



Supermassive black holes

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Content of lectures

- Broad overview of **theory** and **observations** of *supermassive black holes in active galactic nuclei (AGN)*
- Focus on *basic physical concepts*
- Some coverage of galaxy-black hole **coevolution**

As grandes perguntas



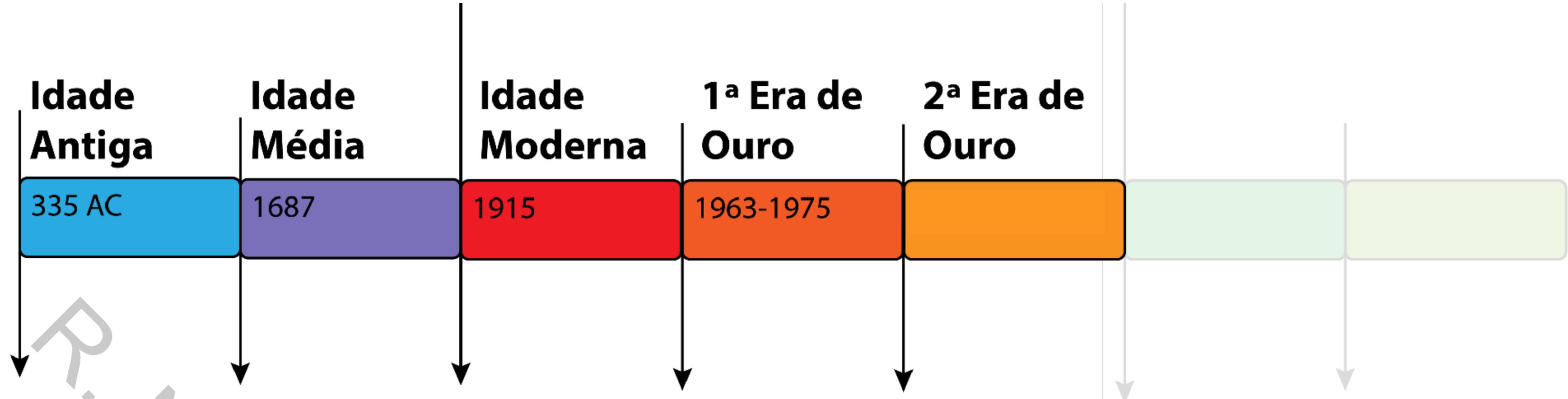
Como as leis da física se comportam perto — e dentro — de um buraco negro?

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = \frac{8\pi G}{c^4}T_{\mu\nu}$$

Como buracos negros afetam o que está ao seu redor?



Eras da gravitação



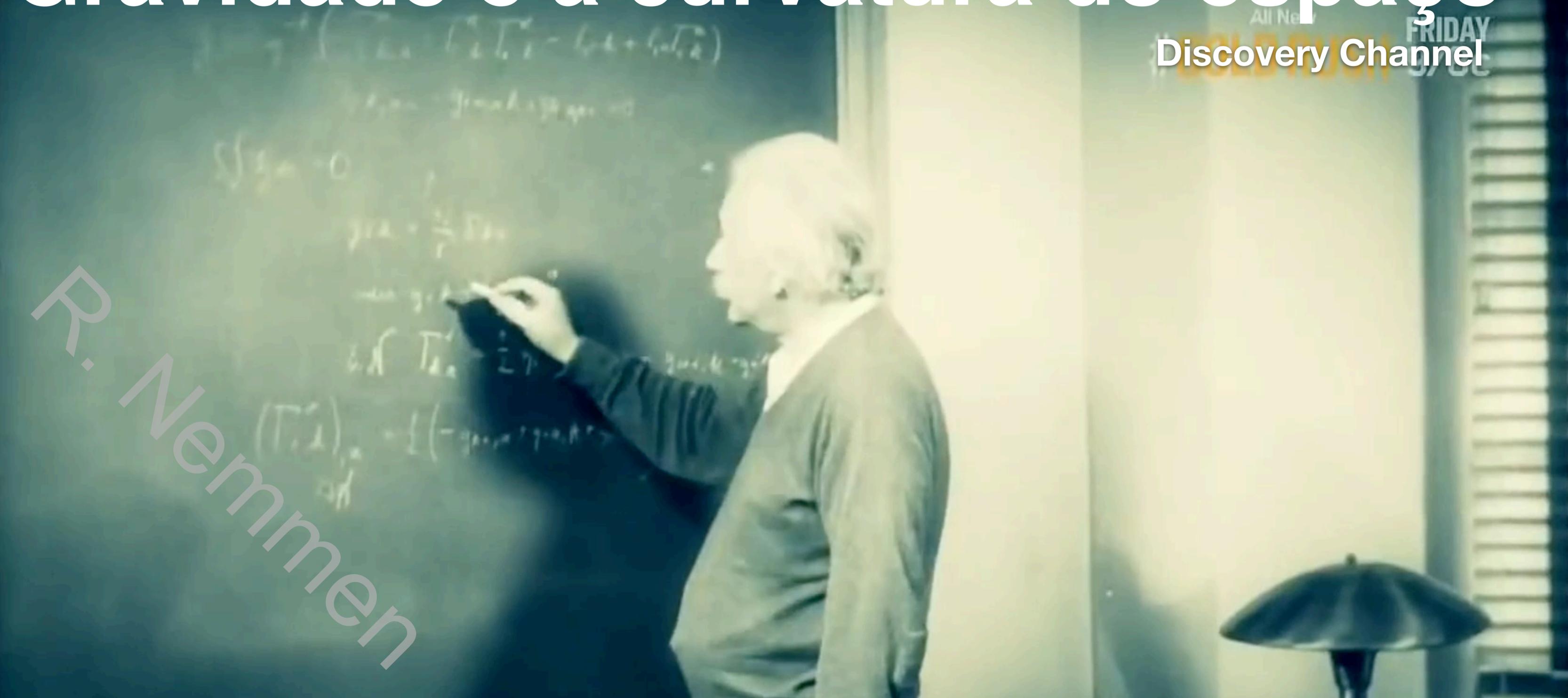
Pseudofísica
Aristotélica

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Relatividade geral de Einstein: Gravidade é a curvatura do espaço

All News
FRIDAY
Discovery Channel
3/8

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Leis da gravitação de Einstein

1. Geometria do espaço-tempo muda na presença de matéria

Equação de campo

2. Objetos se movem tal que sua passagem do tempo é maximizada

Equação de movimento
(equação da geodésica)

1ª lei da gravitação de Einstein



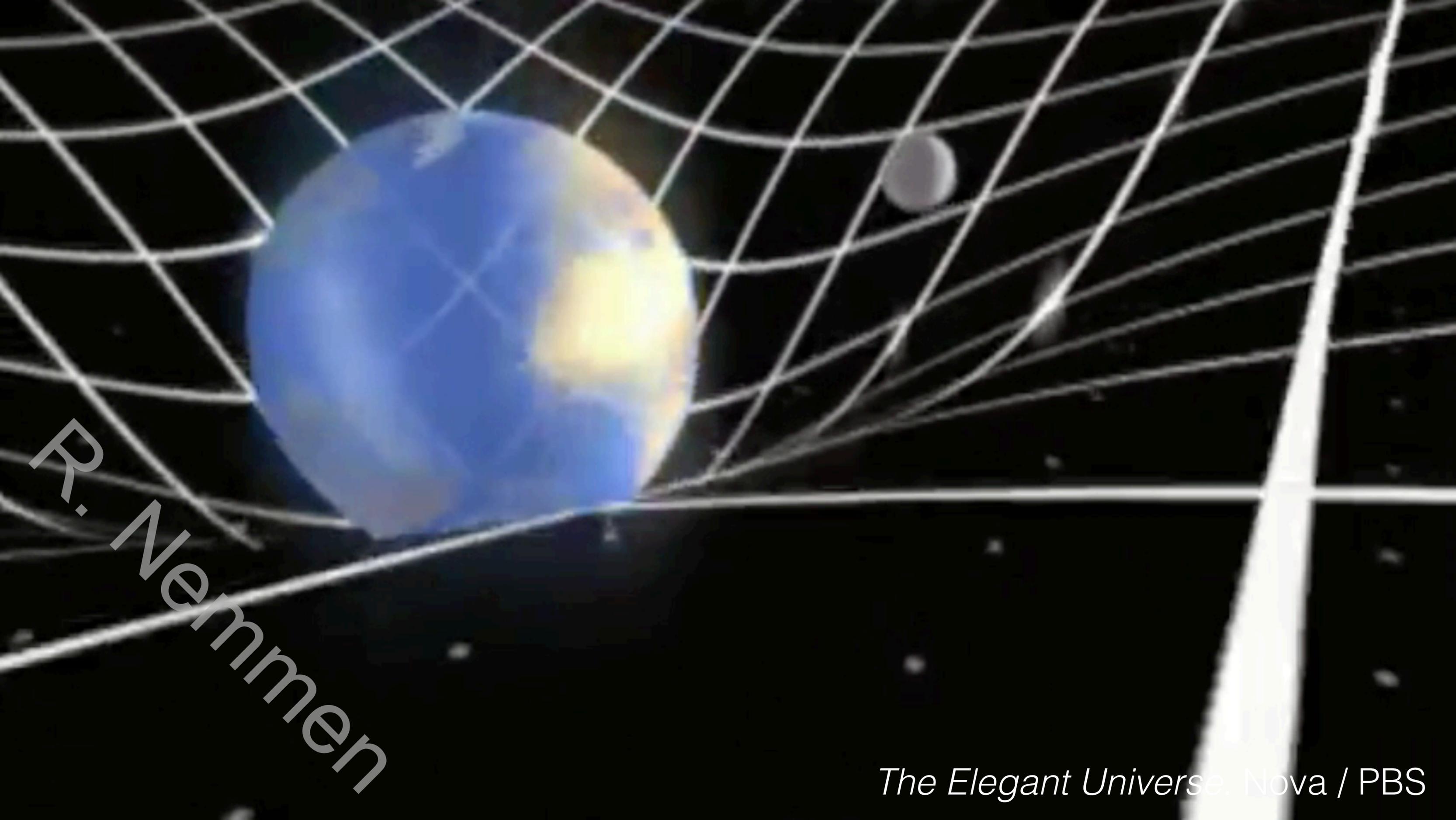
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2ª lei da gravitação de Einstein



Nemmen

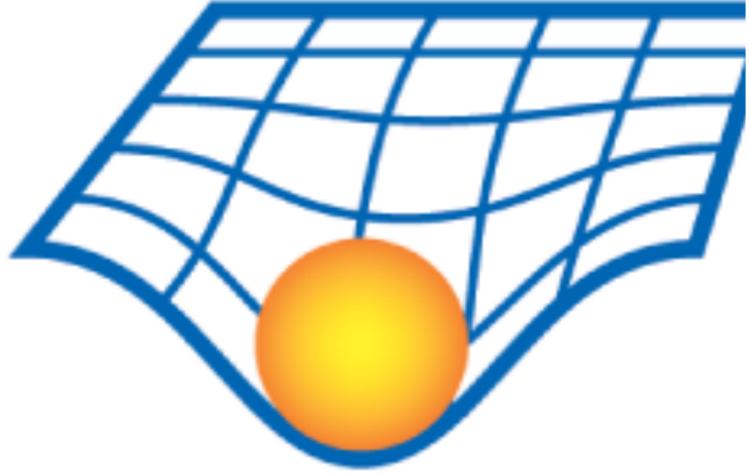
Gravity visualized: <https://www.youtube.com/watch?v=MTY1Kje0yLg&list>



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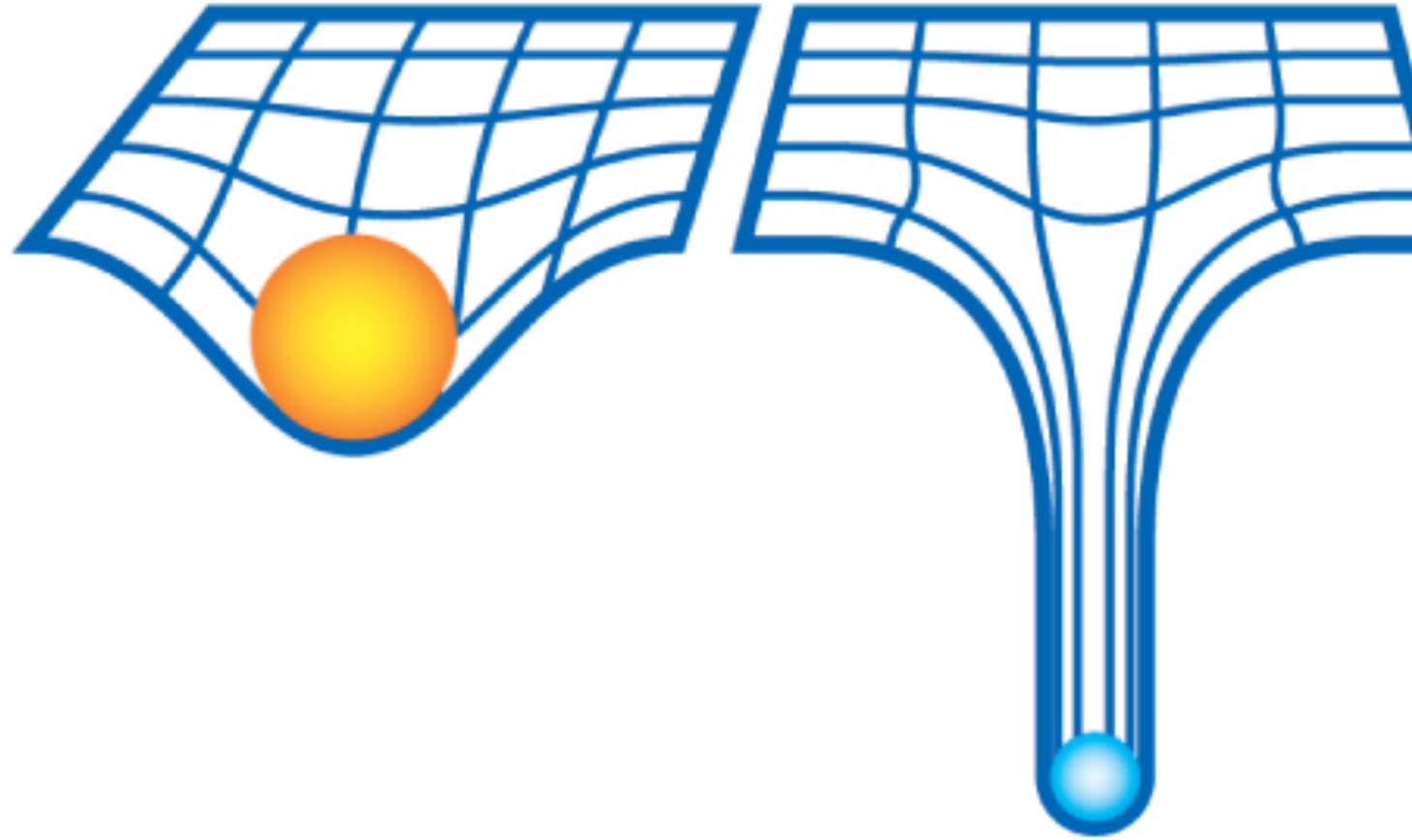
The Elegant Universe, Nova / PBS

Sol



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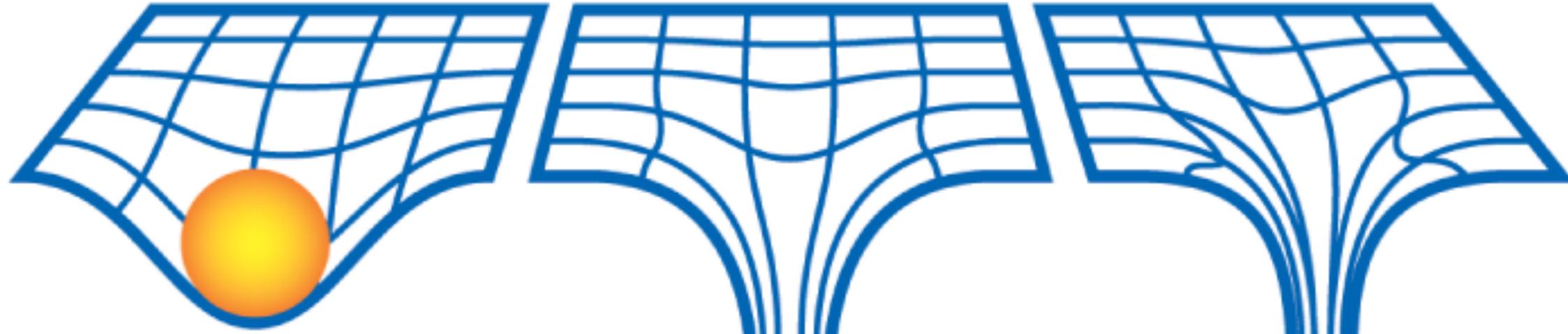
Sol



**Estrela de
nêutrons**

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Sol



Estrela de
nêutrons



Buraco
negro



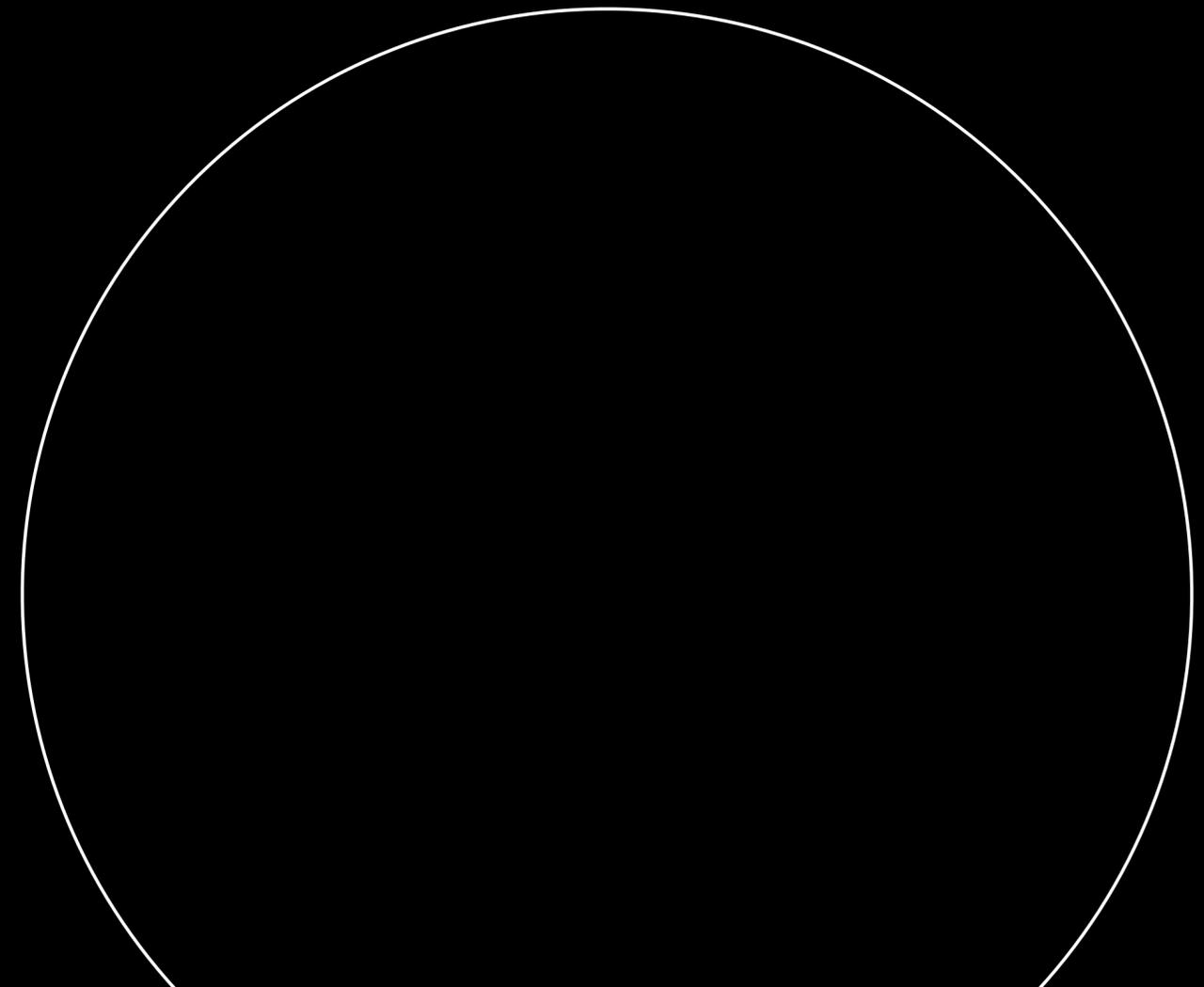
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O que é um buraco negro?



Astro massivo e compacto: gravidade tão forte que aprisiona tudo o que cai dentro dele

Uma vez dentro, nada escapa



Albert Einstein era cético em relação a buracos negros



Chega mais, deixa eu te
contar uma coisa

Buracos negros não
existem

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Eras da gravitação

Idade Antiga

335 AC

Pseudofísica Aristotélica

Idade Média

1687

Mecânica Newtoniana

Idade Moderna

1915

Relatividade Geral
Solução matemática dos buracos negros

1ª Era de Ouro

1963-1975

2ª Era de Ouro

Revisemmen

Eras da gravitação

Idade Antiga

335 AC

Pseudofísica Aristotélica

Idade Média

1687

Mecânica Newtoniana

Idade Moderna

1915

Relatividade Geral

Solução matemática dos buracos negros

1ª Era de Ouro

1963-1975

Renascimento Teórico

Buracos negros giram, vibram, são carecas e evaporam; termodinâmica; singularidades

2ª Era de Ouro

Remember

1ª era de ouro: Renascimento teórico dos buracos negros

1963: Buracos negros giram

Kerr 1963

1964: Energia gravitacional extraível

Salpeter 1964;
Zeldovich 1964

1965: Singularidades

Penrose 1965

1967: BNs carecas

Israel 1967; Carter 1971; Hawking 1972

1969: Energia *rotacional* extraível

Penrose 1969

1971: BNs vibram

Press 1971; Teukolsky 1972

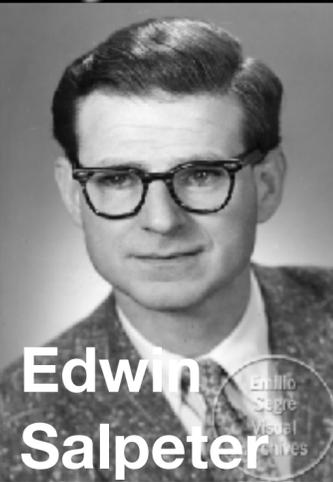
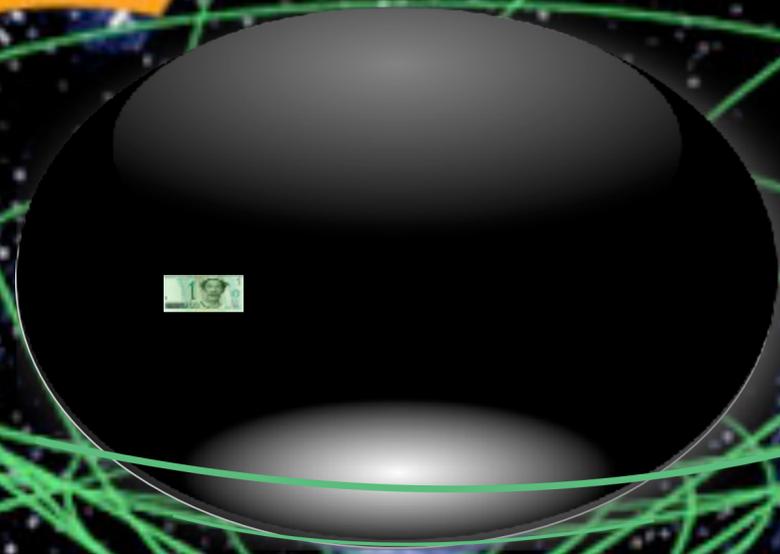
1973: Leis da termodinâmica

Bekenstein 1973; Bardeen+1973

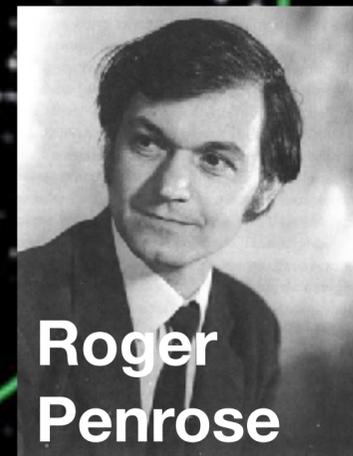
1974: BNs evaporam

Hawking 1974

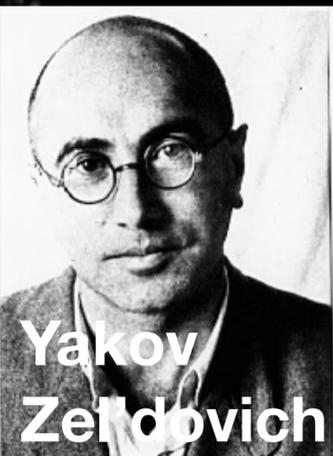
Melhores usinas de energia do universo: Mais de 6% de retorno energético



Edwin Salpeter



Roger Penrose



Yakov Zel'dovich



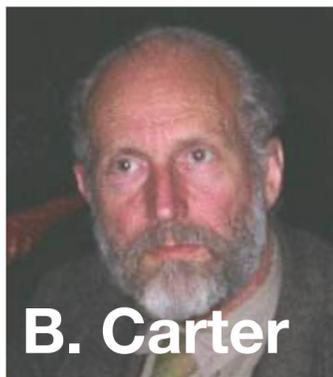
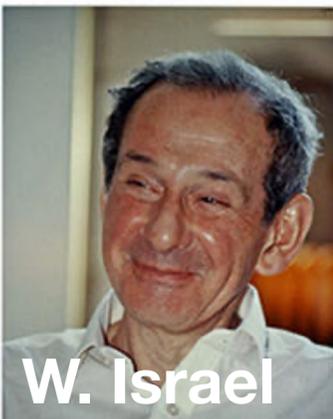
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Buracos negros são carecas

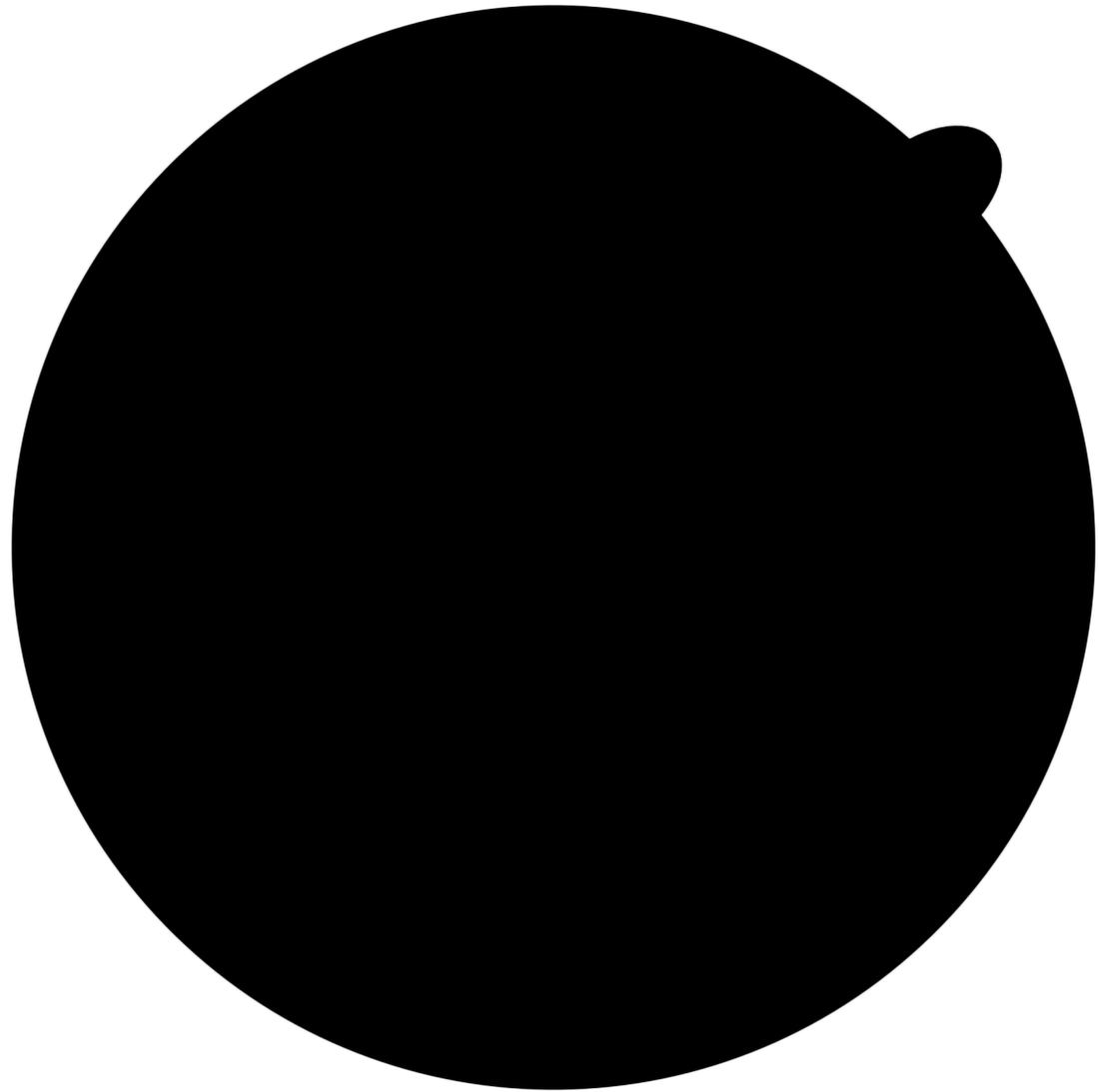
Um buraco negro é caracterizado por **dois números** e nada mais

Mass M

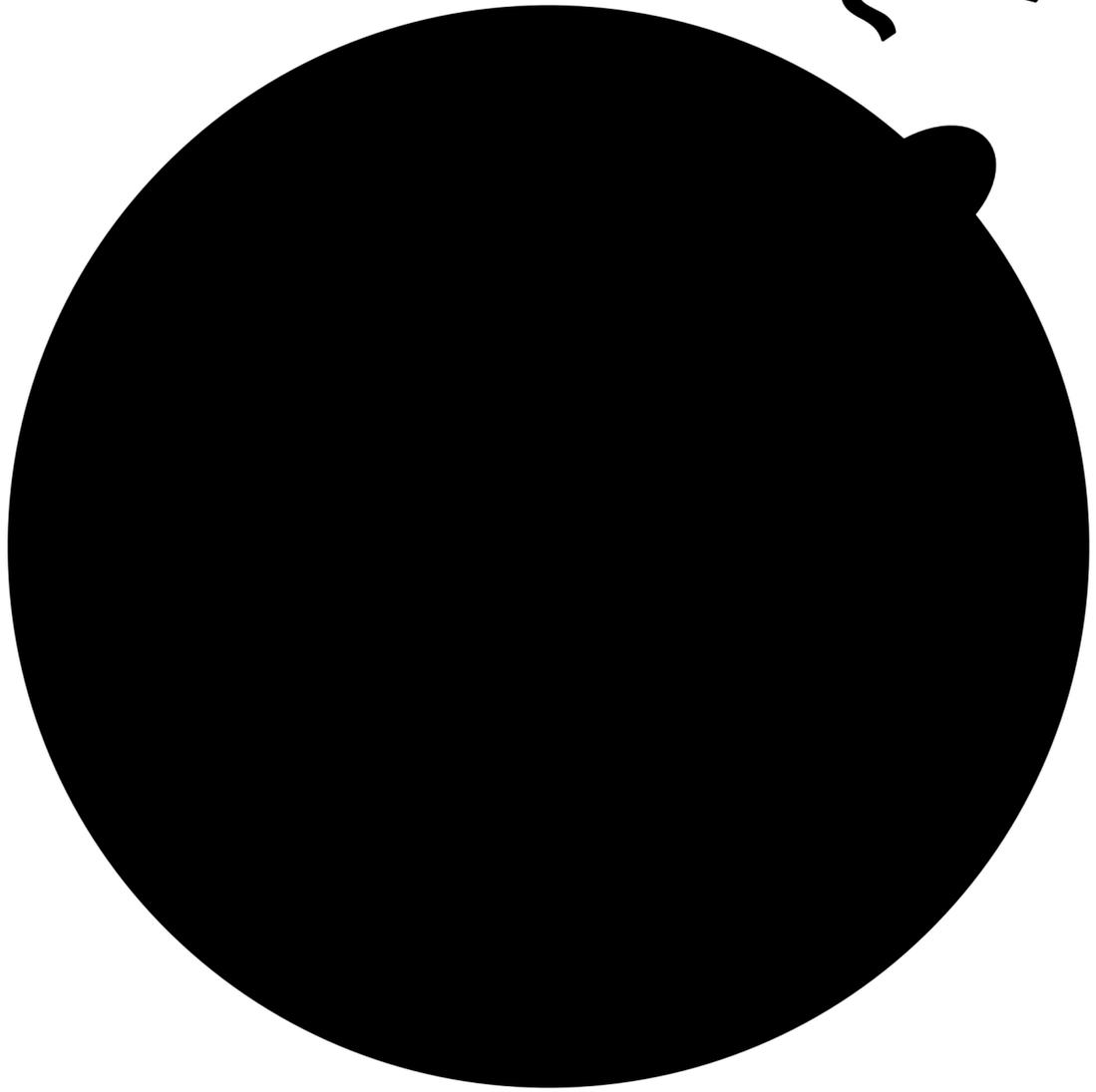
Spin: momento angular a_*



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**ondas
gravitacionais**

Buracos negros evaporam

Possuem temperatura, portanto emitem radiação e perdem massa

∴ BNs não são eternos



Lições: 1ª era de ouro

Buracos negros são:

1. Dinâmicos Giram e vibram

2. Usinas de energia

3. Perecíveis Evaporam e eventualmente desaparecerão

Dominada por avanços *teóricos*

Recap: Aula 1

- **Breve história da gravitação**
- **Leis da gravitação de Einstein**
 - Massa curva o espaço
 - Espaço curvo diz a partículas como se moverem
- **1ª era de ouro dos buracos negros**
 - Principais resultados

References: theory

- ***Physical processes in active galactic nuclei.*** Blandford, R. in ***Active galactic nuclei Saas-Fee lecture notes***
- ***Black holes, white dwarfs and neutron stars.*** Shapiro, S. L. & Teukolsky, S. A. (ch. 12, 14)

More details

- ***Foundations of black hole accretion disk theory.*** Fragile, C. & Abramowicz, M.
- ***The Formation and Disruption of Black Hole Jets.*** Contoupoulos, I. et al. (ch. 3, 6, 7)

References: observations

***Active galactic nuclei.* Beckmann V. & Schrader, C.**

- ***An introduction to active galactic nuclei: Classification and unification.* New Ast. Rev. Tadhunter, C.**
- ***Relativistic jets in active galactic nuclei.* ARAA. Blandford, R.
arXiv:1812.06025**
- ***The Coevolution of Galaxies and Supermassive Black Holes: Insights from Surveys of the Contemporary Universe.* ARAA. Heckman, T. & Best, P.**
- ***Observational Evidence of Active Galactic Nuclei Feedback.* ARAA. Fabian, A.**

What is an active galactic nuclei?

AGN

Presence of accreting, supermassive black hole at the center of a galaxy

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What is an active galactic nuclei?

AGN

Presence of **accreting**, **supermassive** black hole at the center of a galaxy

Mass

$$M > 10^6 M_{\odot}$$

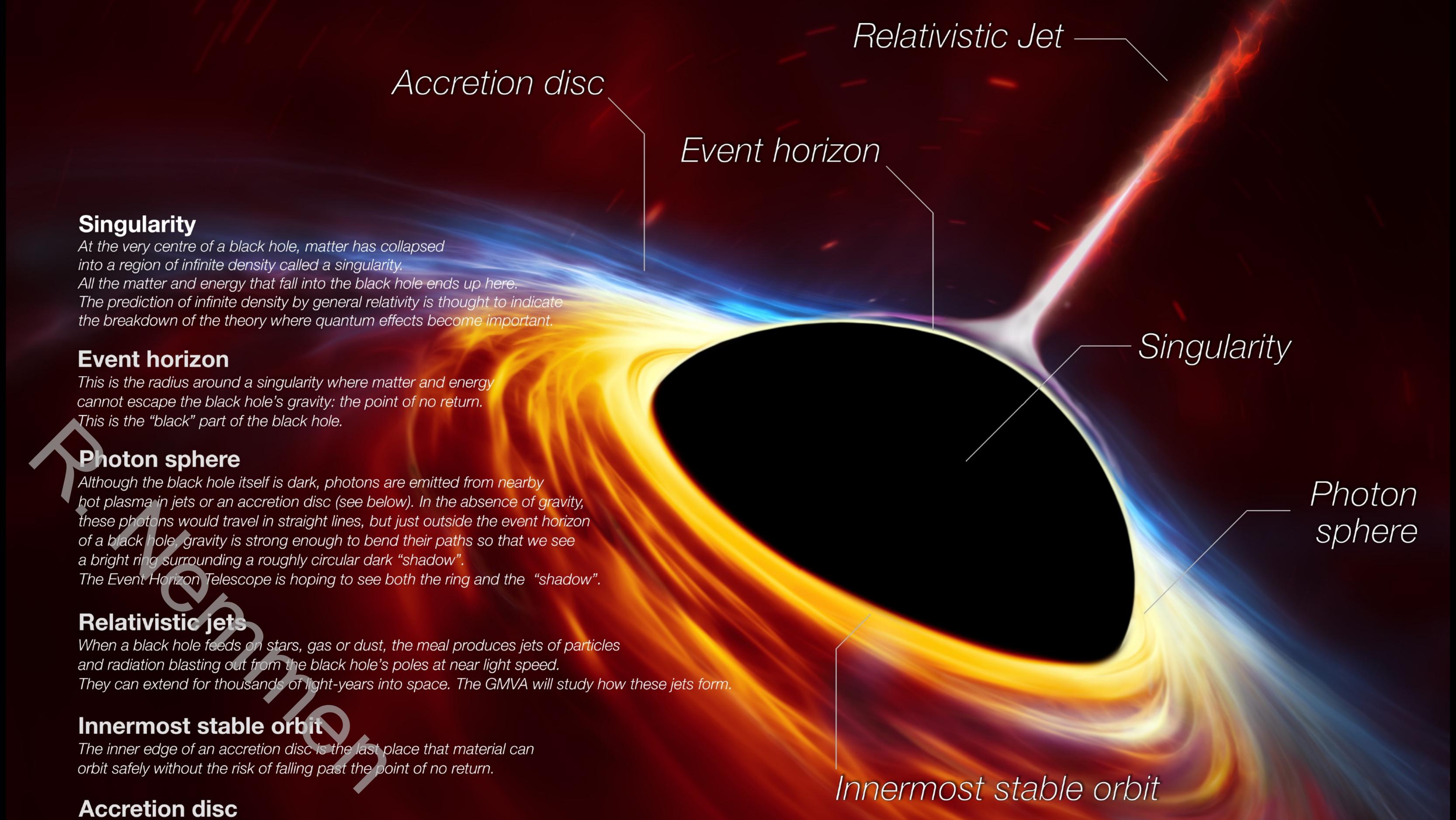
Black hole
feeding rate

$$\dot{M} > 10^{-3} \dot{M}_{\text{Edd}}$$
$$(L > 10^{-5} L_{\text{Edd}})$$





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Singularity

At the very centre of a black hole, matter has collapsed into a region of infinite density called a singularity. All the matter and energy that fall into the black hole ends up here. The prediction of infinite density by general relativity is thought to indicate the breakdown of the theory where quantum effects become important.

Event horizon

This is the radius around a singularity where matter and energy cannot escape the black hole's gravity: the point of no return. This is the "black" part of the black hole.

Photon sphere

Although the black hole itself is dark, photons are emitted from nearby hot plasma in jets or an accretion disc (see below). In the absence of gravity, these photons would travel in straight lines, but just outside the event horizon of a black hole, gravity is strong enough to bend their paths so that we see a bright ring surrounding a roughly circular "shadow". The Event Horizon Telescope is hoping to see both the ring and the "shadow".

Relativistic jets

When a black hole feeds on stars, gas or dust, the meal produces jets of particles and radiation blasting out from the black hole's poles at near light speed. They can extend for thousands of light-years into space. The GMVA will study how these jets form.

Innermost stable orbit

The inner edge of an accretion disc is the last place that material can orbit safely without the risk of falling past the point of no return.

Accretion disc

Accretion disc

Event horizon

Relativistic Jet

Singularity

Photon sphere

Innermost stable orbit

What physics is necessary?

(magneto)hydrodynamics

aka MHD

general relativity
Kerr spacetime

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What physics is necessary?

general relativistic MHD
(GRMHD)

at low accretion rates:
general relativistic kinetic theory
(GRK)

however...

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What physics is necessary?

at $r > 100GM/c^2$ can use Newtonian approximations

- Will use mostly Newtonian treatment here
- Concepts more important than detailed calculations

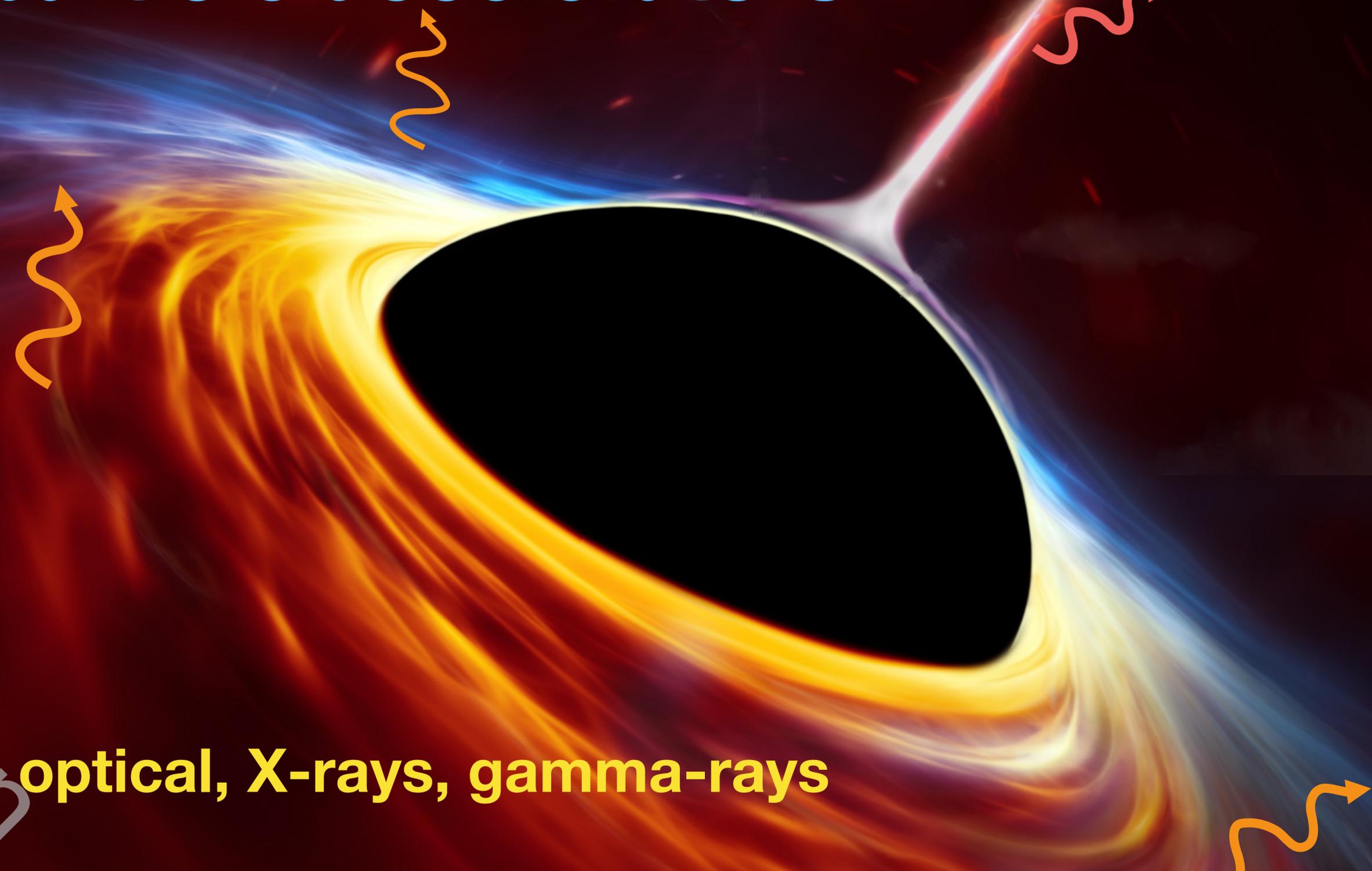
Nature of AGNs: Accreting black holes

Gravitational energy source

- enormous free energy
- can be extracted by particles/fields

AGNs: Powerful electromagnetic radiators, particle accelerators

neutrinos,
cosmic rays



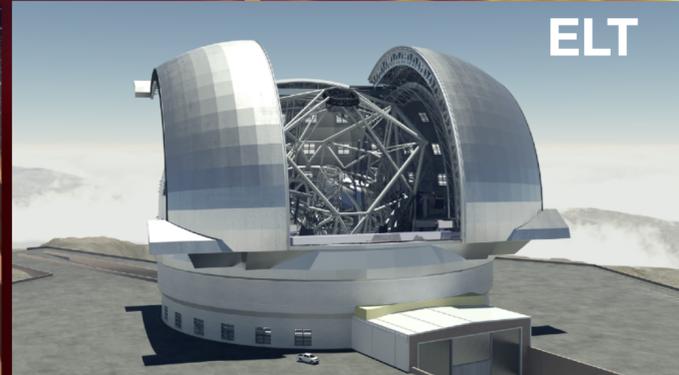
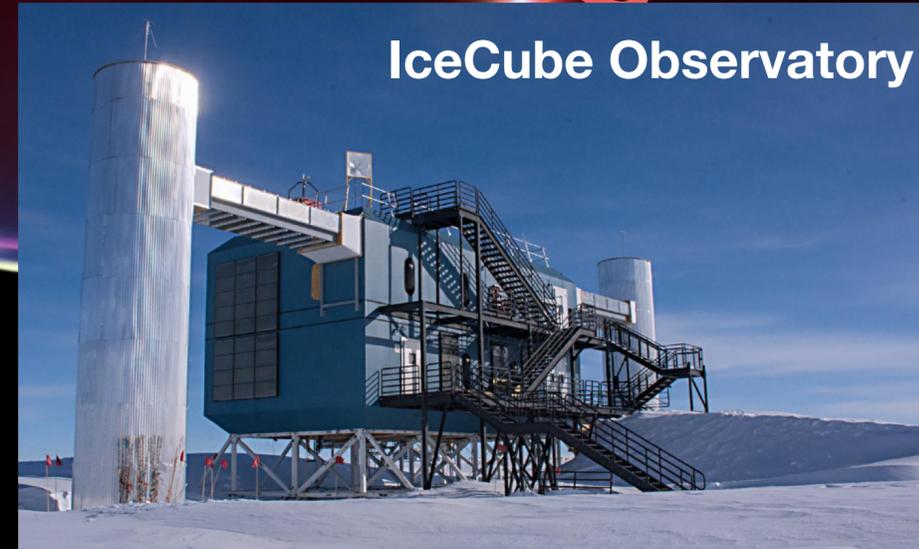
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EM radiation:
radio, infrared, optical, X-rays, gamma-rays

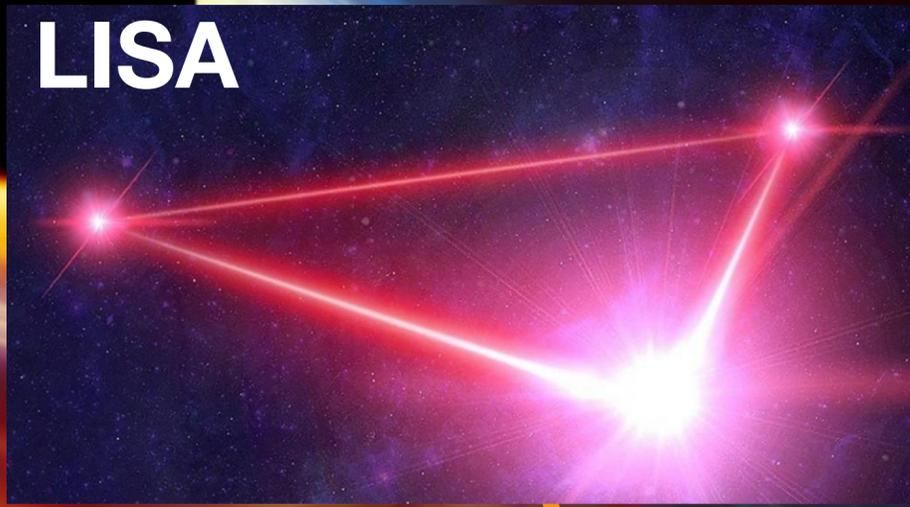
AGNs: Powerful EM radiators, particle accelerators

Crucial for multi messenger astronomy

neutrinos,
cosmic rays



GWs



EM radiation:
radio, infrared, optical, X-rays, gamma-rays

Why are AGNs important?

- **Laboratories to test general relativity, plasma physics**
- **Brightest persistent astronomical sources** ∴ cosmic background
- **Affect large scale structure with their gas outflows and radiation**
- **Reionization sources during dark ages**
- **Crucial sources for multimessenger astronomy: photons, cosmic rays, neutrinos, GWs**

Challenges

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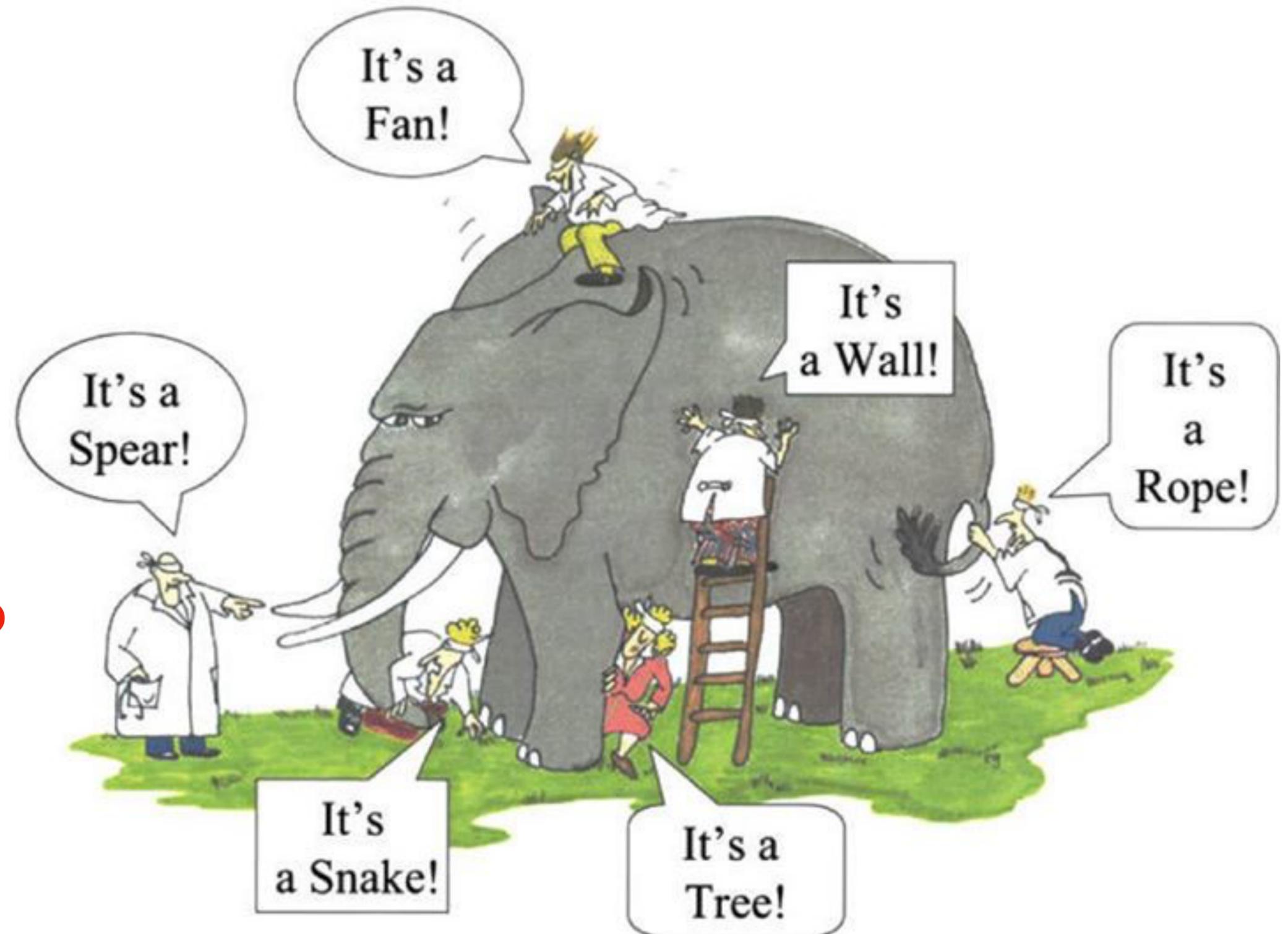


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AGNs: multifaceted phenomenon (challenge #1)

Depending on how you observe, AGNs look different

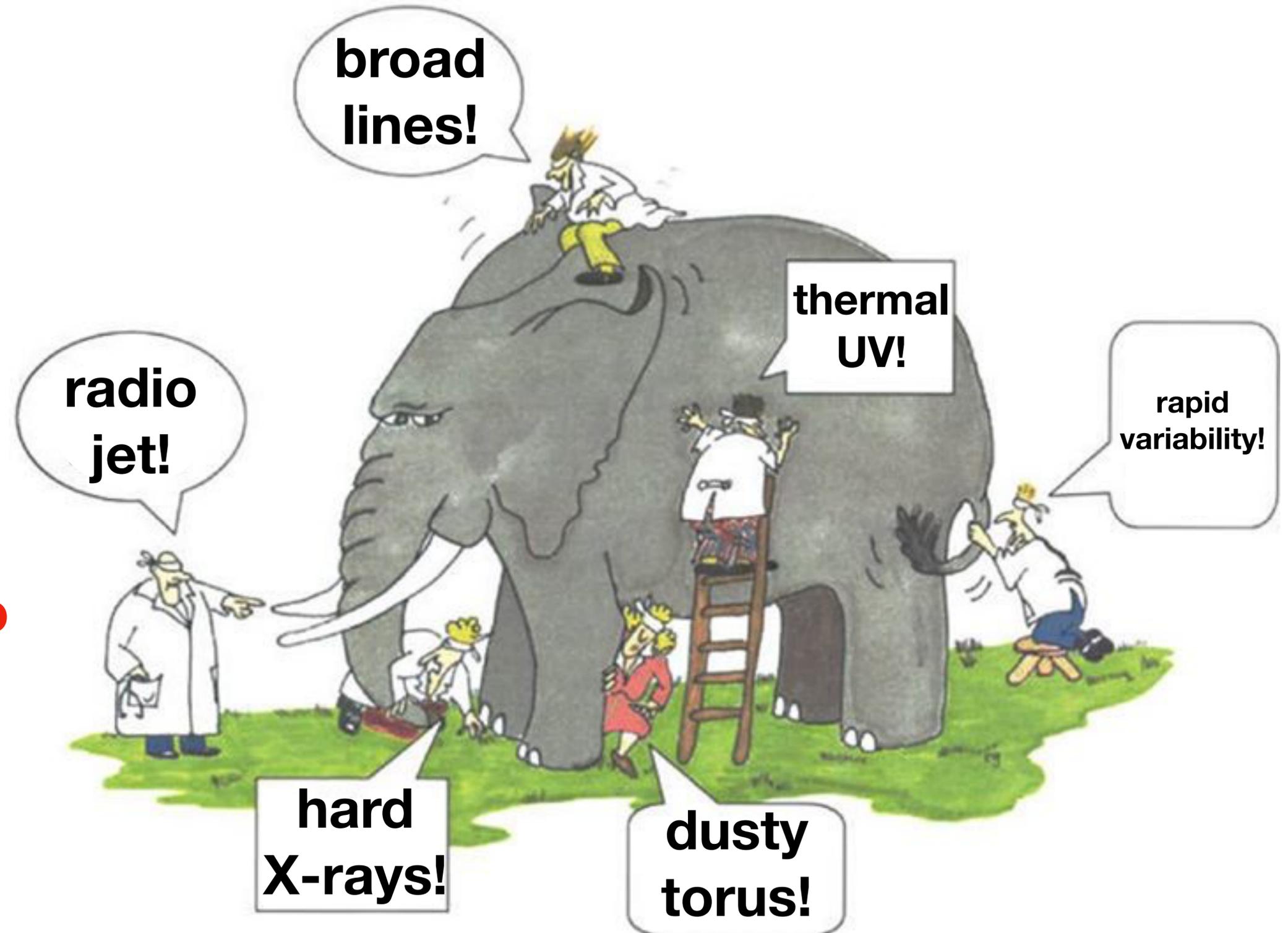
Appearance varies with EM energy band (radio to gamma-rays)



AGNs: multifaceted phenomenon (challenge #1)

Depending on how you observe, AGNs look different

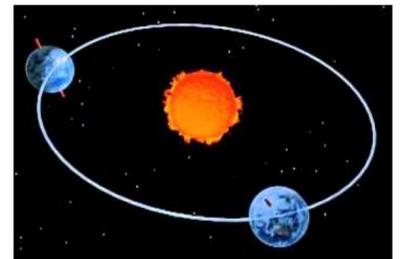
Appearance varies with EM energy band (radio to gamma-rays)



Quasar light curves imply $\Delta t_{\text{var}} < 1$ light-week
variability timescale

Size of system must satisfy $\text{size} < c\Delta t_{\text{var}}$ light-crossing radius

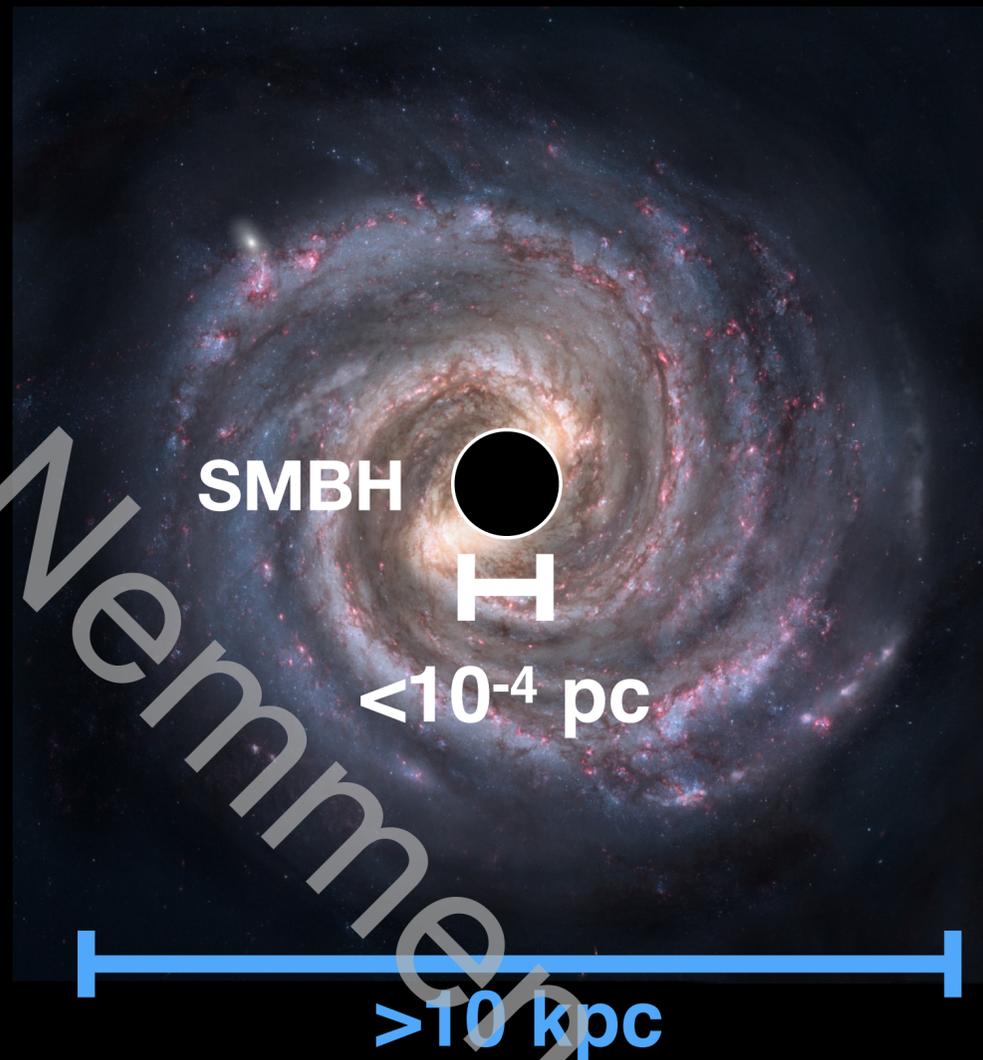
≈ 0.01 pc ~ 1000 AU



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Supermassive black holes (SMBHs) are extremely small on the sky

Very hard to observe (challenge #2)



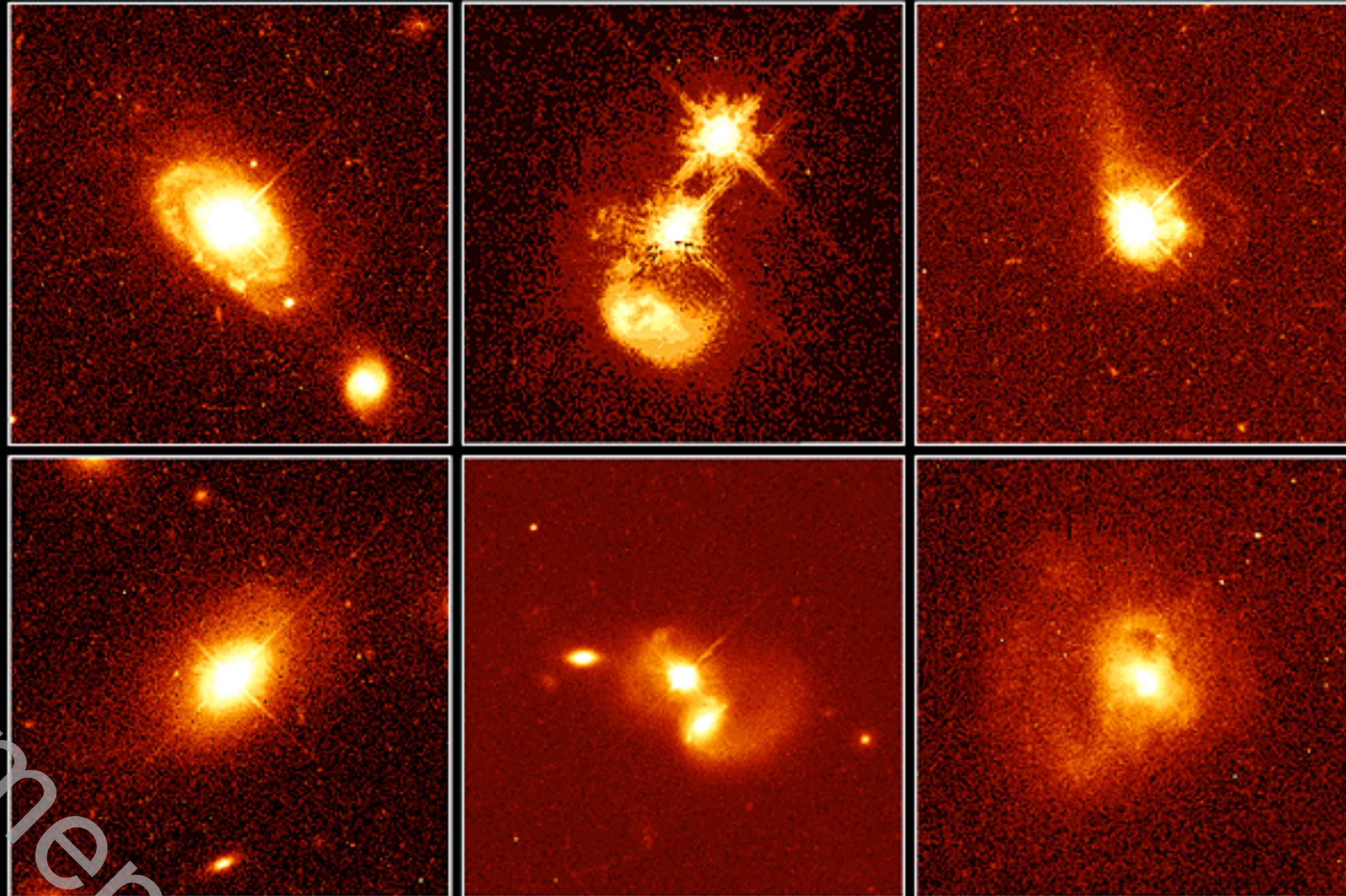
$$\frac{\text{galaxy size}}{\text{event horizon size}} \sim 10^9$$



Grapefruit



AGNs easily outshine their host galaxies (challenge #3)



Hubble Space
Telescope

Bahcall+1997

this image: $z \sim 0.2$
 $d_L \sim 1$ Gpc

Four golden lessons

(1979 Nobel Prize, Physics)

Steven Weinberg

When I received my undergraduate degree — about a hundred years

ago — the world seemed to me a vast, unexplored ocean, every part of which I was beginning to explore. At the beginning of any research, you don't know what you can do or what you can't do. I do anything I can do, and I do everything that I can do. Fortunately, in my first year of school, I had the good fortune to be in the hands of senior physicists who were very patient with my anxious objections and persistent questions. I was surprised to find that I was not it. But I have learned, to continue using my oceanographic metaphor, is that

2003 Nature



work of many theoretical and experimental physicists has been able to sort it out, and put everything (well, almost everything) together in a beautiful theory known as

1. **Start doing research and pick up what you need as you go along** — No one knows everything, and you don't have to.
2. **Aim for the rough water** (“the mess”) — that's where the action is.
3. **Forgive yourself for wasting time**
4. **Learn the history of science** — or at least of your own field.

Scientist

Advice to students at the start of their scientific careers.

ing most of your time not being to being becalmed on the ocean of knowledge.

7, learn something about the history of science, or at a minimum the history of your field of science. The least important part of this is that the history may actually be of use to you in your own scientific work. For instance, now and then scientists are misled by believing one of the overall models of science that have

been proposed by philosophers from the 17th century. Thomas Kuhn and Karl Popper are antidotes to the philosophy of science. The edge of the history of science is important, the history of your work seem more w



slide by Ken Nagamine

Recap: Aula 2

- O que é um AGN
- Componentes: ●, acreção, jatos
- Desafios do estudo de AGNs
 - Multifacetados
 - Minúsculo tamanho angular
 - Muito brilhantes!

Historical perspective on AGNs

- 1783:** Newtonian “dark stars” predicted Michell 1783
- 1915:** Einstein publishes his field equation Einstein 1915
- 1916:** black hole solution derived from GR Schwarzschild 1916
- 1918:** "curious straight ray" in galaxy M87, "connected with the nucleus by a thin line of matter" — jets discovered Curtis 1918
- 1963:** strong optical point source found at 3C 273 nucleus — quasars discovered Schmidt+1963
- Early 1990s:** HST finds SMBHs at centers of nearby galaxies Ford+1994;
Harms+1994;
Ferrarese &
Ford 2004
- Late 1990s:** stellar orbits at Galactic Center — strongest BH case until 2015 (Sagittarius A*, $4 \times 10^6 M_{\odot}$) Genzel &
Gillessen 2010

Historical perspective on AGNs

- Late 1990s, early 2000s:** M - σ relation – SMBHs and host galaxies are tightly connected  **Magorrian+1998; Kormendy & Ho 2013**
- 2000:** SMBHs disturb thermodynamics of entire galaxy clusters **McNamara+2000; Fabian 2012**
- 2003:** Sloan Digital Sky Survey (SDSS) finds $>100k$ AGNs **Abazajian+2003**
- 2015:** direct observation of gravitational waves from stellar-mass BHs  **Abbott+2015**
- 2018a:** 1st multimessenger observation from AGNs (blazar TXS 0506+056) **IceCube, Fermi LAT Collaborations**
- 2018b:** GRAVITY resolves orbit at $r = 7M$ (Sgr A*) **Abuter+2018**
- 2019:** EHT images event horizon (M87*) **EHTC**

(new technologies)·(engineering)
= (new astronomical windows)

(new observations)×(grad students)
= paradigm change



General lessons from history

~ Pace of discovery is **accelerating**

~ Future: immense discovery space

awaiting

~ We entered **2nd golden age** of

black hole (astro)physics

Black hole physics

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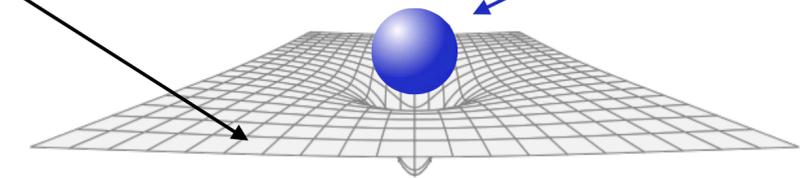
A general relativity primer

Einstein's field equation

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = \frac{8\pi G}{c^4}T_{\mu\nu}$$

Ricci curvature Metric Ricci scalar Stress-energy

\Rightarrow spacetime curvature = constant \times matter-energy



Solution to field equation gives

$$g_{\mu\nu} \quad ds^2 = g_{\mu\nu}dx^\mu dx^\nu$$

Metric Line element



Newtonian analogue

$$\nabla^2 \phi = 4\pi G \rho \quad \text{Poisson equation}$$

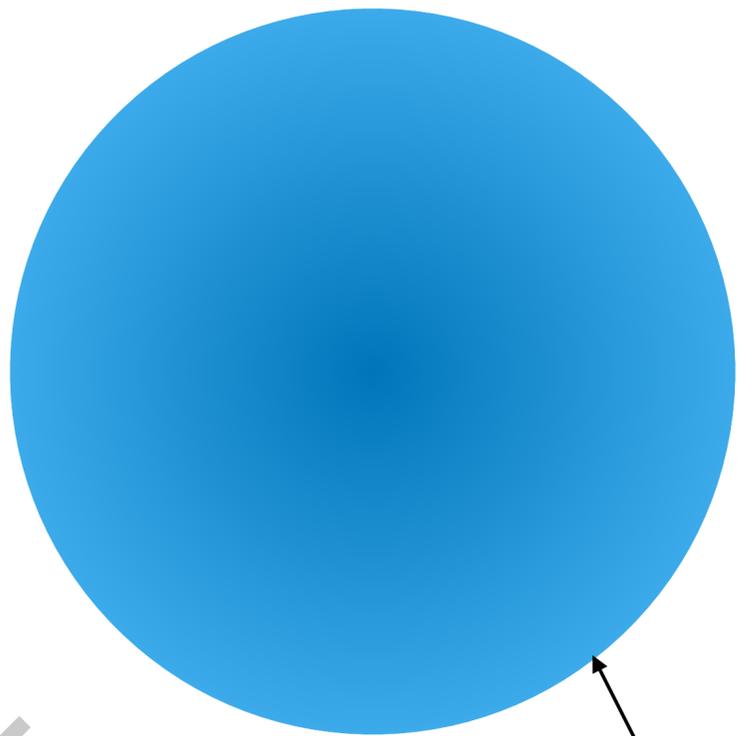
For a free particle:

$$\delta S = 0 \rightarrow \frac{d^2 x^\mu}{d\tau^2} + \Gamma_{\alpha\beta}^\mu \frac{dx^\alpha}{d\tau} \frac{dx^\beta}{d\tau} = 0$$

Geodesic equation

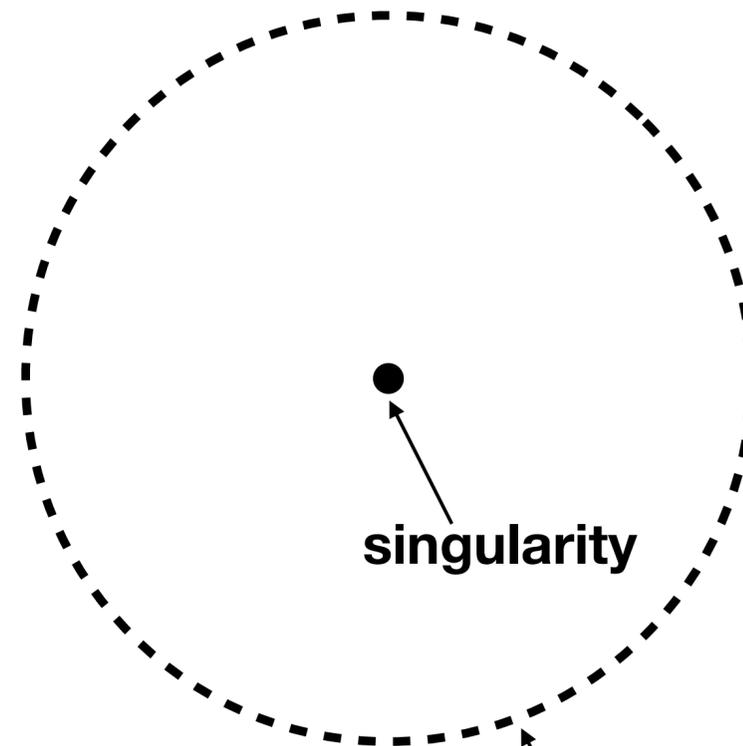
What is a black hole? Remarkable prediction of general relativity

Normal object



surface

Black hole



singularity

event horizon

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Event horizon: one-way membrane, matter/energy can fall in, but nothing gets out

Region inside event horizon causally cut-off from outside

Radius of event horizon:

$$R_S = \frac{2GM}{c^2} = 2.95 \left(\frac{M}{M_\odot} \right) \text{ km}$$

Schwarzschild radius

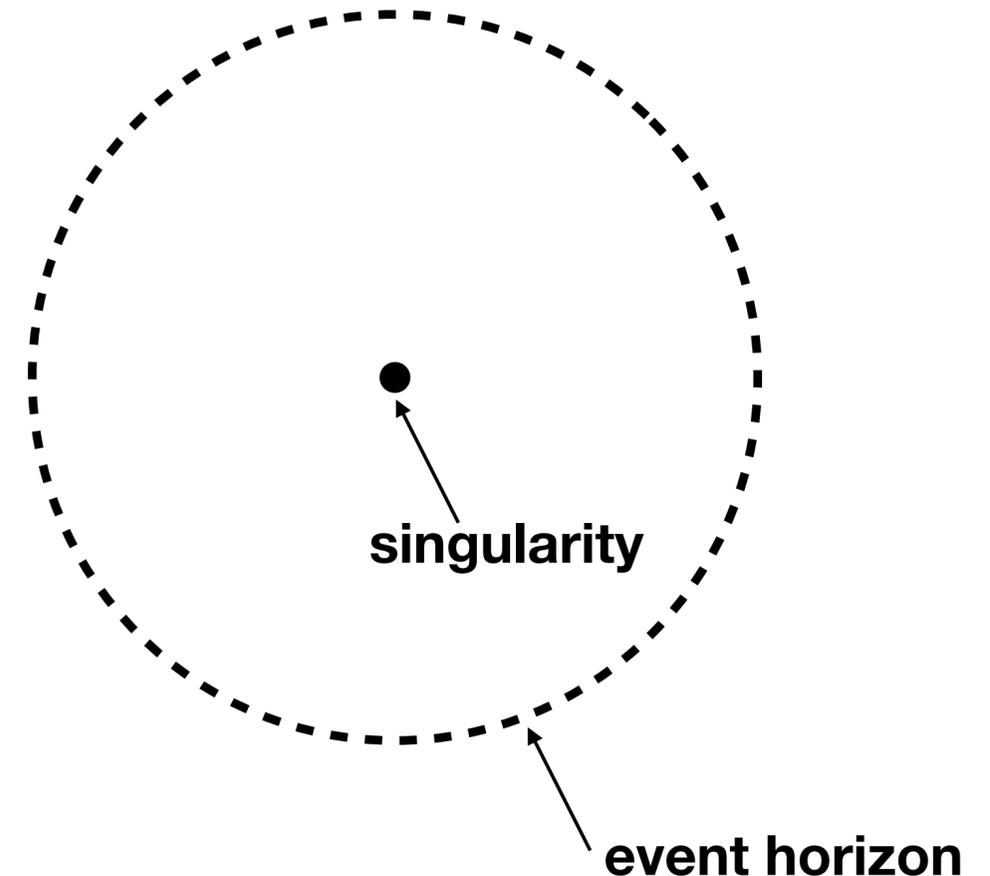


Gravitational radius:

$$R_g \equiv \frac{GM}{c^2}$$

Useful scale

Black hole



Growth of black holes

If particles fall into the black hole

- **M increases**
- **Schwarzschild radius $R_s = 2M$ increases**
- **surface area increases**

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Growth of black holes

If particles fall into the black hole

- M increases
- Schwarzschild radius $R_s = 2M$ increases
- surface area increases

There is no limit to how big a BH can grow. From astrophysics:

- $M_{\min} = 3.3 M_{\text{Sun}}$
- $M_{\max} \sim 10^{10} M_{\text{Sun}}$

A black hole has no hair

All black hole solutions of Einstein's equation completely characterized by only three externally observable classical parameters:

Mass M

Spin: angular momentum J

Charge Q

$$J \equiv a \frac{GM^2}{c}$$

$$-1 \leq a \leq 1 \text{ spin parameter}$$

No-hair theorem

All other information (“hair”=metaphor) disappears behind the event horizon, therefore permanently inaccessible to external observers

Types of black holes

Mass M

Schwarzschild spacetime

Spin a

Kerr spacetime

Charge Q

Reissner–Nordström spacetime

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Schwarzschild black hole

- Simplest black hole
- Spherically symmetric spacetime
- Relatively “easy” to handle analytically

Schwarzschild geometry in Schwarzschild coordinates

$$ds^2 = - \left(1 - \frac{2M}{r} \right) dt^2 + \left(1 - \frac{2M}{r} \right)^{-1} dr^2 + r^2 (d\theta^2 + \sin^2 \theta d\phi^2)$$

Kerr black hole

Conservation of angular momentum leads to spinning black holes

Rotational energy deforms spacetime → Kerr spacetime

Kerr metric considerably more complex than Schwarzschild

$$ds^2 = - \left(1 - \frac{2Mr}{\rho^2} \right) dt^2 - \frac{4Mar \sin^2 \theta}{\rho^2} d\phi dt + \frac{\rho^2}{\Delta} dr^2 + \rho^2 d\theta^2 + \left(r^2 + a^2 + \frac{2Mra^2 \sin^2 \theta}{\rho^2} \right) \sin^2 \theta d\phi^2$$

Boyer-Lindquist coords.

$$a \equiv J/M, \quad \rho^2 \equiv r^2 + a^2 \cos^2 \theta, \quad \Delta \equiv r^2 - 2Mr + a^2$$

Main parameters for *astrophysical* BHs

Gravity units

Mass M ($M_{\odot} = 2 \times 10^{33}$ g)

Spin a_* (1 = max spin)

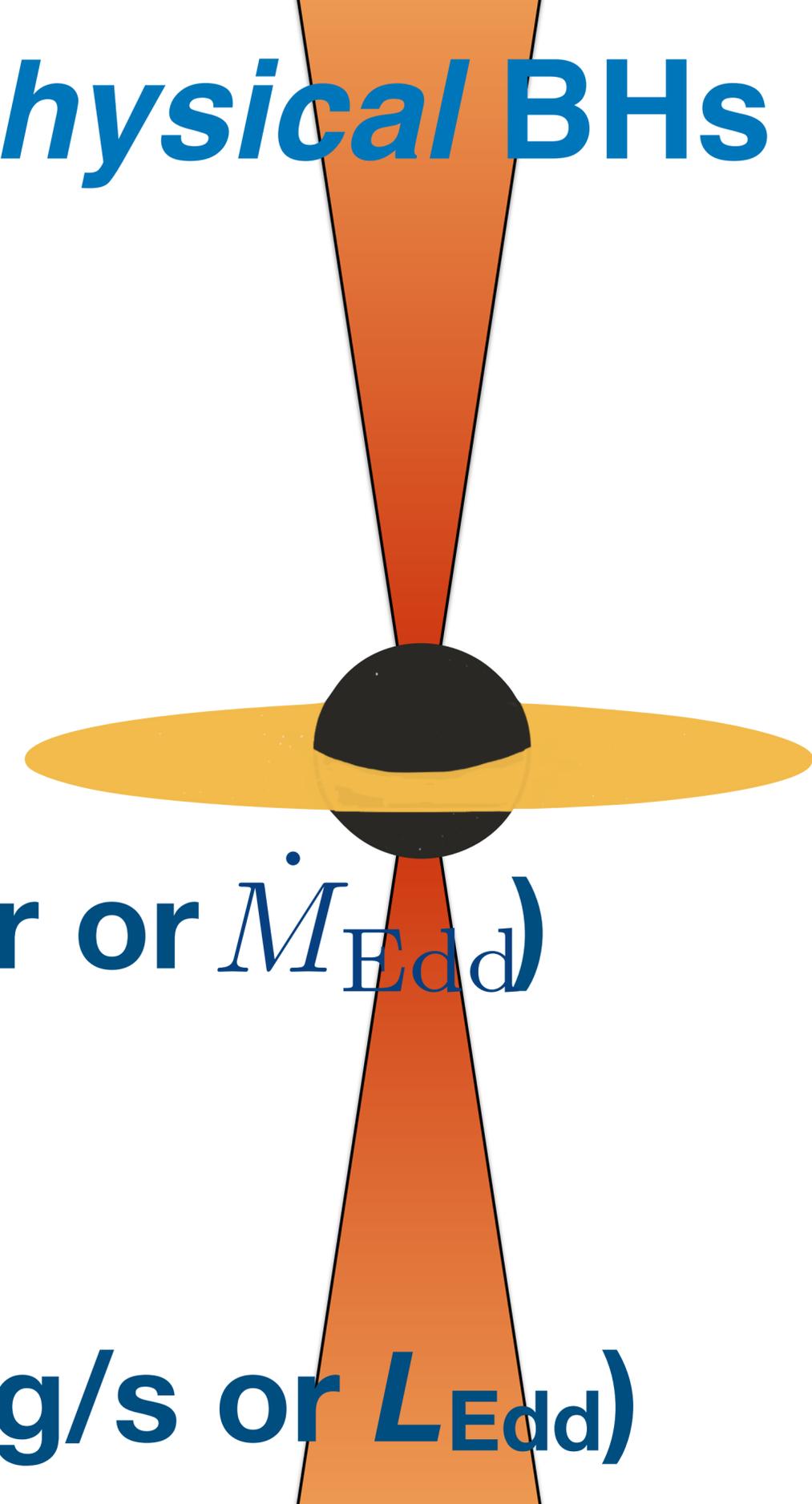
Accretion

Mass accretion rate \dot{M} (M_{\odot}/yr or \dot{M}_{Edd})

Magnetic flux Φ

Predict

Energy output in all forms (erg/s or L_{Edd})



Main problem in BH astrophysics

$$\text{AGN}(t) = f(M, a_*, \dot{M})$$

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Eddington luminosity L_{Edd}

Luminosity L

from central object



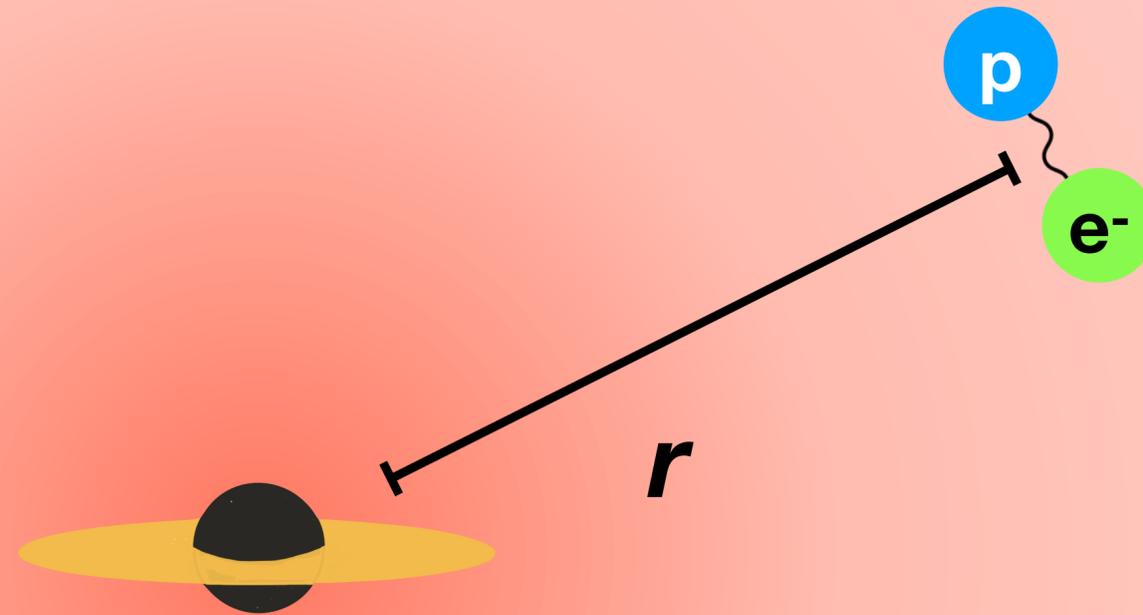
photon
field

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Eddington luminosity L_{Edd}

Luminosity L

from central object



When is the radiation *strong enough to prevent accretion* of particles?

Solve this to get L_{Edd} : $F_{\text{rad}} = F_g$

$$P_{\text{rad}} = \frac{F_{\text{rad}}}{A_{\text{area}}} = \frac{F_{\text{flux}}}{c}$$

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Solve this to get L_{Edd} : $F_{\text{rad}} = F_g$

$$P_{\text{rad}} = \frac{F_{\text{rad}}}{A_{\text{area}}} = \frac{\overset{\text{flux}}{F}}{c} \Rightarrow F_{\text{rad}} = \overset{\text{radiation force on an electron}}{\frac{F A}{c}}$$

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Solve this to get L_{Edd} : $F_{\text{rad}} = F_g$

$$P_{\text{rad}} = \frac{F_{\text{rad}}}{A_{\text{area}}} = \frac{F_{\text{flux}}}{c} \Rightarrow F_{\text{rad}} = \frac{F_{\text{radiation force on an electron}} A}{c} \Rightarrow F_{\text{rad}} = \frac{L}{4\pi r^2} \frac{\sigma_T}{c}$$

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Solve this to get L_{Edd} : $F_{\text{rad}} = F_g$

$$P_{\text{rad}} = \frac{F_{\text{rad}}}{A_{\text{area}}} = \frac{F}{c} \Rightarrow F_{\text{rad}} = \frac{F A}{c} \Rightarrow F_{\text{rad}} = \frac{L}{4\pi r^2} \frac{\sigma_T}{c}$$

flux
radiation force on an electron

$$F_g = \frac{GM(m_e + m_p)}{r^2} \approx \frac{GMm_p}{r^2}$$

why?

$$L_{\text{Edd}} = \frac{4\pi GMm_p c}{\sigma_T} = 1.3 \times 10^{38} \left(\frac{M}{M_{\odot}} \right) \text{ erg s}^{-1}$$

Eddington luminosity: importance

$$L > L_{\text{Edd}}$$



photon
field



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Eddington luminosity: importance

Useful luminosity unit in BH astrophysics

A system radiating at $L > L_{\text{Edd}}$ can halt mass accretion due to strong radiation pressure

Roughly maximal luminosity that can be powered by accretion (if spherical symmetry)

R. Klemmen

Eddington accretion rate

- Assume an engine radiating at $L = L_{\text{Edd}}$
- If it were converting mass to radiative energy with efficiency η

R. Nemmen

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Eddington accretion rate

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- If it were converting mass to radiative energy with efficiency η

$$L_{\text{Edd}} = \eta \dot{M}_{\text{Edd}} c^2$$

\Rightarrow

$$\dot{M}_{\text{Edd}} \equiv \frac{L_{\text{Edd}}}{\eta c^2}$$

usually $\eta = 0.1$

Useful accretion rate
unit in BH astrophysics

$$= 3 \left(\frac{0.1}{\eta} \right) \left(\frac{M}{10^8 M_{\odot}} \right) M_{\odot} \text{ yr}^{-1}$$

Eddington time t_{Edd}

also known as Salpeter time t_s

Assume BH accreting at Eddington rate

$$\dot{M} = \frac{dM}{dt} = \dot{M}_{\text{Edd}} \Rightarrow \frac{dM}{dt} = \frac{M}{t_{\text{Edd}}}$$

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Useful timescale

$$t_{\text{Edd}} \equiv \frac{\eta c \sigma_T}{4\pi G m_p} = 4 \times 10^7 \left(\frac{\eta}{0.1} \right) \text{ yr}$$

Useful websites and apps for grad students

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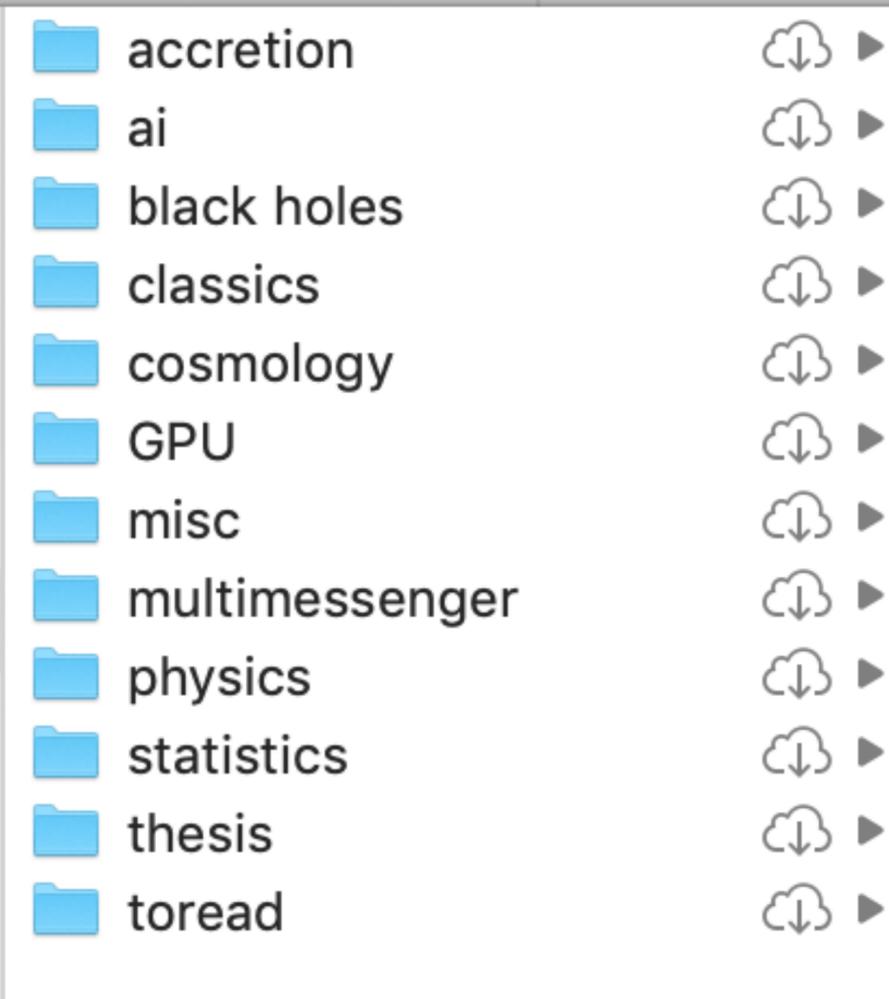
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Pro tips

Organize papers using convention:

1. **Folders named after categories**
2. **Filename:** <Last name of first author><publication year>
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R. Nemmen

🔍 nemmen2012



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A Universal Scaling for the Energetics of Relativistic Jets from Black Hole Systems

R. S. Nemmen *et al.*
Science **338**, 1445 (2012);
DOI: 10.1126/science.1227416

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Important lengths from now on, $G = c = 1$

r_{isco} : Innermost stable circular orbit

$$r_{\text{isco}} = 6M \quad \text{for } a_* = 0$$

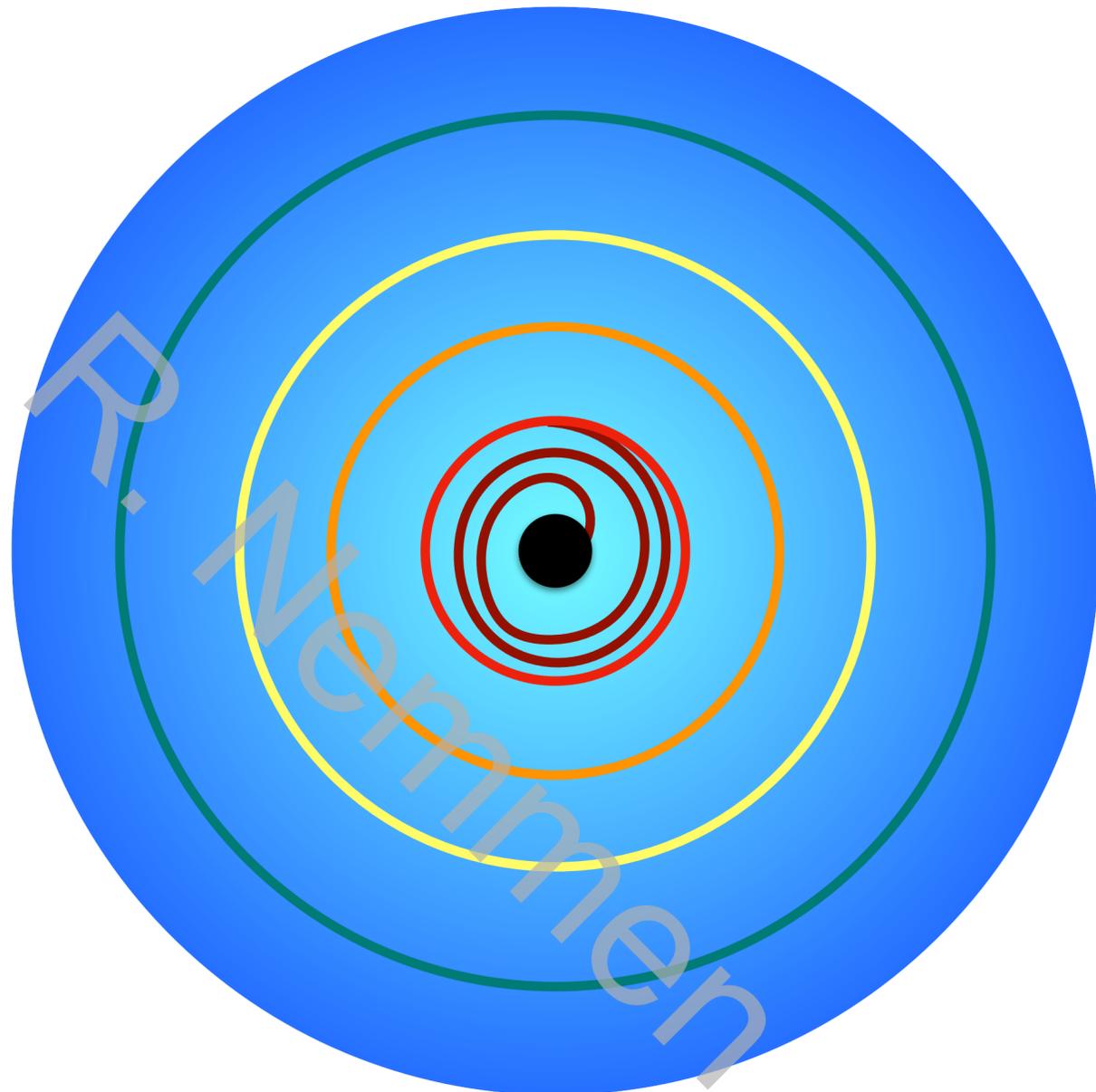
R. Nemmen

Effective potential for orbits around a Schwarzschild black hole

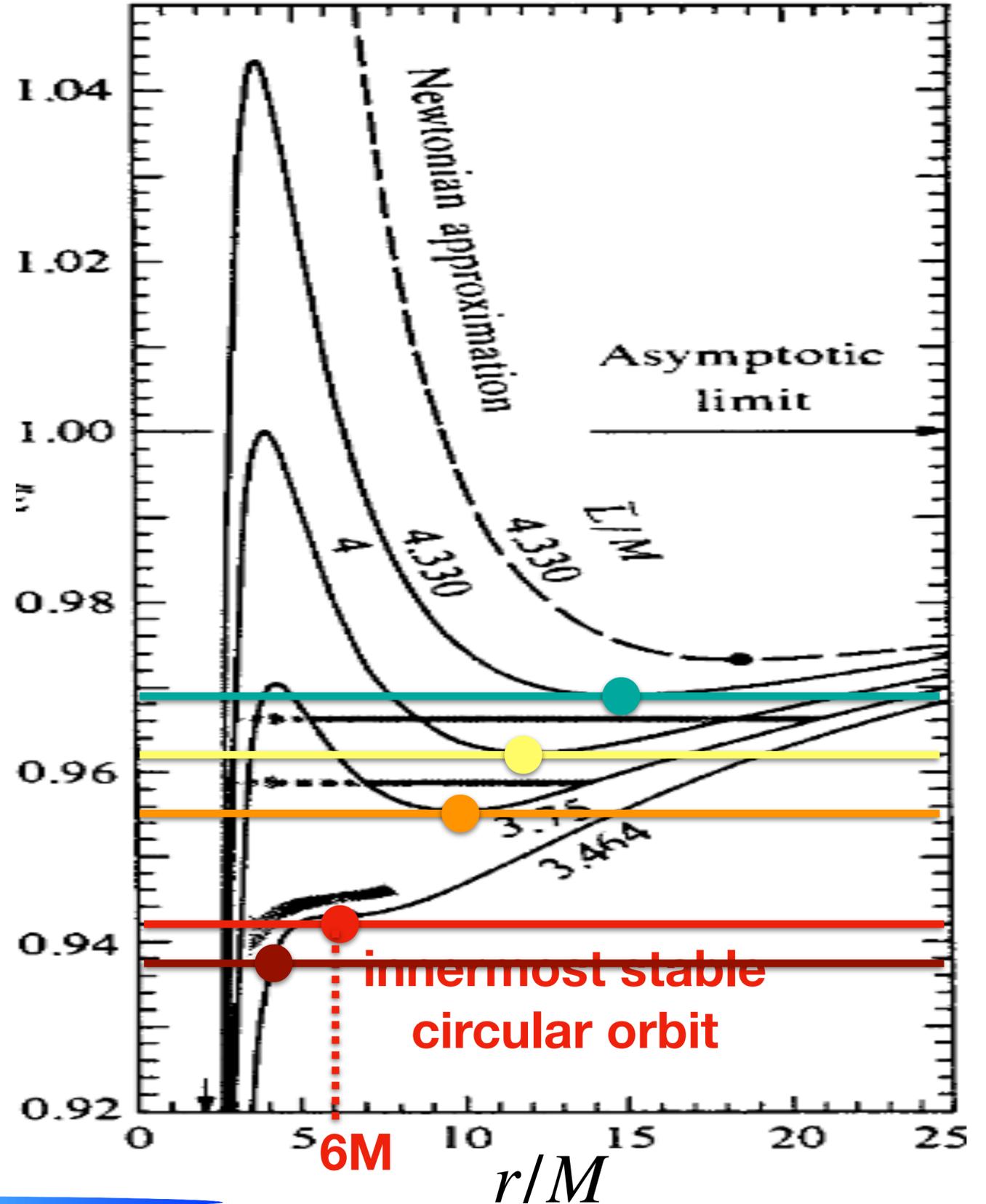
$$E = \frac{1}{2} \left(\frac{dr}{d\tau} \right)^2 + V_{\text{eff}}$$

effective potential

face-on view of accretion disk



V_{eff}



edge-on view

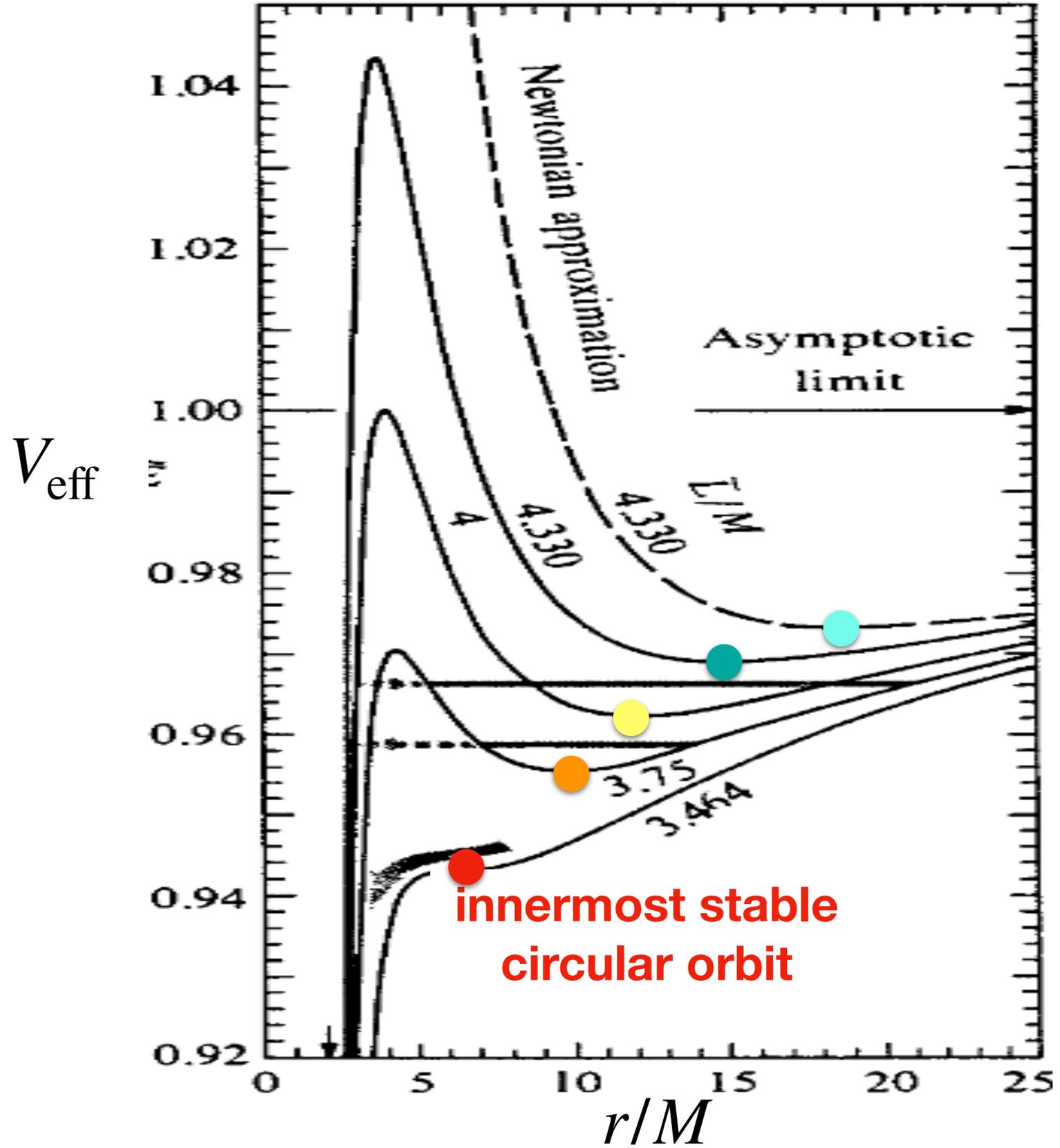


Effective potential for orbits around a Schwarzschild black hole

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effective potential

face-on view of accretion disk



Misner, Thorne & Wheeler

Important radii

from now on, $G = c = 1$

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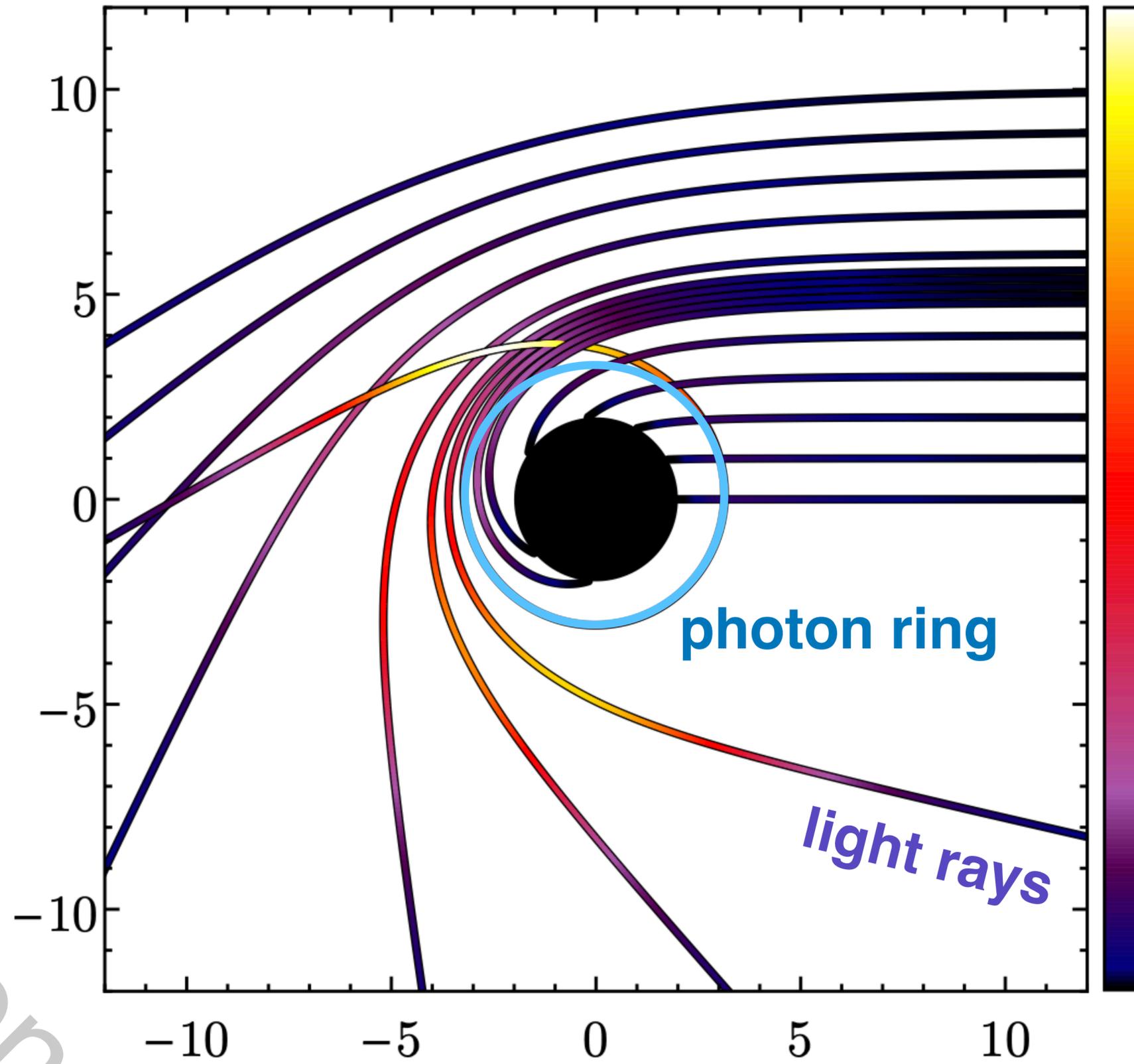
r_c : photon capture radius

also called photon sphere or photon ring

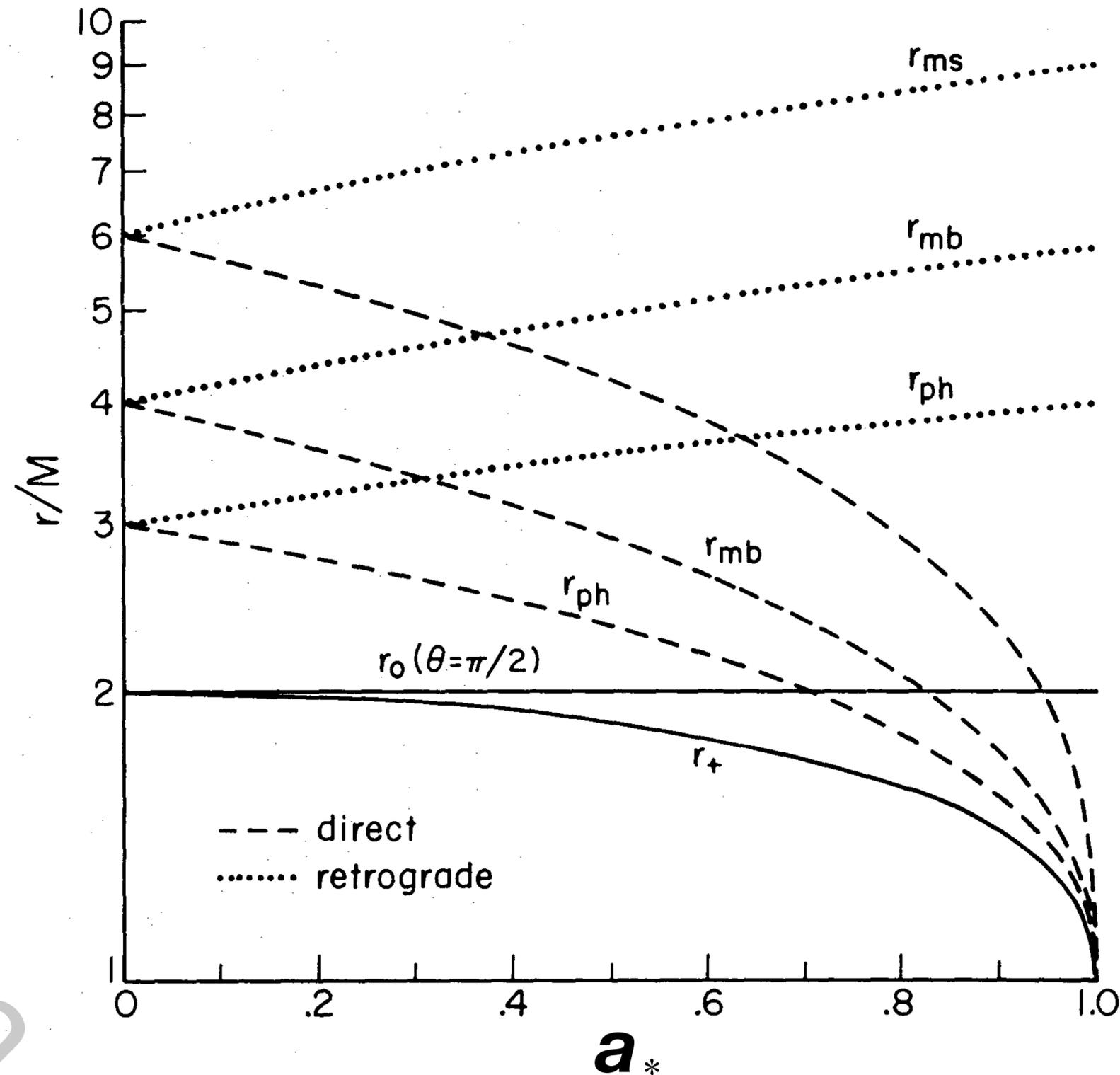
$$r_c = 3M \quad \text{for } a_* = 0$$

apparent radius $\sqrt{27}M$ seen from ∞

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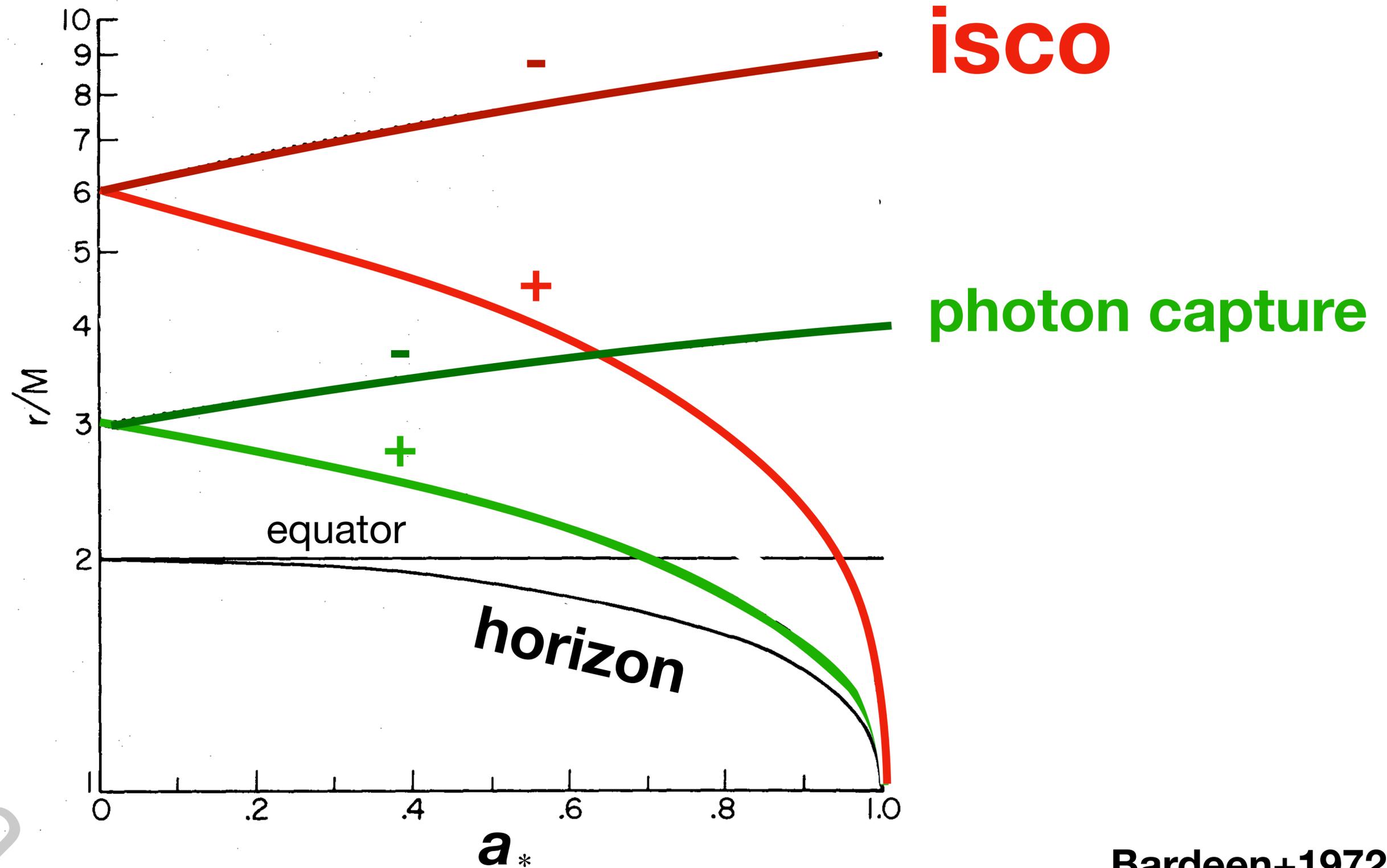


Dependence of radii on BH spin



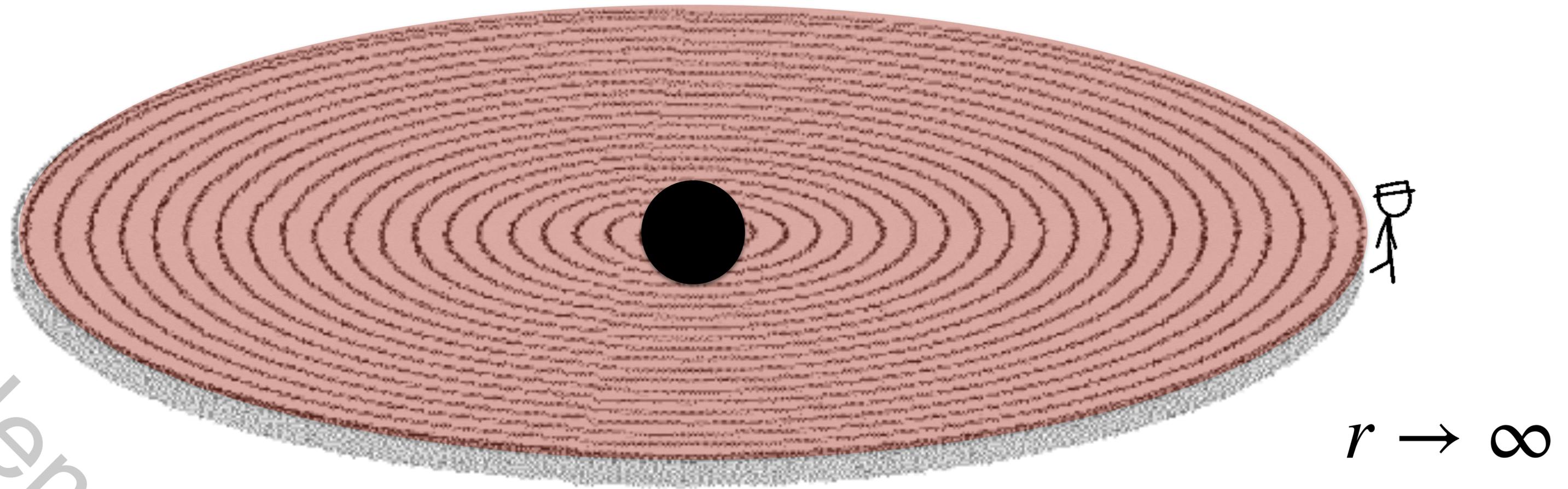
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Dependence of radii on BH spin



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Efficiency of release of free energy from BH accretion disks



How much orbital energy lost by particle when it disappears behind event horizon?

1st order estimate of L_{acc}

How much orbital energy lost by *one* particle?

$$E_{\text{acc}} = U(r \rightarrow \infty) - U(r_{\text{surface}}) \text{ gravitational potential energy} = \frac{GMm}{r_{\text{surface}}}$$

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Energy lost by *continuous inflow* of particles?

$$\dot{m} = \frac{dm}{dt} \quad \frac{dE_{\text{acc}}}{dt} = \frac{GM\dot{m}}{r_{\text{surface}}} \Rightarrow L = \frac{GM\dot{m}}{r_{\text{surface}}}$$

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Luminosity released from accretion

$$L = \eta \dot{m} c^2$$

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Luminosity released from accretion

$$L = \eta \dot{m} c^2 \Rightarrow \eta = \frac{L}{\dot{m} c^2} = \frac{GM}{r_{\text{surface}} c^2}$$

**maximized
for compact
objects**

For a Schwarzschild BH

$$\eta = 0.5$$

incorrect
Newtonian
value

Correct GR result

$$\eta = V_{\text{eff}}(\infty) - V_{\text{eff}}(6M)$$

$$= -V_{\text{eff}}(6M) = \frac{1}{18} = \boxed{0.06}$$

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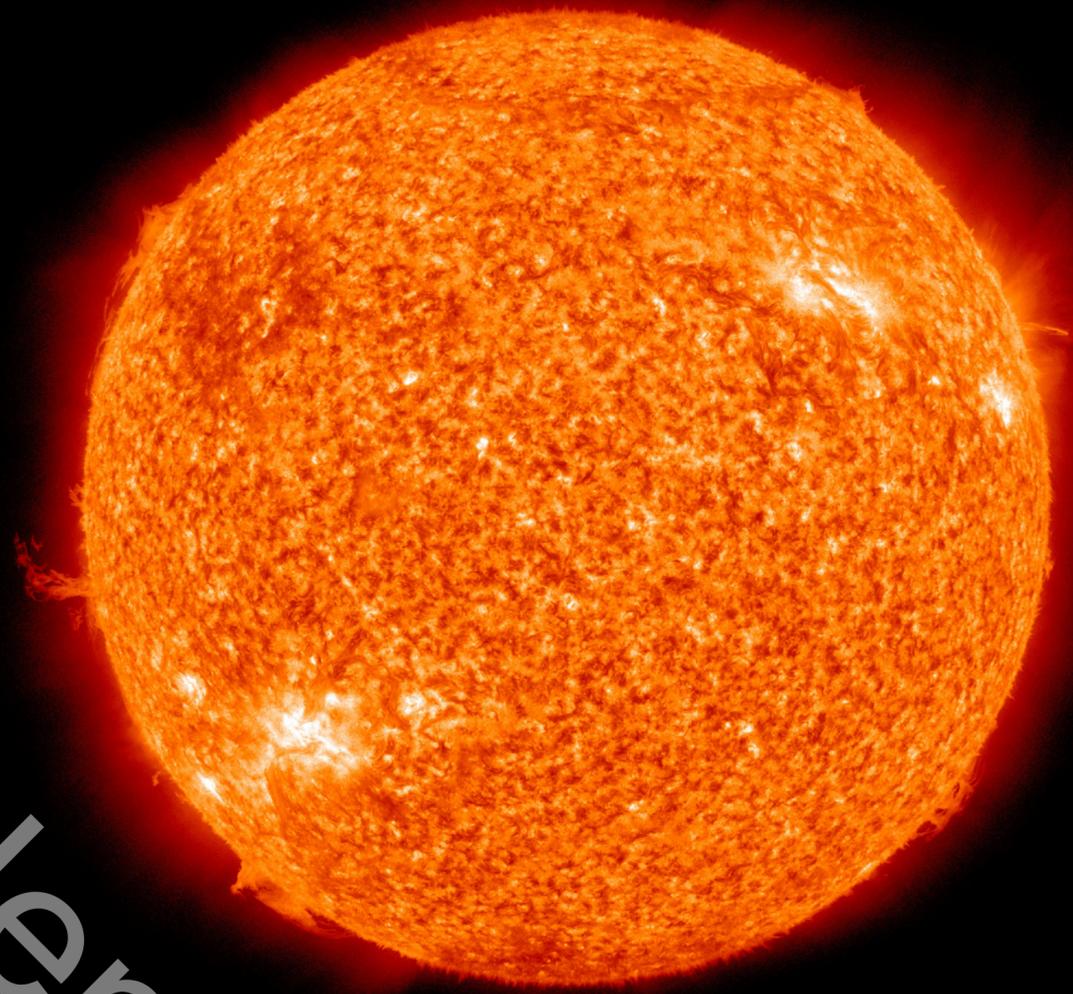
Itaipu Dam – 14 GW



$$\eta = \frac{mgh}{mc^2} = 10^{-14} \left(\frac{h}{100 \text{ m}} \right)$$

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Nuclear fusion



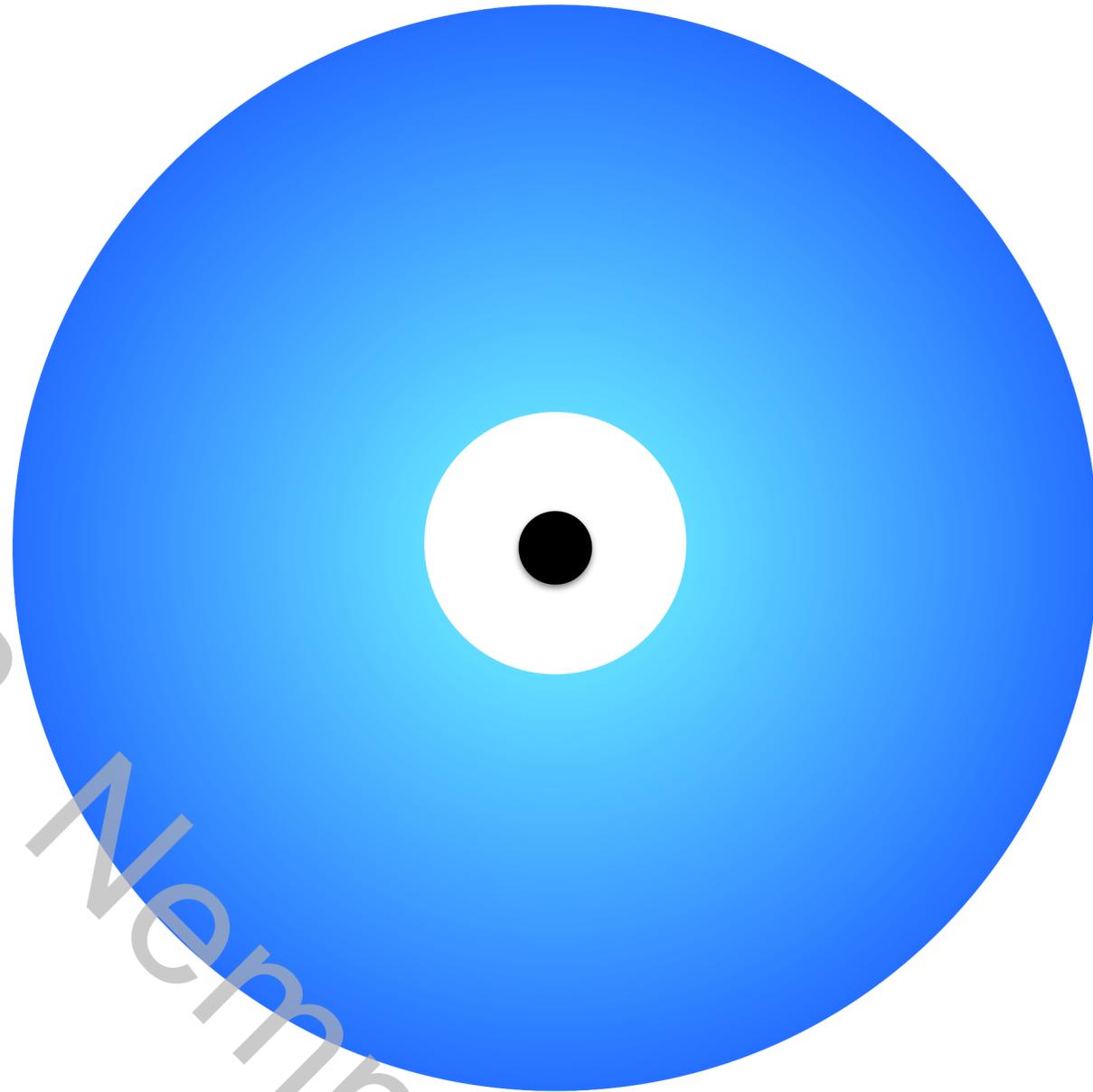
Tsar bomba

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$$\eta = 0.008 \times 0.1 \sim 8 \times 10^{-4}$$

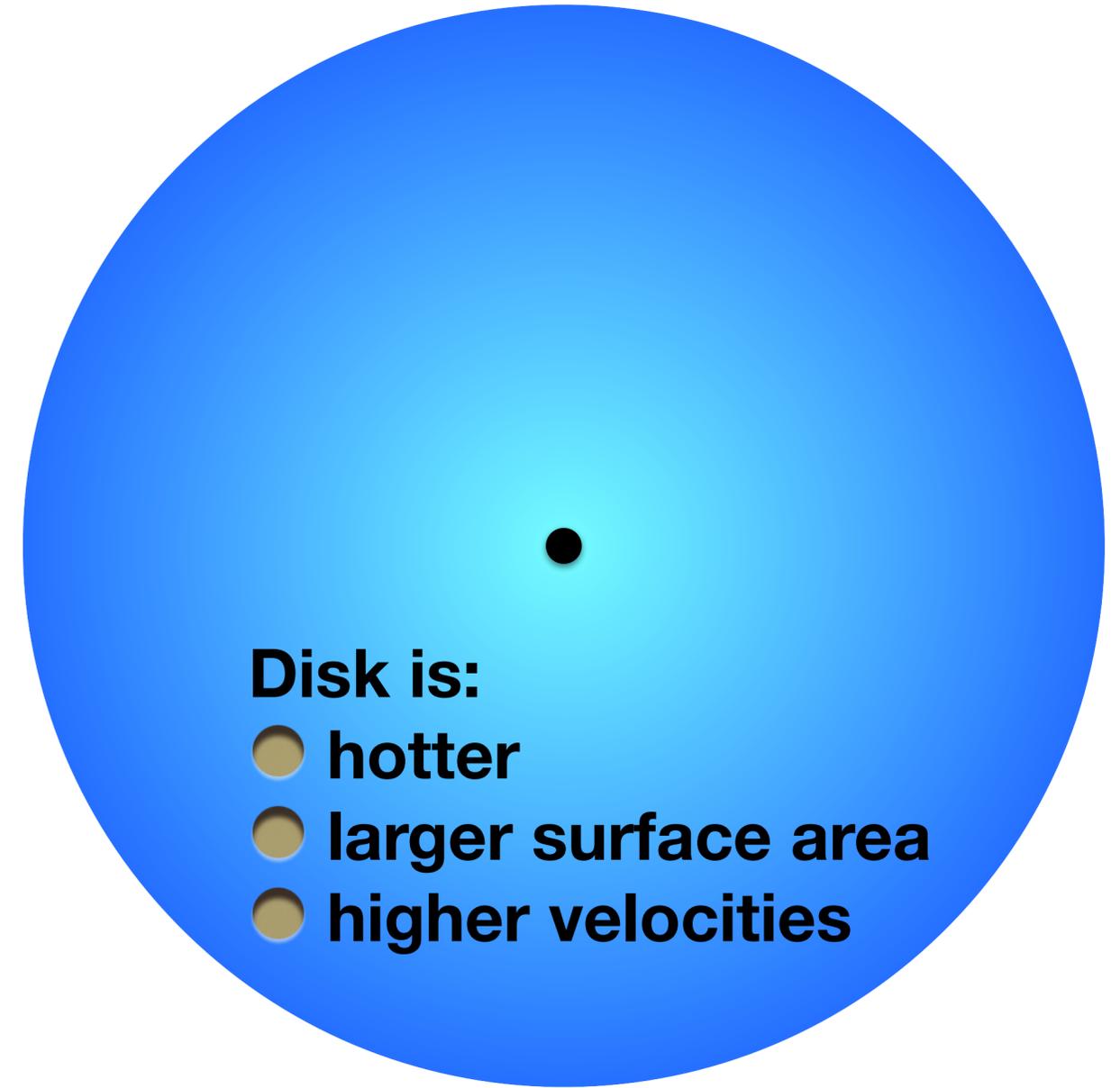
ISCO radius depends on the BH spin

face-on view of accretion disk



edge-on view

$$a_* = 0$$



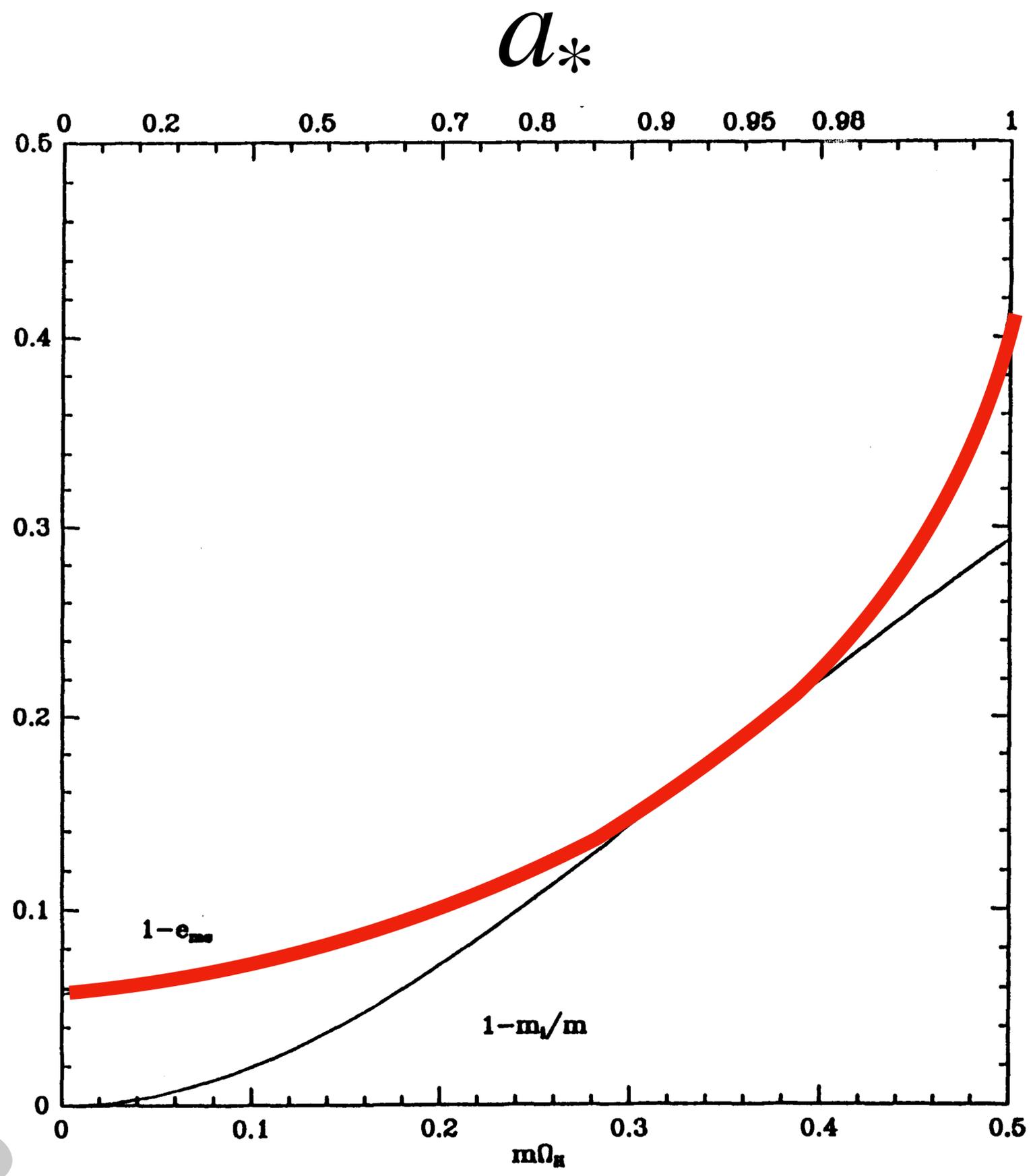
Disk is:

- hotter
- larger surface area
- higher velocities

$$a_* = 0.998$$

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η



$\eta=0.42$
at
 $a_*=0.998$

Black hole spin leaves imprint on accretion disk

Faster, hotter, brighter

but gravitational redshift

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BLACK HOLE PHYSICS SUMMARY

Black holes

- ◆ Mass-energy falls in, but nothing gets out
- ◆ Only three numbers: **mass M , spin a_* and charge**
- ◆ For astrophysics: **accretion rate \dot{M}** also important
- ◆ Mass range: $3.6M_{\odot} < M \lesssim 10^{11}M_{\odot}$

Black hole accretion

- ◆ Accretion converts gravitational potential energy into other forms (e.g. light)
- ◆ BHs maximize energy release efficiency: η up to 40% (for max spin)

Main scales

- ◆ Luminosity: $L_{\text{Edd}} = 1.3 \times 10^{38} (M/M_{\odot}) \text{ erg s}^{-1}$
- ◆ Mass accretion rate: $\dot{M}_{\text{Edd}} \equiv L_{\text{Edd}}/(0.1c^2)$

Main lengths

- ◆ ISCO: Innermost stable circular orbit, $r = 6M$
- ◆ Photon capture: $r = 3M$ ($\sqrt{27}M$) seen from far away
- ◆ Sphere of influence: $r \sim 10^6M$

- ◆ Growth timescale: $t_{\text{Edd}} \equiv 4 \times 10^7 (\eta/0.1) \text{ yr}$