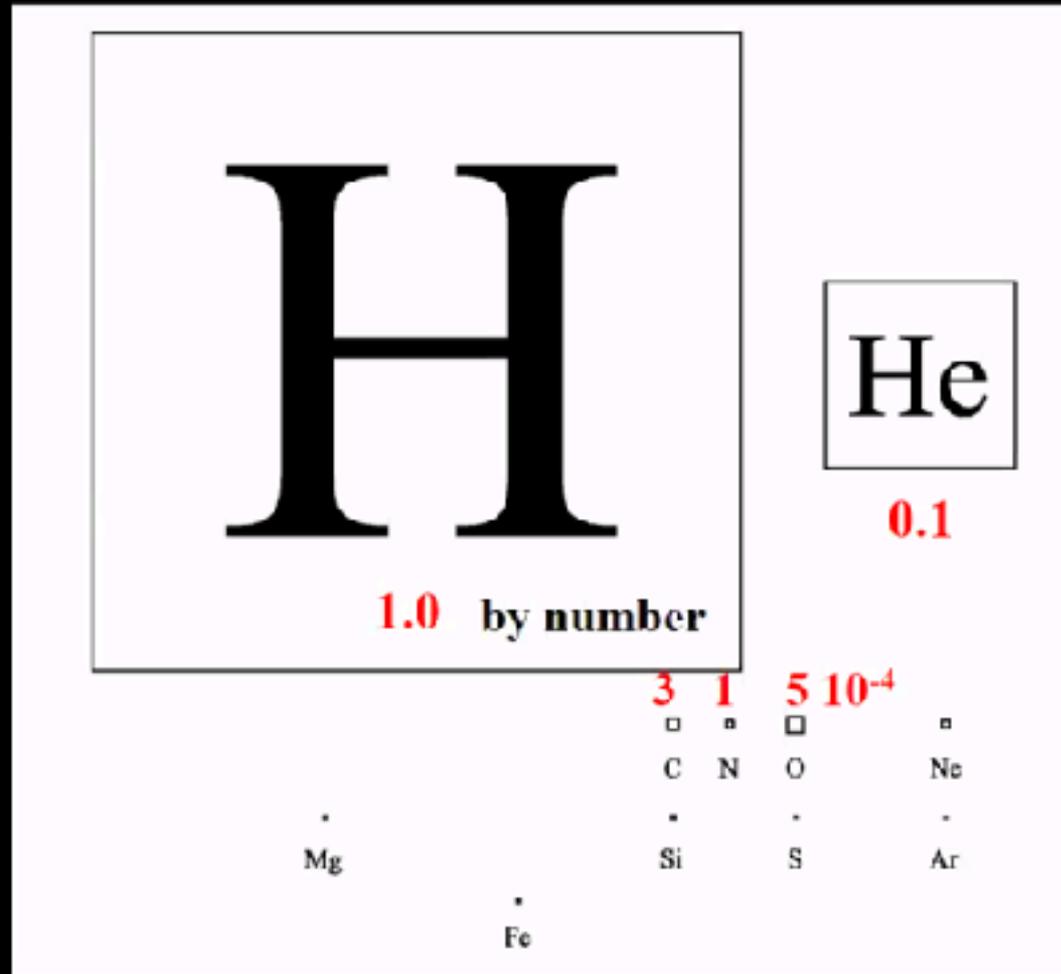
# Standard Model of Elementary Particles



Credit: PBS Nova/Fermilab/Wikipedia



# The astronomer's periodic table



B. McCall 2001

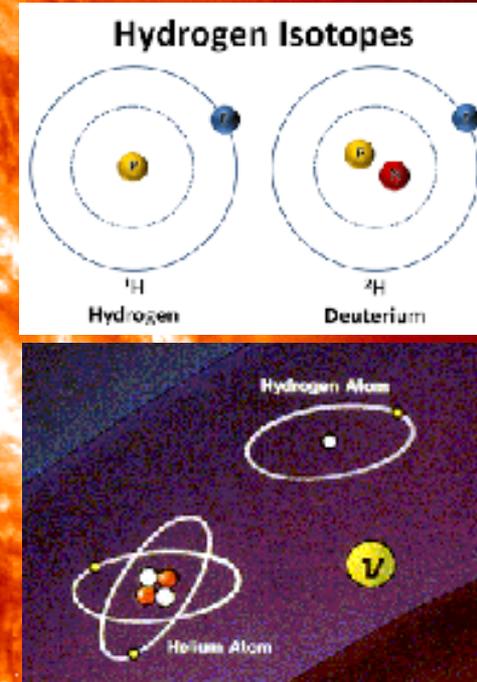
- The Sun, like most stars, is a ball of **Hydrogen** and **Helium**
- Most atoms on Earth were synthesized in stars—we are “**stardust**” (“**nuclear waste**”?)

# The (baryonic) matter content of the Universe



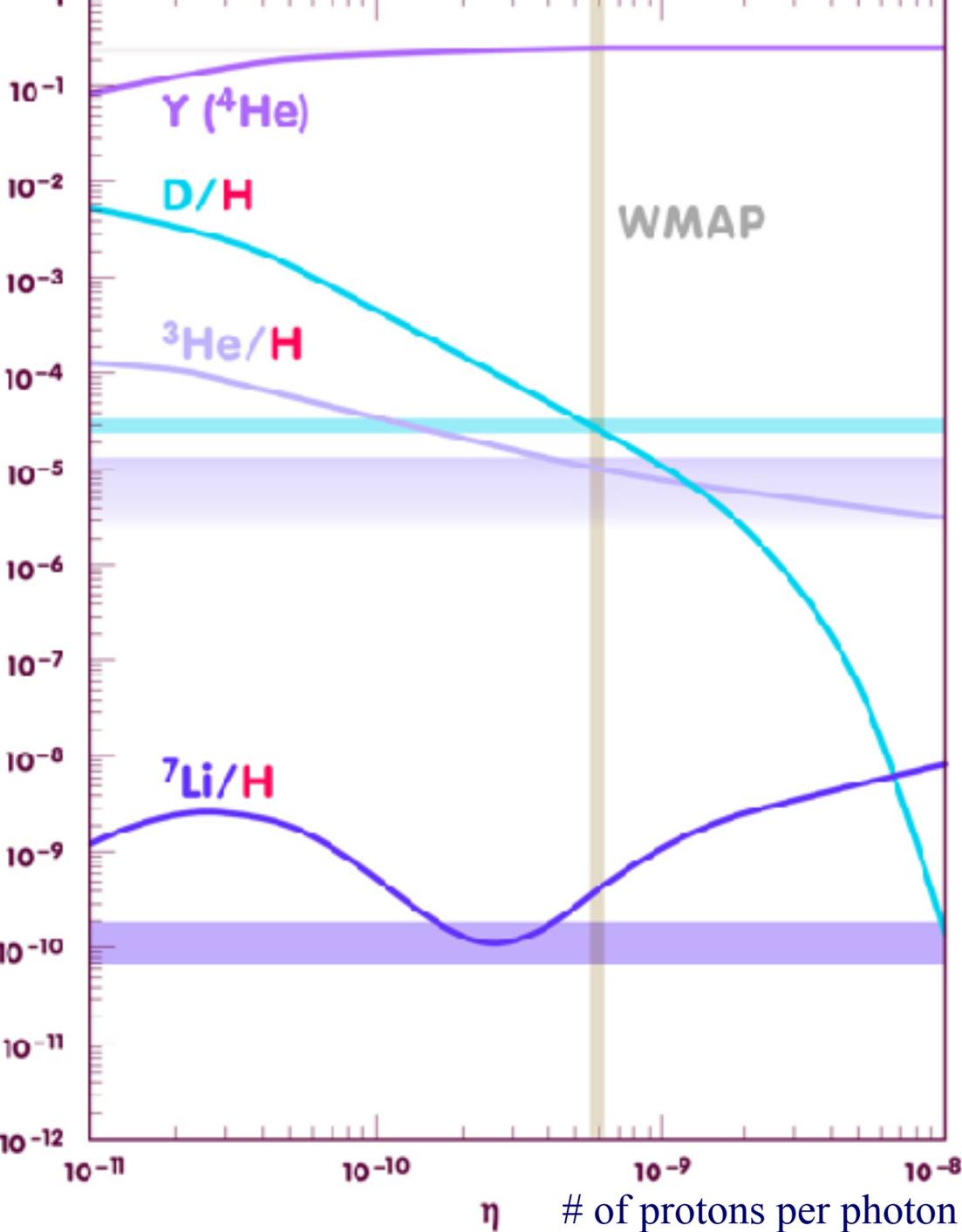
- In the Solar System, most of the mass is in the Sun
- The Sun, like most stars, is a ball of **Hydrogen** and **Helium**
- The light of a star is the result of the fusion of H and He into heavier nuclei
- Most atoms on Earth were synthesized in stars—we are “**stardust**” (or “**nuclear waste**”?)

# The (baryonic) matter content of the Universe



- Nuclear fusion only occurs in dense and hot regions, like the centre of a star
- Most of the observed Universe is **Hydrogen** and **Helium**
- **Why, if the Universe was once hot and dense like a star?**

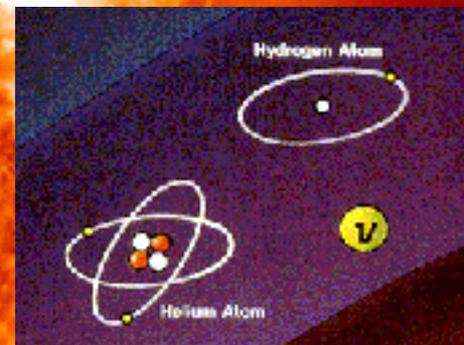
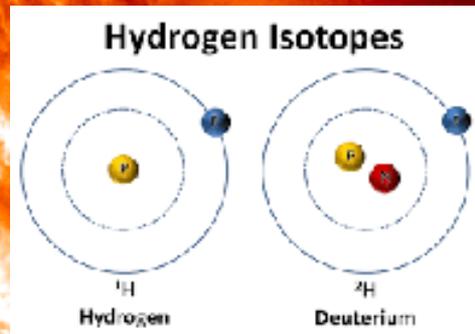




There must be light!

- The abundance of Helium ( $^4\text{He}$ ), Deuterium (D), and other light elements allow us to measure the “matter/energy” ratio (baryons/light) of the Universe
- If we could measure the amount of light in the Universe, we could know the total amount of matter (baryonic)

# Where is that “cosmic light”?



## The expansion of the Universe (backwards in time)

- The galaxy “grid” does not change as the Universe expands
- We can visualize the Universe as “static grid” where the density at each point increases as we go back in time
- Looking back in time, the Universe contracts and every point becomes **denser and hotter**



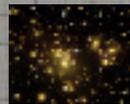
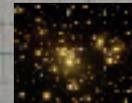
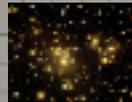
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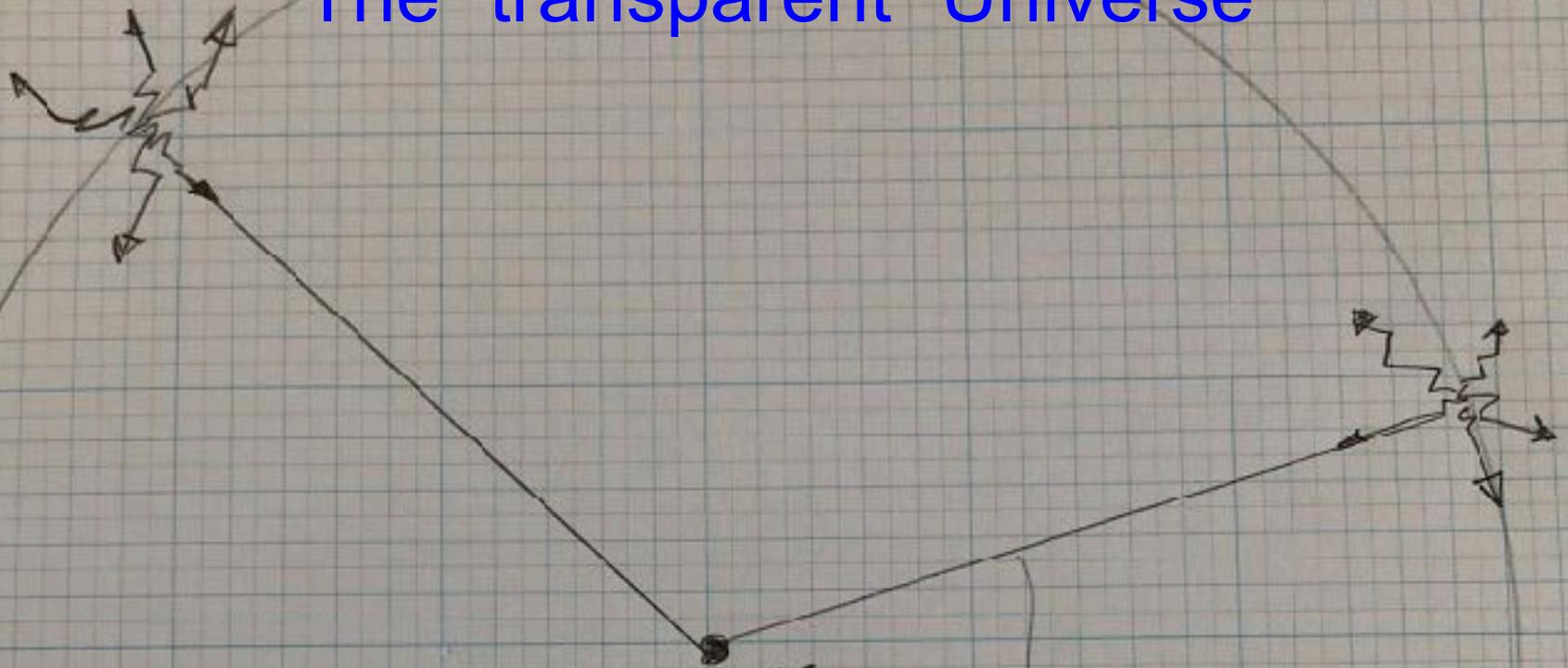


# The “opaque” Universe

- At some point the Universe becomes so hot that electrons cannot remain attached to protons
- Free electrons interact with light and do not allow light to propagate freely. The early Universe is opaque, like a dense fog
- Photons cannot travel far from where they are



# The "transparent" Universe

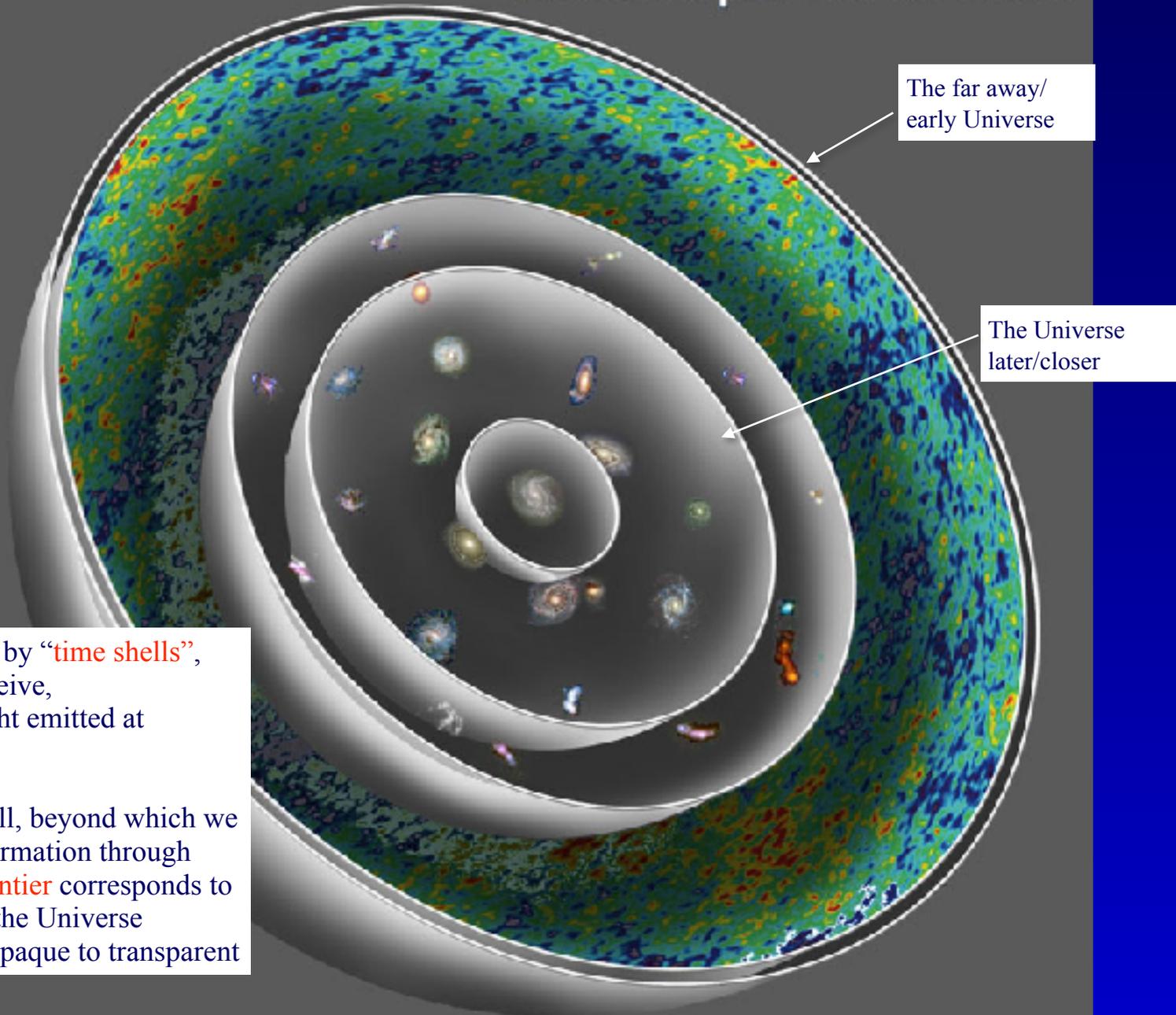


US

Path of photon  
since epoch of  
"recombination"

- When the Universe expands and cools, electrons and protons "recombine" and stop interacting strongly with light
- Photons can propagate freely through the Universe
- Today those photons reach us from every direction

# Cosmic Spheres of Time



The far away/  
early Universe

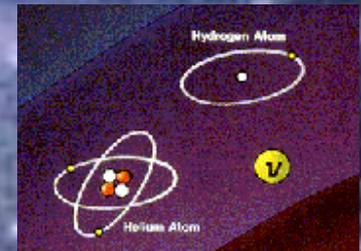
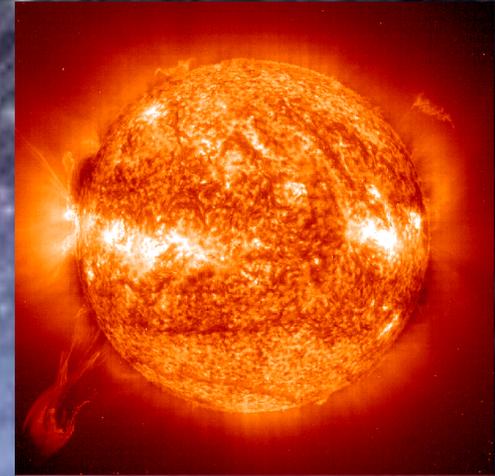
The Universe  
later/closer

We are surrounded by “**time shells**”, from which we receive, simultaneously, light emitted at different epochs

There is a final shell, beyond which we cannot receive information through light. This **light frontier** corresponds to the moment when the Universe transitioned from opaque to transparent

# Summary of Basic Cosmological Facts

- The Universe expands
  - The Universe was once hotter and denser
  - There was a beginning of time: **the Big Bang**
- Most of the matter we see is hydrogen
  - Elements heavier than He are synthesized in stars
  - The Universe must be filled of light: **the Cosmic Microwave Background**
  - The Universe became opaque in the not too distant past

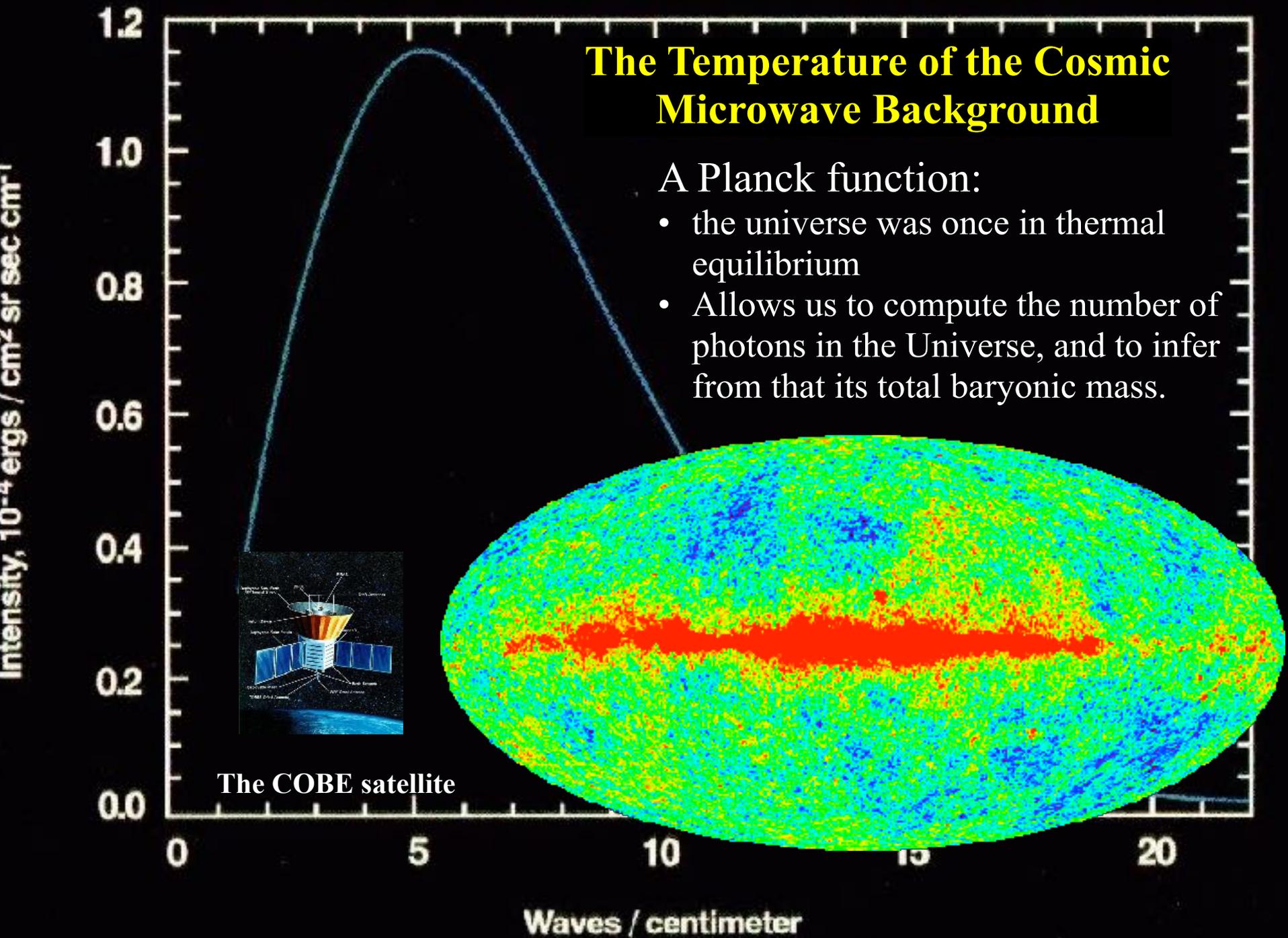


Penzias and Wilson 1964

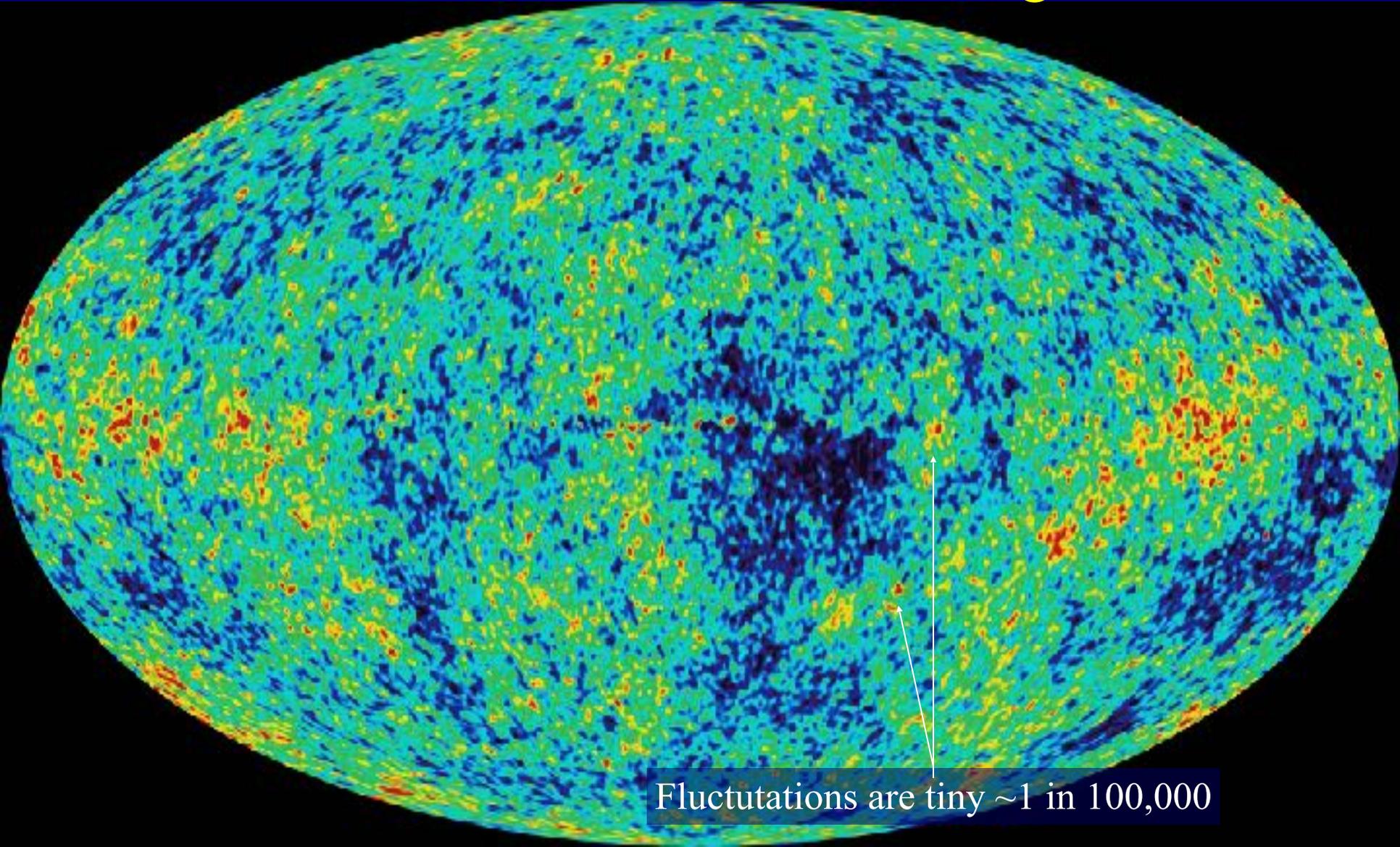
# The Temperature of the Cosmic Microwave Background

A Planck function:

- the universe was once in thermal equilibrium
- Allows us to compute the number of photons in the Universe, and to infer from that its total baryonic mass.

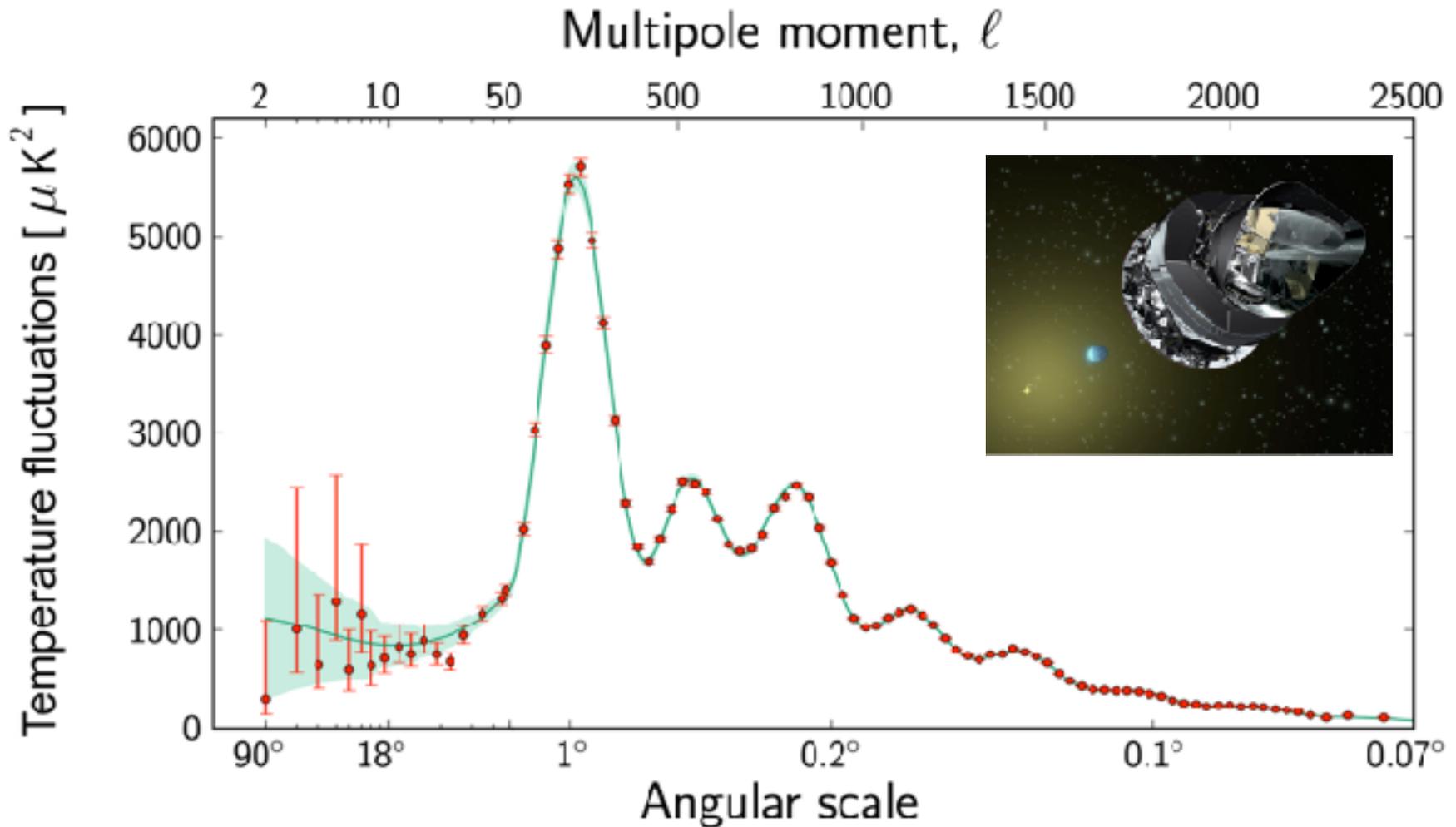


# WMAP Temperature Fluctuations in the Cosmic Microwave Background



Fluctuations are tiny  $\sim 1$  in 100,000

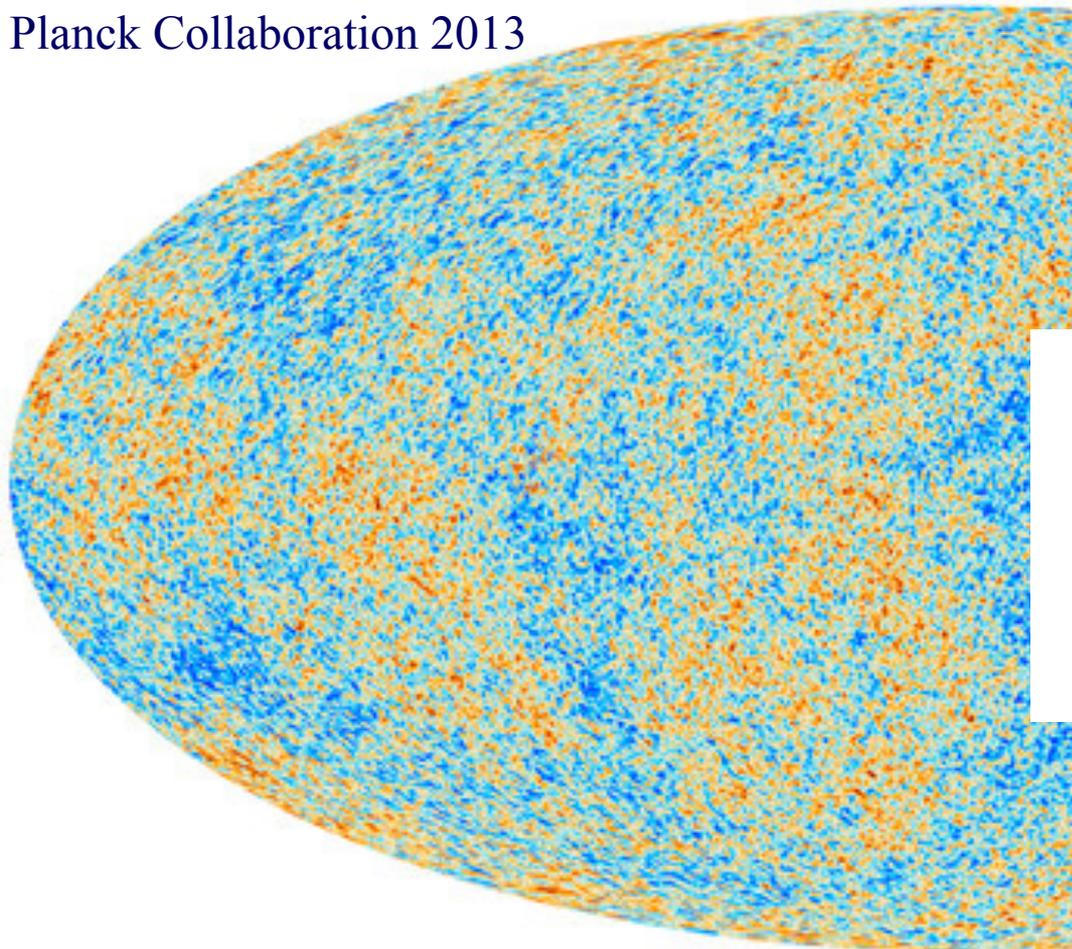
# The Standard Model of Cosmology



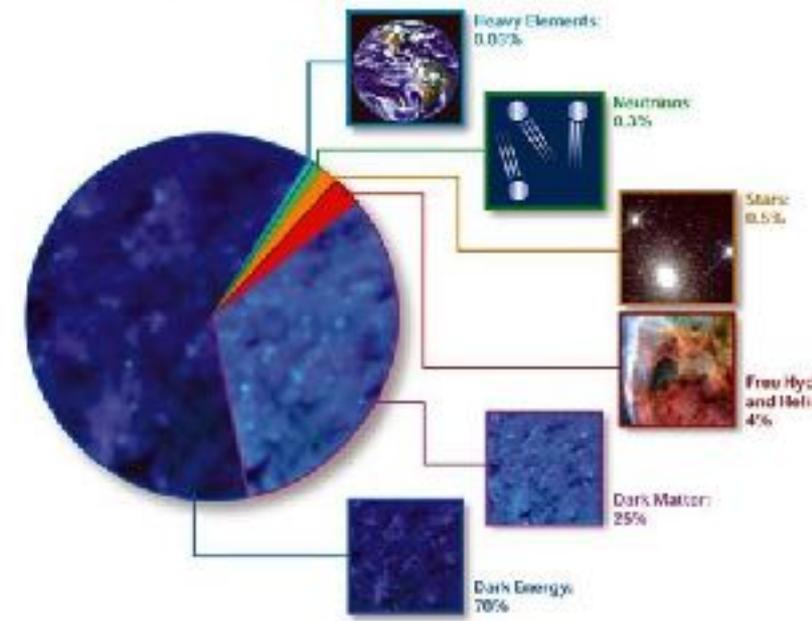
The Planck mission

# The Standard Model of Cosmology

Planck Collaboration 2013



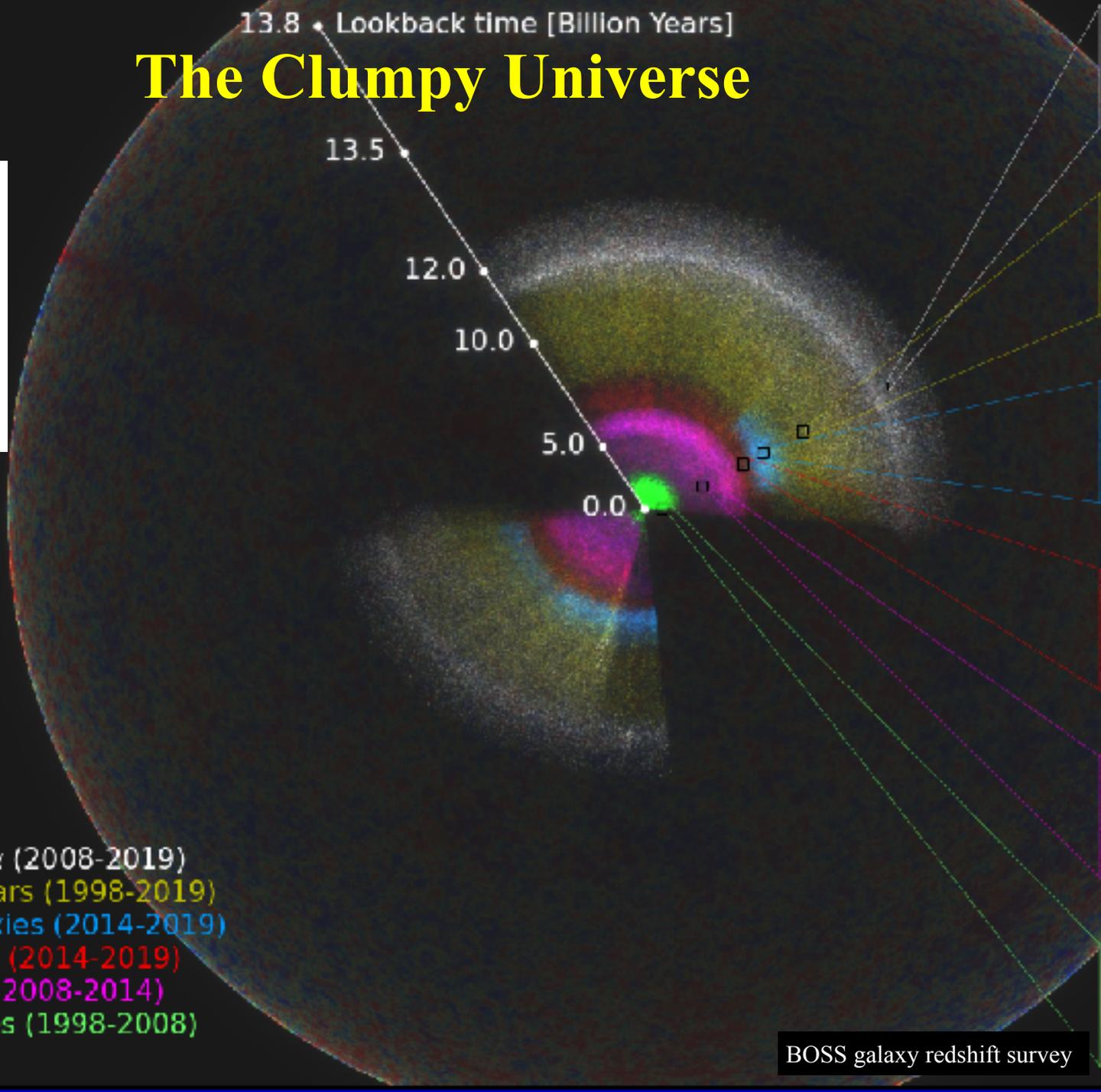
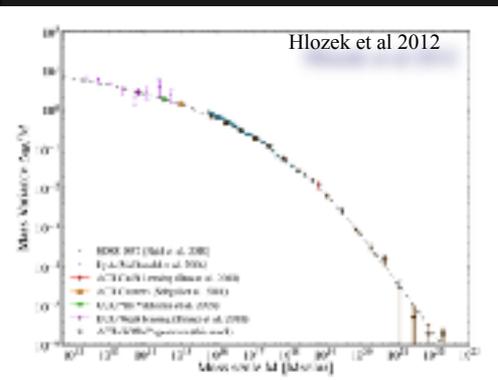
COMPOSITION OF THE COSMOS



This is a universe that we can simulate!

Parameter	Best fit	68% limits
$\Omega_b h^2$	0.022032	$0.02205 \pm 0.00028$
$\Omega_c h^2$	0.12038	$0.1199 \pm 0.0027$
$100\theta_{MC}$	1.04119	$1.04131 \pm 0.00063$
$\tau$	0.0925	$0.089^{+0.012}_{-0.014}$
$n_s$	0.9619	$0.9603 \pm 0.0073$

# The Clumpy Universe

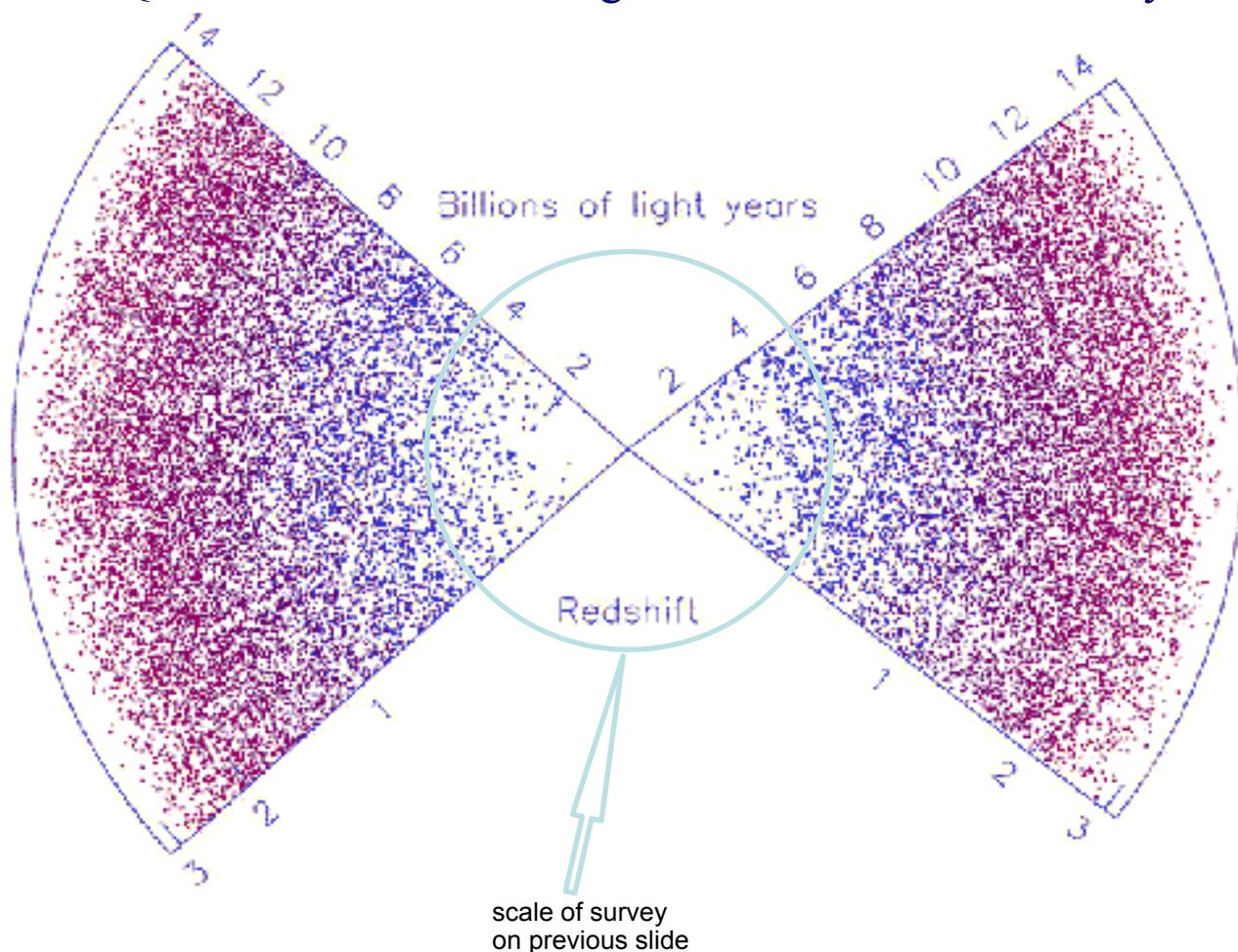


- eBOSS + BOSS Lyman- $\alpha$  (2008-2019)
- eBOSS + SDSS I-II Quasars (1998-2019)
- eBOSS Young Blue Galaxies (2014-2019)
- eBOSS Old Red Galaxies (2014-2019)
- BOSS Old Red Galaxies (2008-2014)
- SDSS I-II Nearby Galaxies (1998-2008)

# The Clumpy Universe on large scales

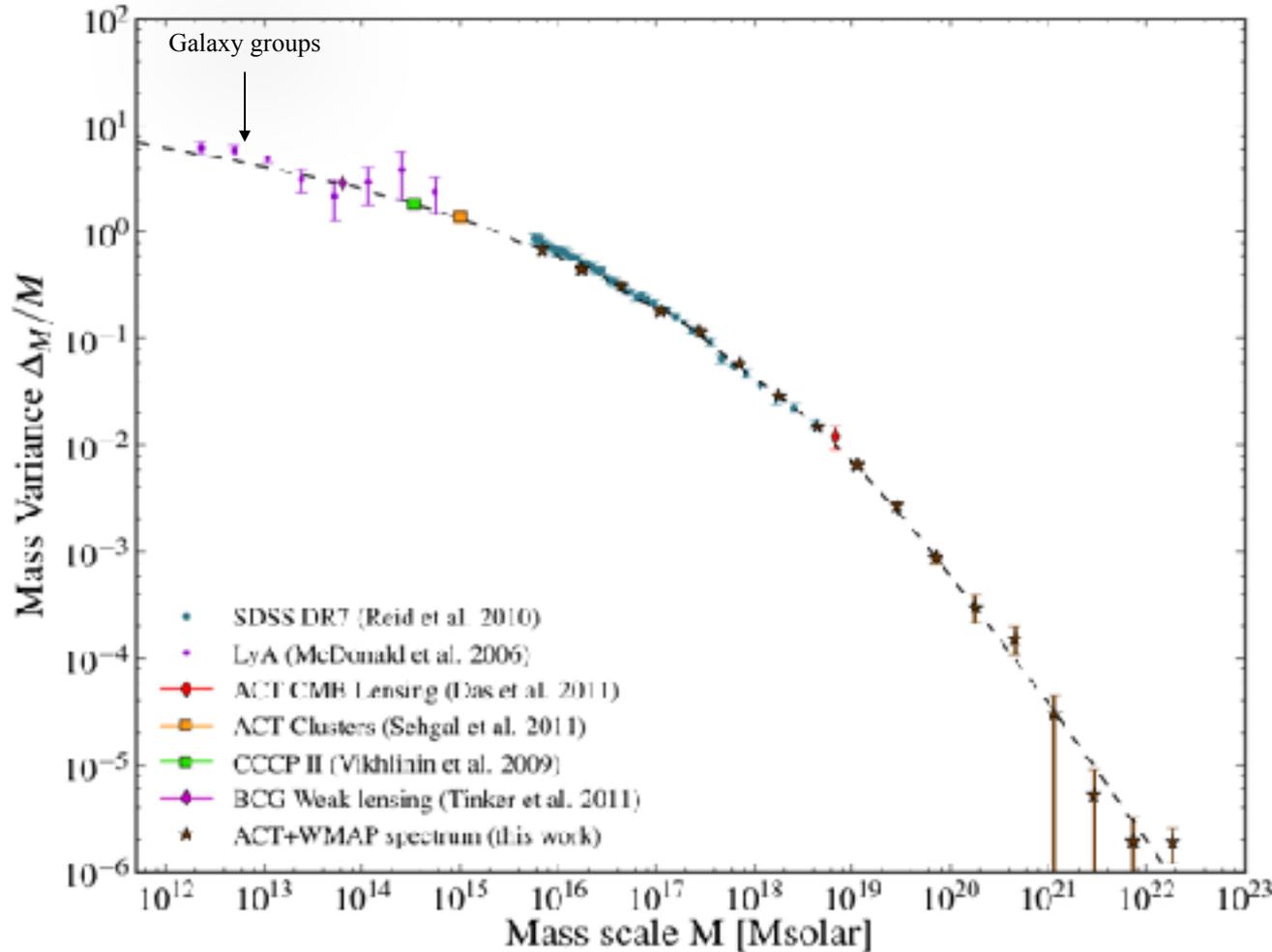
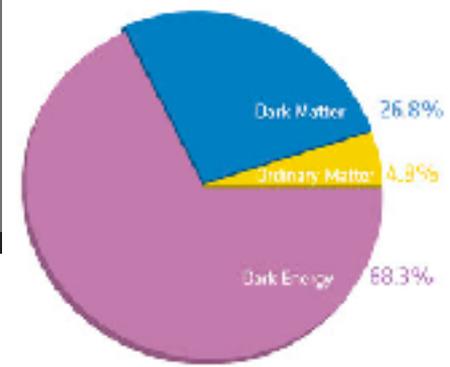
On large scales the  
Universe appears  
homogeneous and  
isotropic

Quasar distribution on large scales from redshift surveys



The Universe is close to homogeneous and isotropic

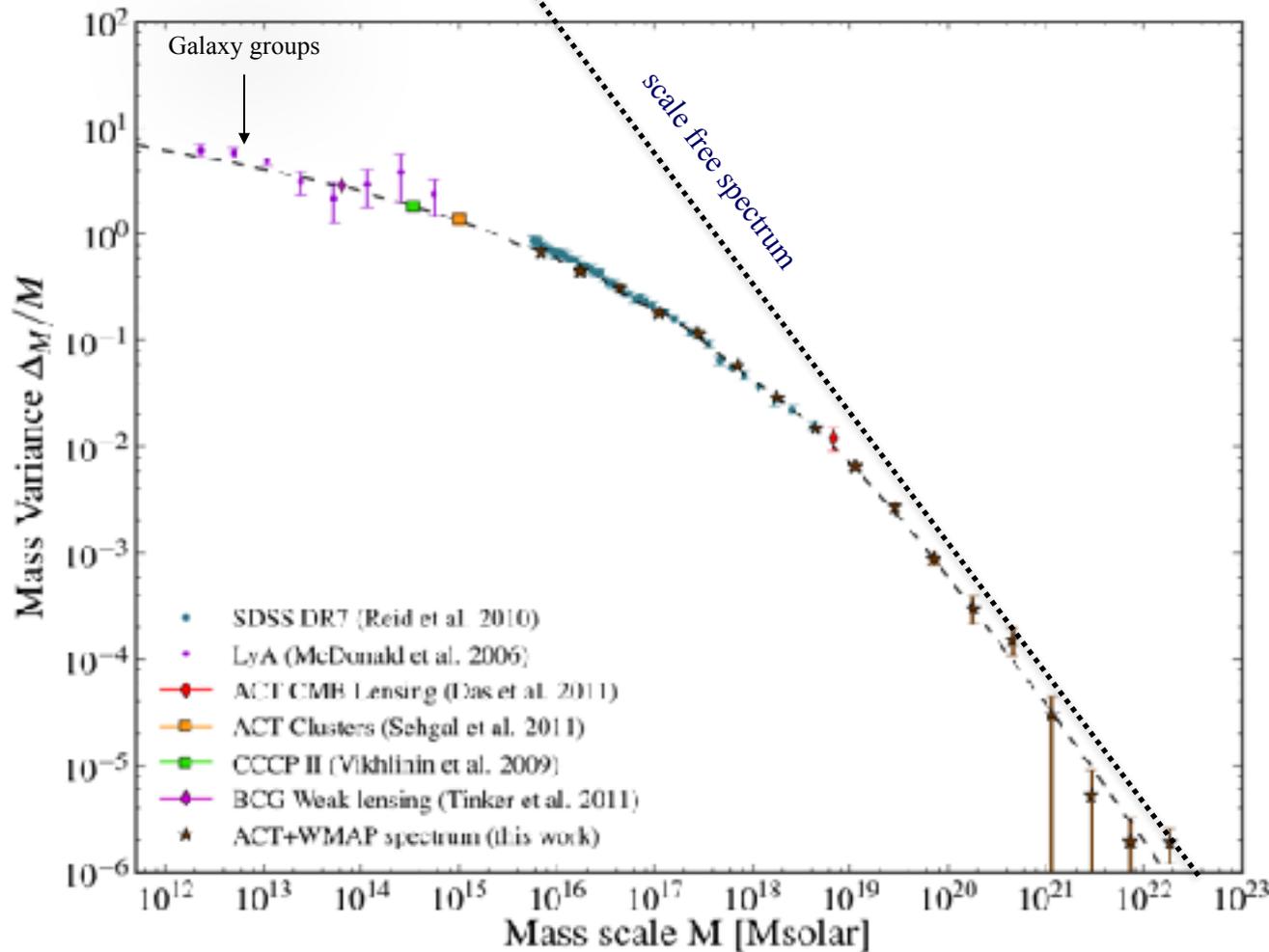
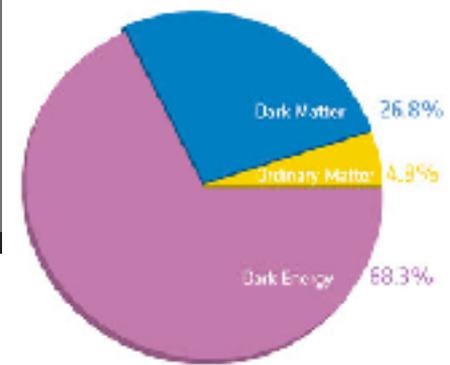
# The Clumpiness of the Universe as a function of scale



The power spectrum of density fluctuations over a wide range of scales is very well measured at various redshifts

Measurements on various scales trace a smooth curve if the Universal expansion started to accelerate in “recent” cosmological times

# The LCDM paradigm: Structure in the Universe in the Linear Regime



The power spectrum of density fluctuations in the linear regime is very well matched by assuming that the initial density fluctuations are Gaussian and “scale free” and that the Universe is dominated by collisionless Cold Dark Matter (CDM)

This represents astonishing success!

# End of Lecture 1

