

Looking for interactions in the dark sector: An update

Saulo Carneiro

PPGCosmo - Vitória - 2020

A perfect fluid

$$T^{\mu\nu} = (\rho + p)u^\mu u^\nu - pg^{\mu\nu}$$

can always be decomposed as

$$T^{\mu\nu} = \rho_m u^\mu u^\nu + \Lambda g^{\mu\nu}$$

with

$$T^{\mu\nu}_{m;\nu} = Q^\mu,$$

$$T^{\mu\nu}_{\Lambda;\nu} = -Q^\mu$$

where

$$Q^\mu = Qu^\mu + \bar{Q}^\mu,$$

$$\bar{Q}^\mu u_\mu = 0$$

Background

$$Q = -\Lambda_{,\nu} u^\nu,$$
$$\bar{Q}^\mu = \Lambda_{,\nu} (u^\mu u^\nu - g^{\mu\nu})$$

Perturbations

$$\delta Q = \delta \bar{Q}^0 = 0,$$
$$\delta \bar{Q}_i = (\delta \Lambda + \dot{\Lambda} \theta)_{,i} \equiv \delta \Lambda^c_{,i}$$

If dark matter is cold, dark energy is homogeneous, and vice-versa.

Friedmann equations

$$3H^2 = \rho_m + \Lambda,$$

$$\dot{\rho}_m + 3H\rho_m = \Gamma\rho_m = -\dot{\Lambda}$$

Parametrising the interaction

$$\Lambda = \sigma H^{-2\alpha},$$

$$\Gamma = -\alpha\sigma H^{-(2\alpha+1)}$$

Non-adiabatic Chaplygin gas

$$H^2(z) = H_0^2 \left[1 - \Omega_{m0} + \Omega_{m0}(z+1)^{3(1+\alpha)} \right]^{\frac{1}{1+\alpha}}$$

Matter power spectrum

$$P(k) = P_0 k^{n_s} T^2(k/k_{eq}),$$

Matter-radiation equality

$$\rho_m(z) = 3H_0^2 \Omega_{m0}^{\frac{1}{1+\alpha}} z^3 \quad (z \gg 1)$$

$$k_{eq} = \frac{H(z_{eq})}{z_{eq}} = 0.073 \text{ Mpc}^{-1} h^2 \Omega_{m0}^{\frac{1}{1+\alpha}}$$

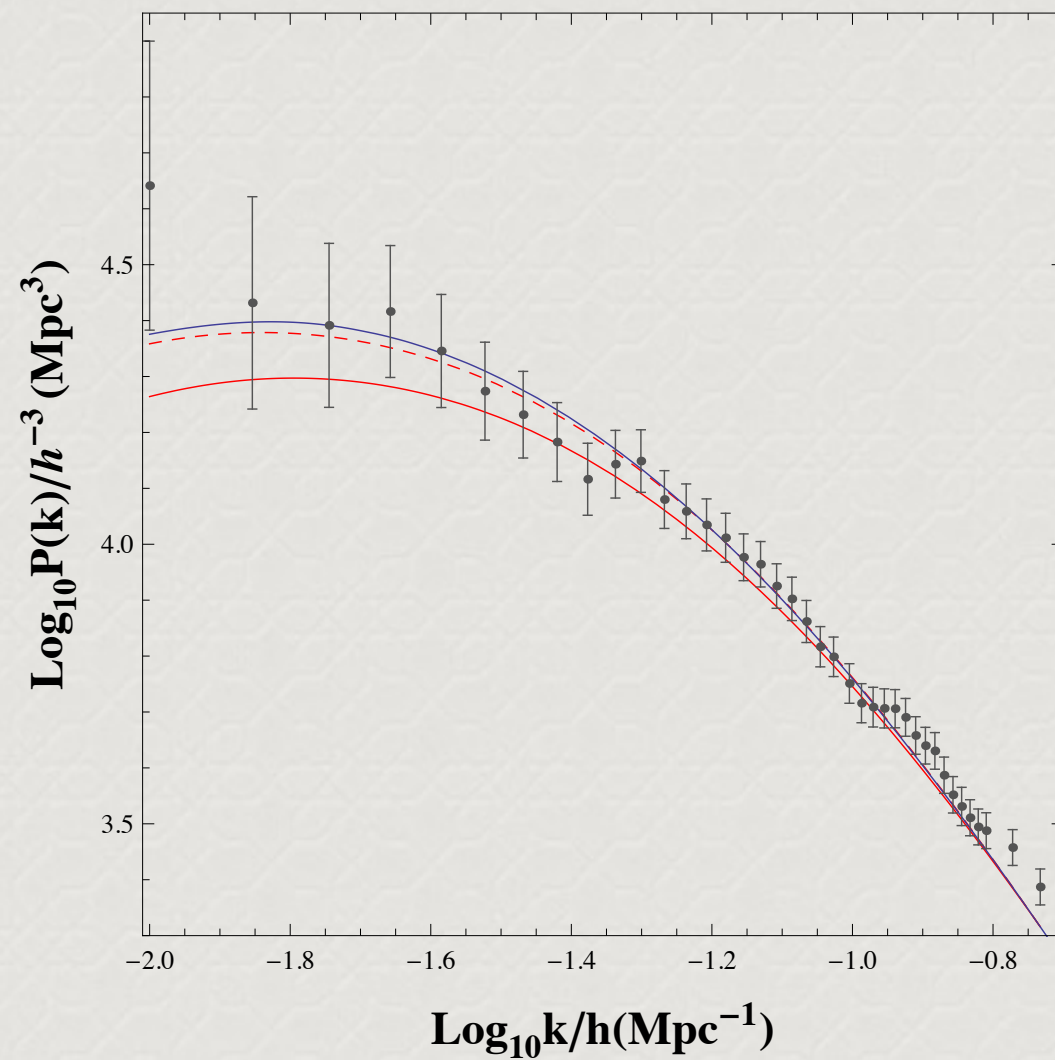


FIG. 1: The linear power spectrum for $\alpha = -1/2$ and $\Omega_{m0} = 0.45$ [18]. The blue line was obtained by a direct integration of the perturbation equations [25]. The dashed red line corresponds to the use of (14) and (18). The solid red line corresponds to the concordance Λ CDM model. Data come from the 2dFGRS catalogue [7].

Redshift space distortions

$$f_b(z) = \frac{\delta'_b(z)}{H a \delta_b(z)},$$

$$f_{rsd}(z) \sigma_8(z) = f_b(z) \sigma_8 D_{b+}^N(z)$$

Perturbation equations

$$a^2 H^2 \delta''_m + aH (aH' + 3H + \Gamma) \delta'_m + 2\Gamma H \delta_m = \frac{\rho_m \delta_m}{2}$$

$$a^2 H^2 \delta''_b + aH (aH' + 3H) \delta'_b = \frac{\rho_m \delta_m}{2}$$

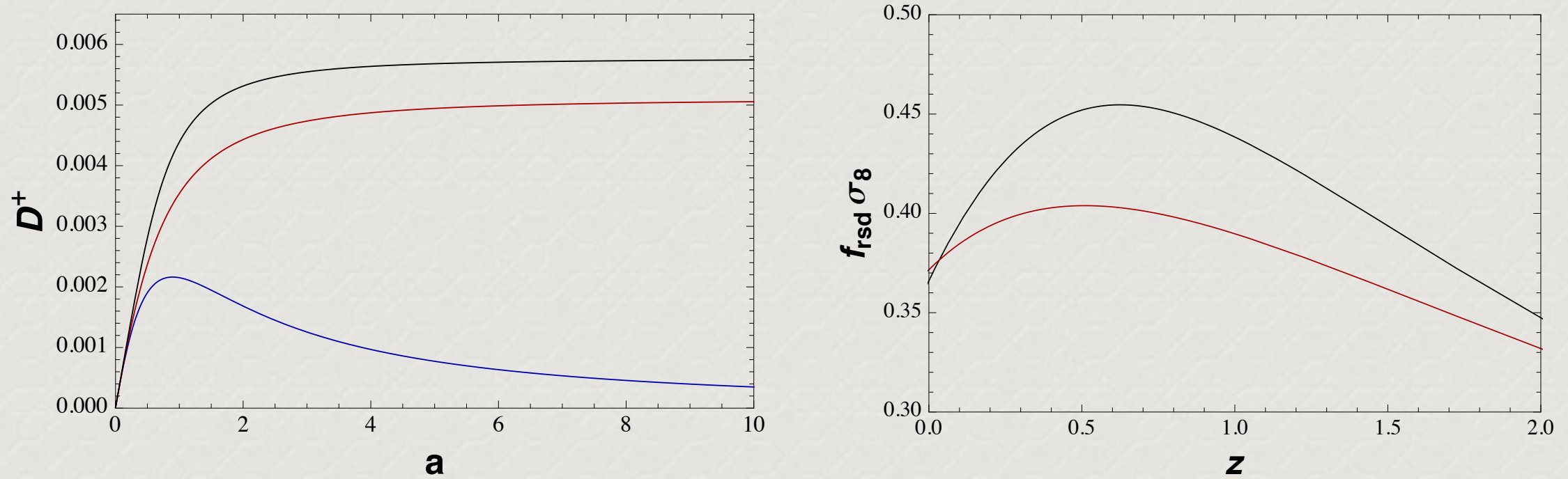


FIG. 2: **Left panel:** Evolution of the matter contrast in the Λ CDM model (black curve), and of the total matter (blue) and baryonic (red) contrasts for $\alpha = -1/2$ [27]. **Right panel:** Evolution of the baryonic $f_{\text{rsd}}\sigma_8$ for Λ CDM (black) and for $\alpha = -1/2$ (red).

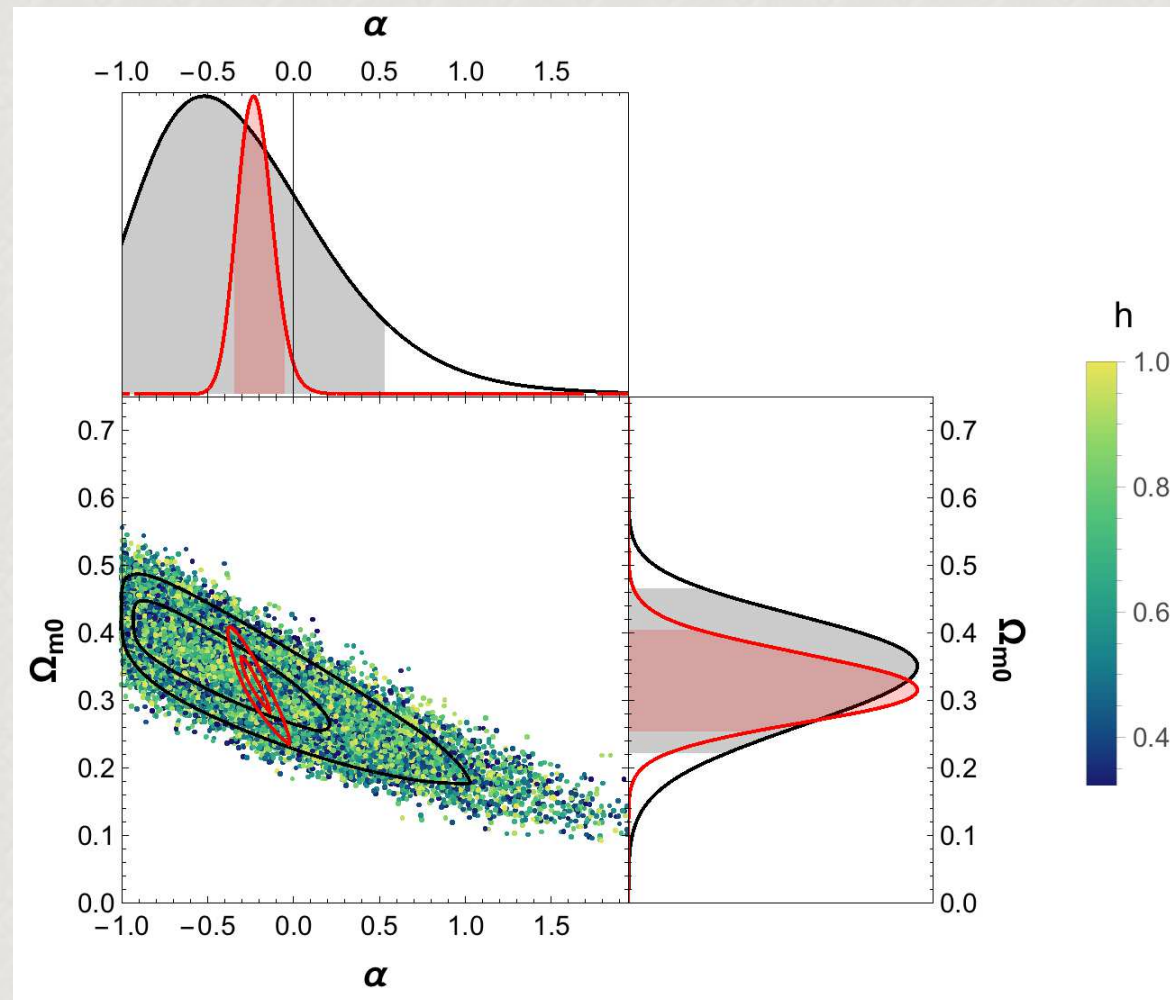


FIG. 3: Likelyhoods for the interaction parameter and the matter density parameter from the joint analysis of SNe Ia (JLA) + LSS (2dFGRS) + l_1 (red) [20]. The black lines are PDFs for just JLA supernovae. The confidence regions in the $\alpha \times \Omega_{m0}$ plane are also shown.

CMB - full

Background

$$\rho_m = 3H_0^2 \left[\Omega_{m0}^2 (z+1)^3 + \Omega_{m0} (1 - \Omega_{m0}) (z+1)^{3/2} \right]$$

$$\rho_b = 3H_0^2 \Omega_{b0} (z+1)^3 \qquad \rho_{dm} = \rho_m - \rho_b \qquad \rho_R = 3H_0^2 \Omega_{R0} (z+1)^4$$

$$H(z) = H_0 \left\{ \left[1 - \Omega_{m0} + \Omega_{m0} (z+1)^{3/2} \right]^2 + \Omega_{R0} (z+1)^4 \right\}^{1/2}$$

Perturbations

$$\theta'_{dm} = -aH\theta_{dm} + k^2\phi,$$

$$\delta'_{dm} = -\theta_{dm} + 3\phi' + \Gamma a \left(\frac{\rho_m}{\rho_{dm}} \right) (\phi - \delta_{dm})$$

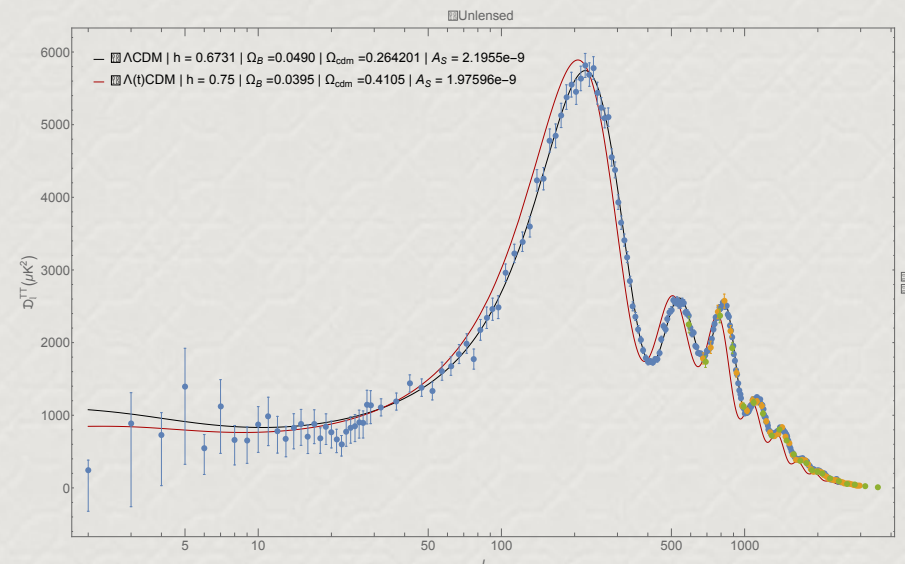
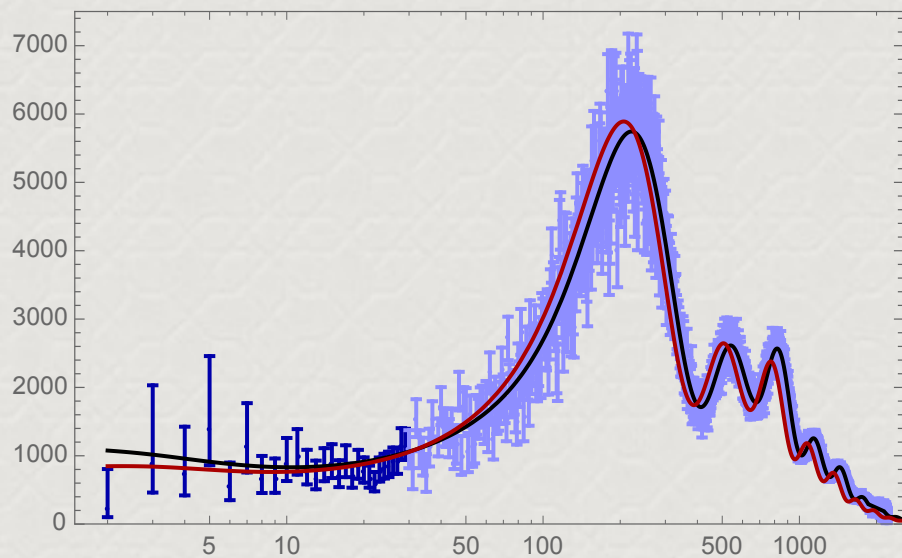


FIG. 4: The CMB anisotropy spectra for the Λ CDM model ($\alpha = 0$, black) and for the model with constant matter-creation rate ($\alpha = -1/2$, red), superposed to the unbinned (left) and binned (right) Planck data. For the standard model we have adopted $\Omega_m = 0.31$ and $h = 0.67$, while for the interacting model we have used $\Omega_m = 0.45$ and $h = 0.75$.

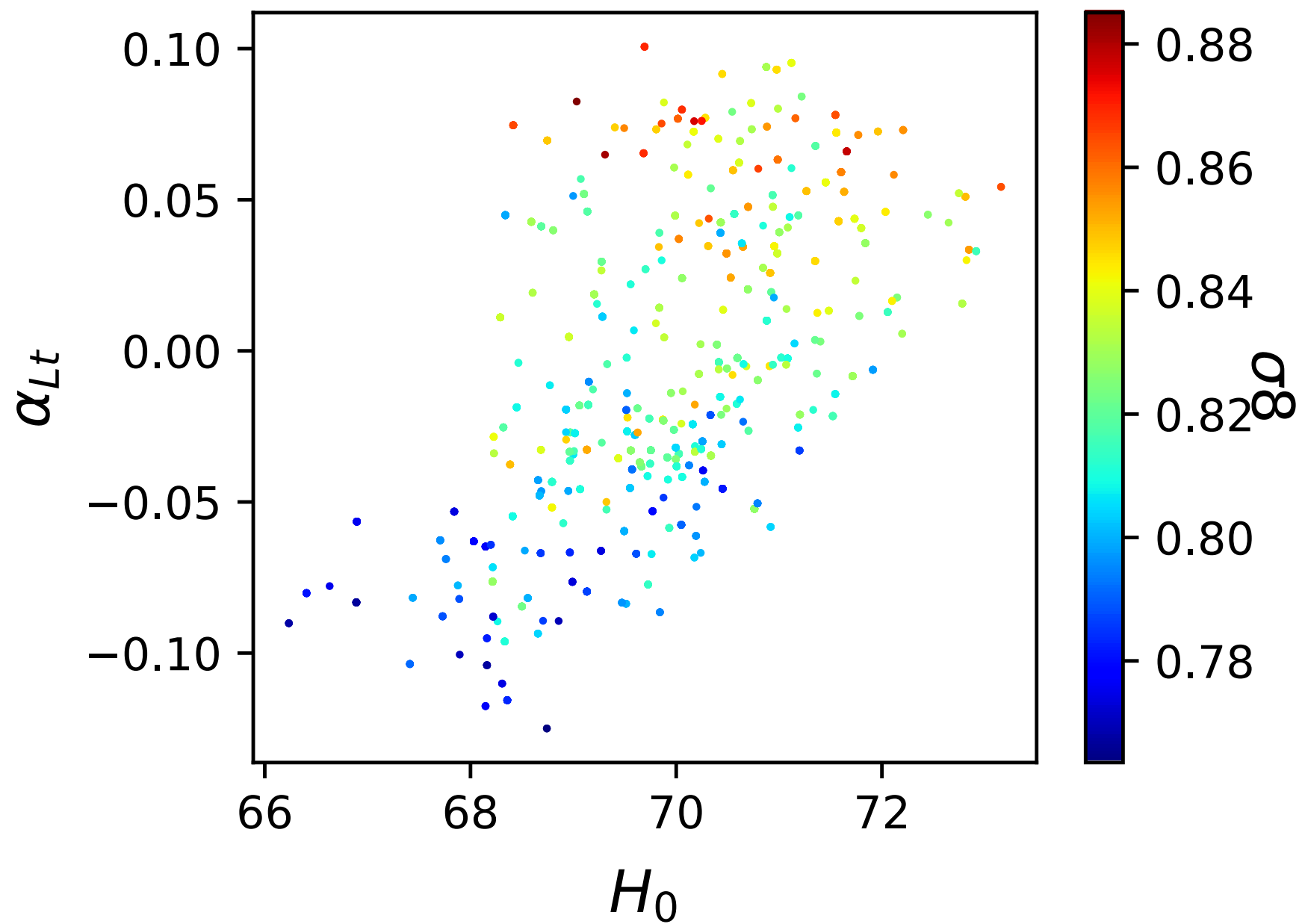
Perturbations (general case)

$$\begin{aligned}\theta'_{dm} + \mathcal{H}\theta_{dm} - k^2\Phi &= 0, \\ \delta'_{dm} - 3\Phi' + \theta_{dm} &= -\frac{aQ}{\rho_{dm}} \left[\delta_{dm} - \frac{1}{k^2} \left(k^2\Phi + \frac{Q'}{Q}\theta_{dm} \right) \right], \\ -k^2\Phi &= \frac{a^2}{2}(\rho_{dm}\delta_{dm} + \rho_b\delta_b) - \left(\frac{a^3Q}{2} - \frac{3a^2}{2}\mathcal{H}\rho_m \right) \frac{\theta_{dm}}{k^2},\end{aligned}$$

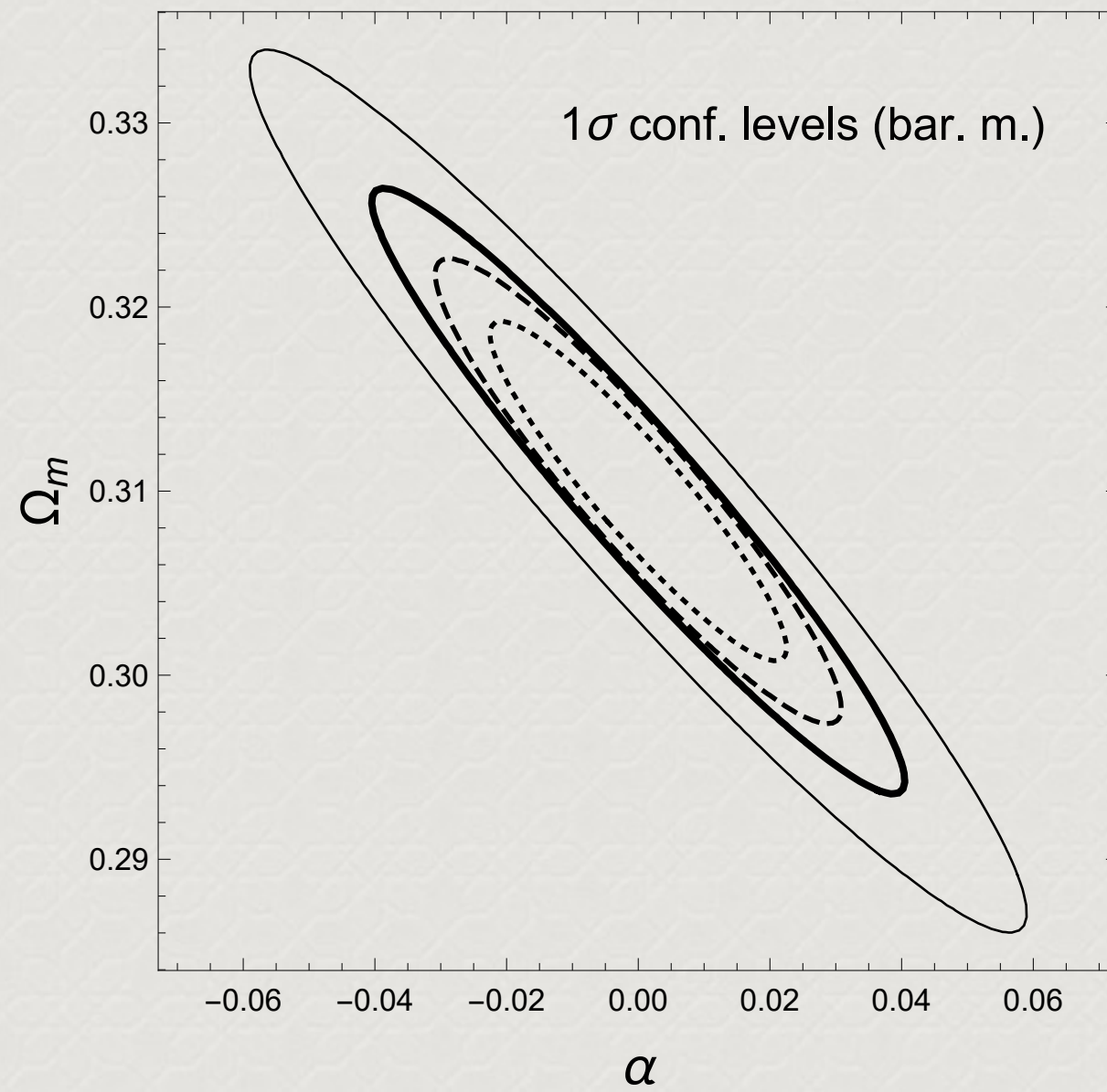
$$\delta\Lambda = -aQ\theta_m/k^2 \text{ and } \delta Q = Q'\theta_m/k^2,$$

Sub-horizon limit

$$\begin{aligned}\theta'_{dm} + \mathcal{H}\theta_{dm} - k^2\Phi &= 0, \\ \delta'_{dm} + \theta_{dm} &= -\frac{aQ}{\rho_{dm}}\delta_{dm}, \\ -k^2\Phi &= \frac{a^2}{2}(\rho_{dm}\delta_{dm} + \rho_b\delta_b).\end{aligned}$$



Forecasts



Salzano et al. [J-PAS collaboration], to appear.

Thanks

