

Horizontes para ondas superficiais em fluidos

Alberto Saa

Buracos negros acústicos

- Introdução/Motivação
- Fundamentos hidrodinâmicos
- Horizontes para ondas superficiais

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Dimensionless quantity

From Wikipedia, the free encyclopedia
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In [dimensional analysis](#), a **dimensionless quantity** is a [quantity](#)

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In [dimensional analysis](#), a **dimensionless quantity** is a [quantity](#)

List of dimensionless quantities [\[edit\]](#)

All numbers are dimensionless [quantities](#). Certain dimensionless quantities of some importance are given below:

Name ↕	Standard symbol ↕	Definition	Field of application ↕
Abbe number	<i>V</i>	$V = \frac{n_d - 1}{n_F - n_C}$	optics (dispersion in optical materials)
Activity coefficient	γ	$\gamma = \frac{a}{x}$	chemistry (Proportion of "active" molecules or atoms)
Albedo	α	$\alpha = (1 - D)\bar{\alpha}(\theta_i) + D\bar{\bar{\alpha}}$	climatology , astronomy (reflectivity of surfaces or bodies)
Archimedes number	<i>Ar</i>	$Ar = \frac{gL^3\rho_\ell(\rho - \rho_\ell)}{\mu^2}$	fluid mechanics (motion of fluids due to density differences)
Arrhenius number	α	$\alpha = \frac{E_a}{RT}$	chemistry (ratio of activation energy to thermal energy) ^[5]
Atomic weight	<i>M</i>		chemistry (mass of atom over one atomic mass unit, u, where carbon-12 is exactly 12 u)

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Dimensionless quantity

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Bond number	Bo	$\text{Bo} = \frac{\rho a L^2}{\gamma}$	geology , fluid mechanics , porous media (buoyant versus capillary forces, similar to the Eötvös number) ^[10]
Eötvös number	Eo	$\text{Eo} = \frac{\Delta \rho \, g \, L^2}{\sigma}$	fluid mechanics (shape of bubbles or drops)

List of dimensionless quantities ^[edit]

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Phase velocity

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Phase velocity

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$$v_p = \frac{\omega}{k}.$$

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Phase velocity

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Group velocity

From Wikipedia, the free encyclopedia

$$v_g \equiv \frac{\partial \omega}{\partial k}$$

Ondas de superfície

Fluido incompressível

$$\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial z^2} = 0$$

Condições de contorno

$$\mathbf{v} \cdot \hat{\mathbf{k}} = \left. \frac{\partial \psi}{\partial z} \right|_{z=-h} = 0$$

$$\left. \frac{\partial \psi}{\partial z} \right|_{z=0} = \frac{\partial \xi}{\partial t}$$

$$g\zeta + \left. \left(\frac{\partial \psi}{\partial t} \right) \right|_{z=0} = 0$$

Ondas de superfície

$$\psi(x, z, t) = \varphi(z) \sin(kx - \omega t)$$

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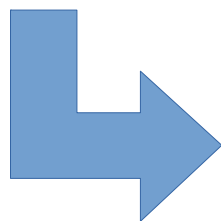
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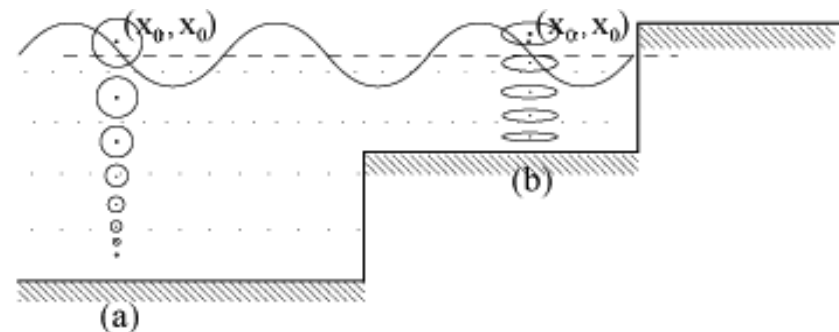


Figura 4 - Trajetórias das partículas em (a) águas profundas e (b) rasas.

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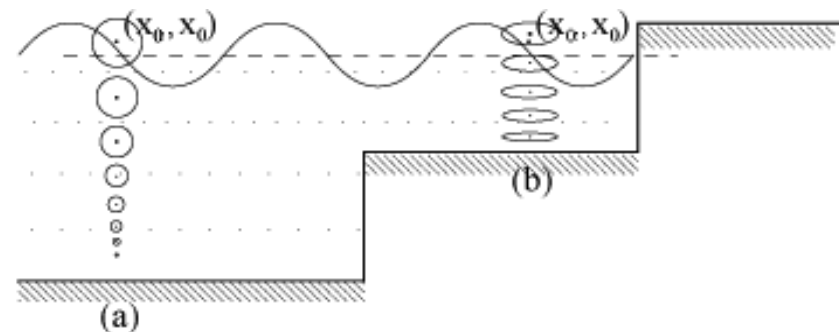


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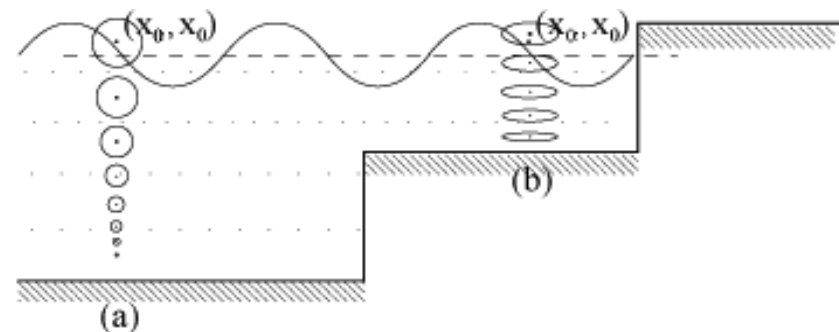


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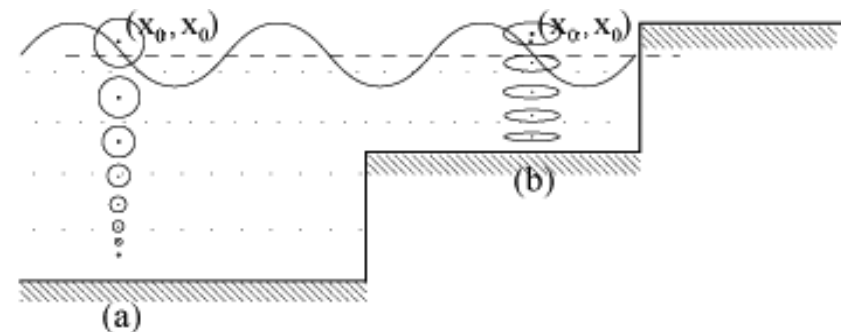


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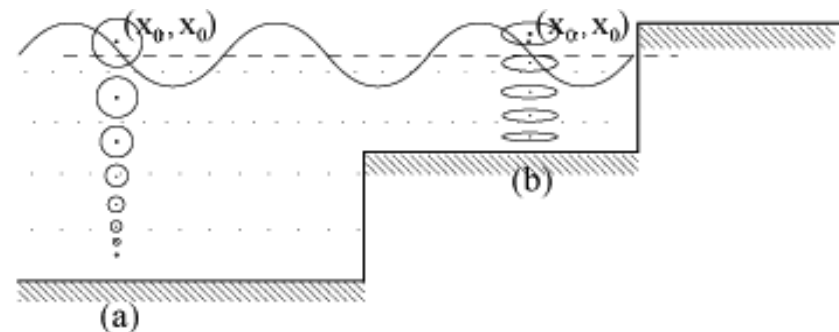


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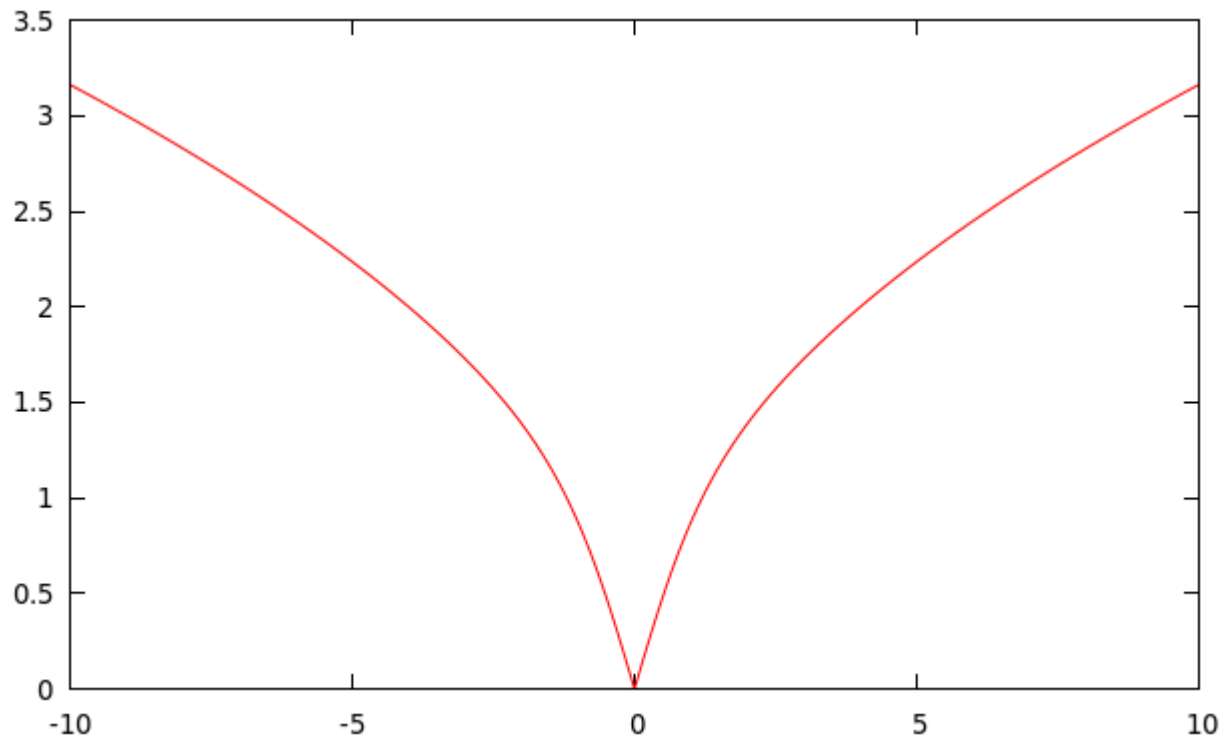
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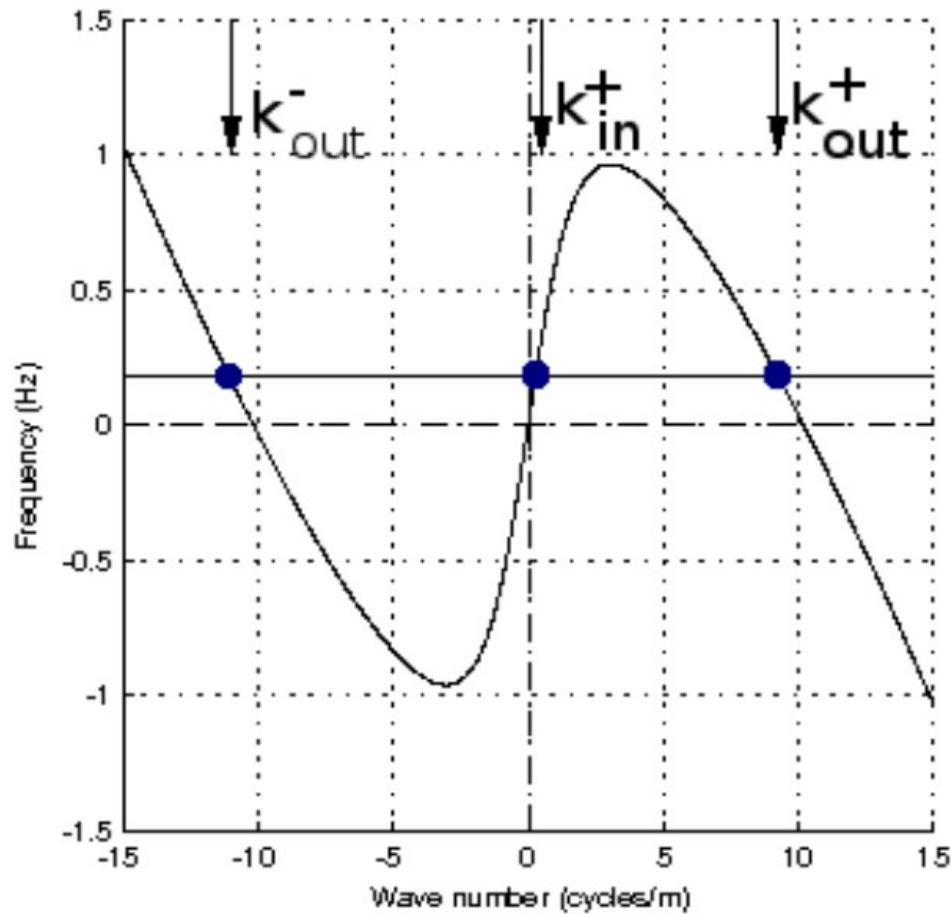
$$\omega(k) = \sqrt{kg \tanh(kh)} \quad \longrightarrow \quad (\omega(k) + kv)^2 = kg \tanh(kh)$$

Ondas de superfície



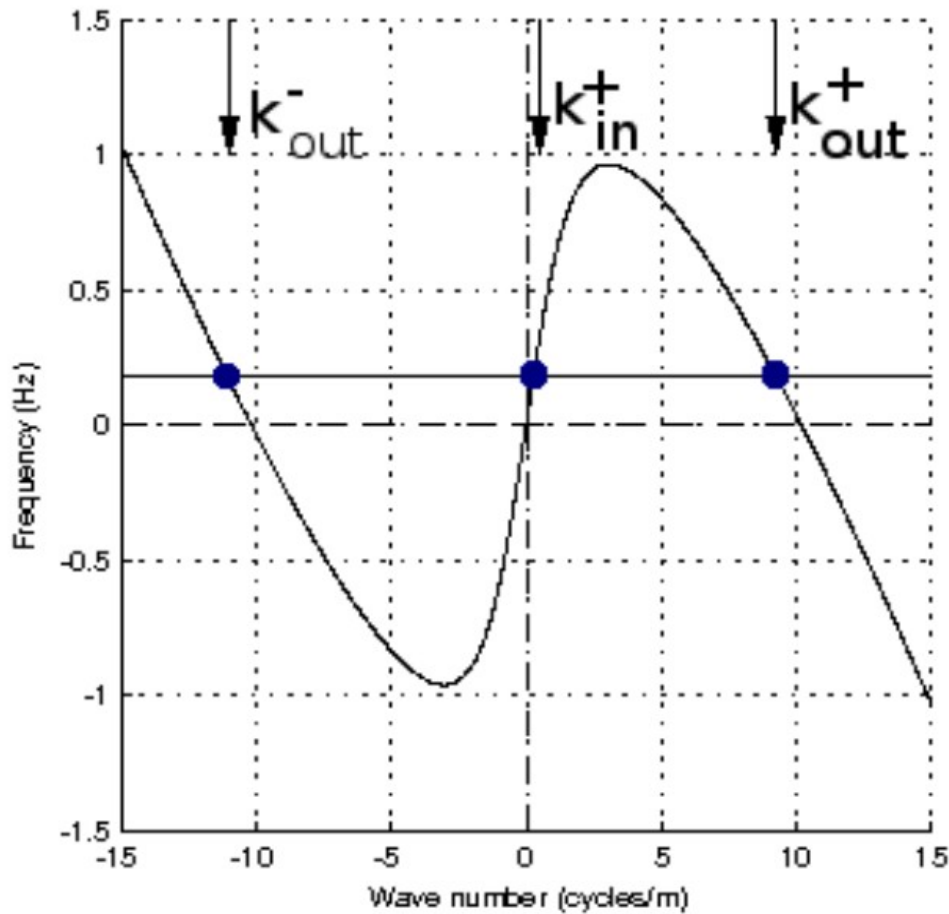
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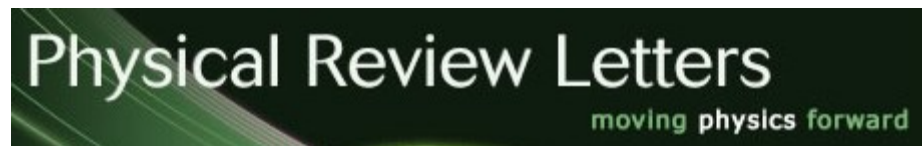


$$(\omega(k) + kv)^2 = kg \tanh(kh)$$

Ondas de superfície



$$(\omega(k) + kv)^2 = kg \tanh(kh)$$



Silke Weinfurter¹, Edmund W. Tedford², Matthew C. J. Penrice¹, William G. Unruh¹, and Gregory A. Lawrence²

¹Department of Physics and Astronomy, University of British Columbia, Vancouver, Canada V6T 1Z1

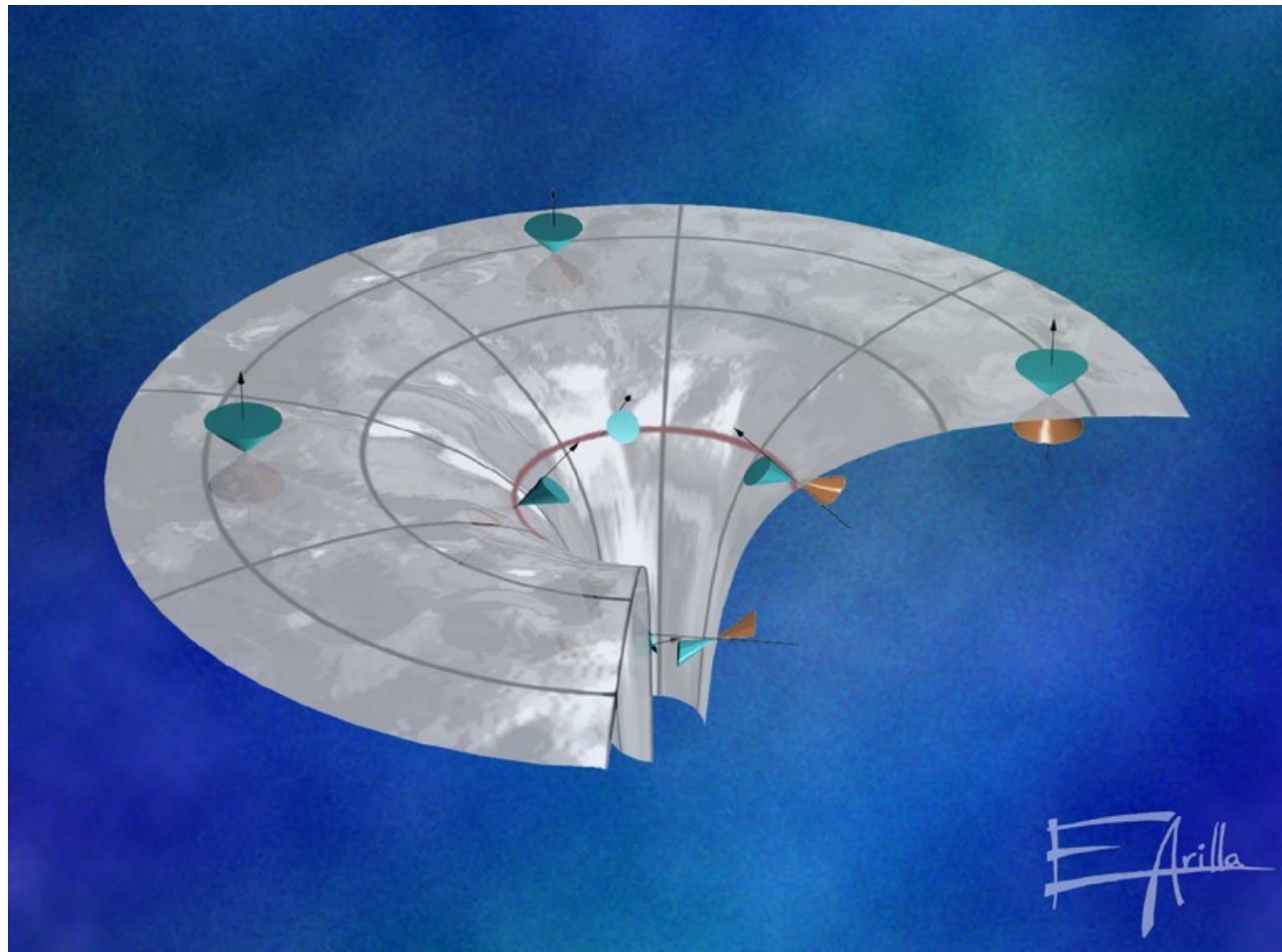
²Department of Civil Engineering, University of British Columbia, 6250 Applied Science Lane, Vancouver, Canada V6T 1Z4

Espalhamento por BN

$$ds^2 = - \left(1 - \frac{2M}{r} \right) dt^2 + \frac{dr^2}{1 - \frac{2M}{r}} + r^2 d\Omega^2$$

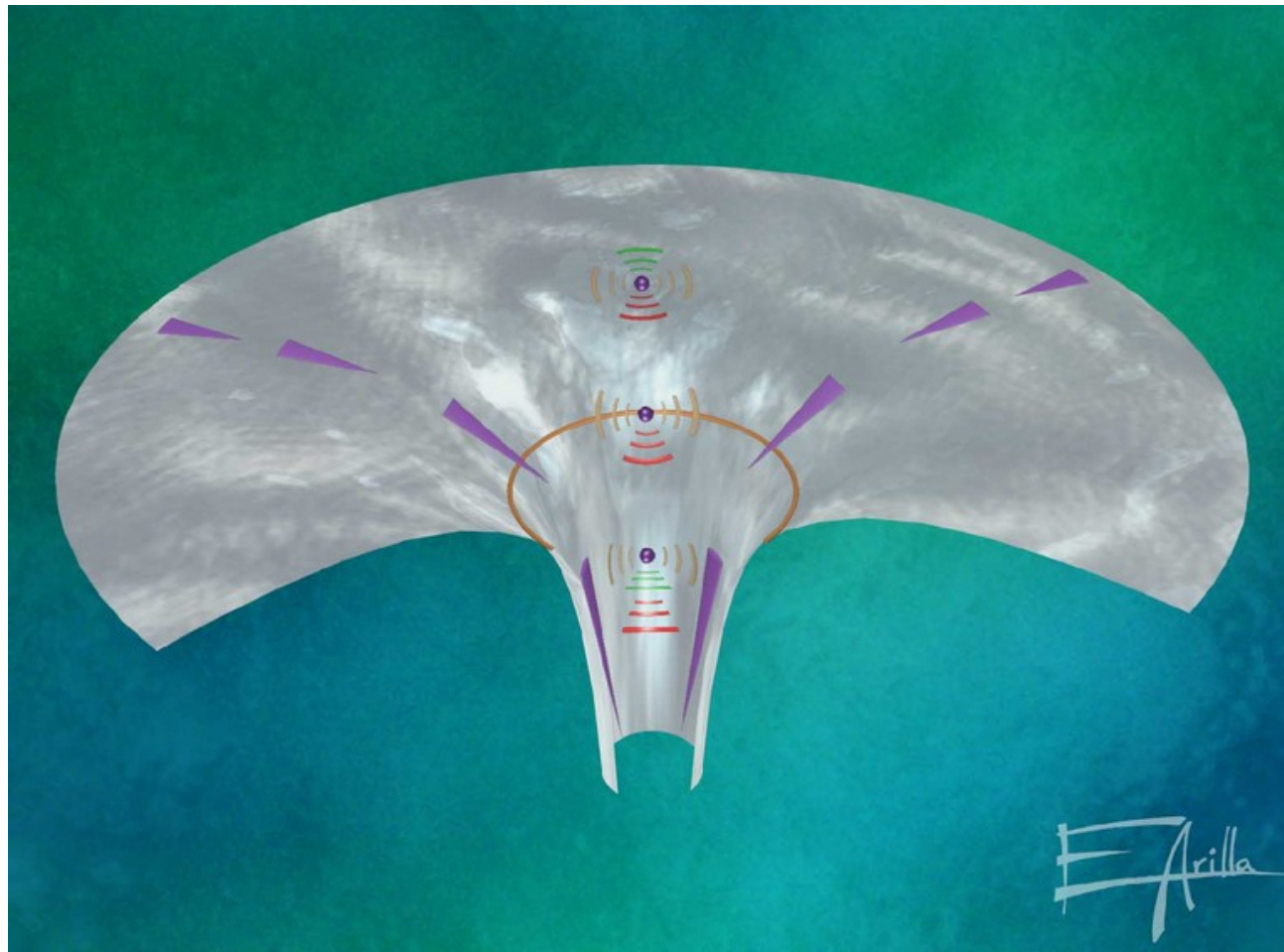
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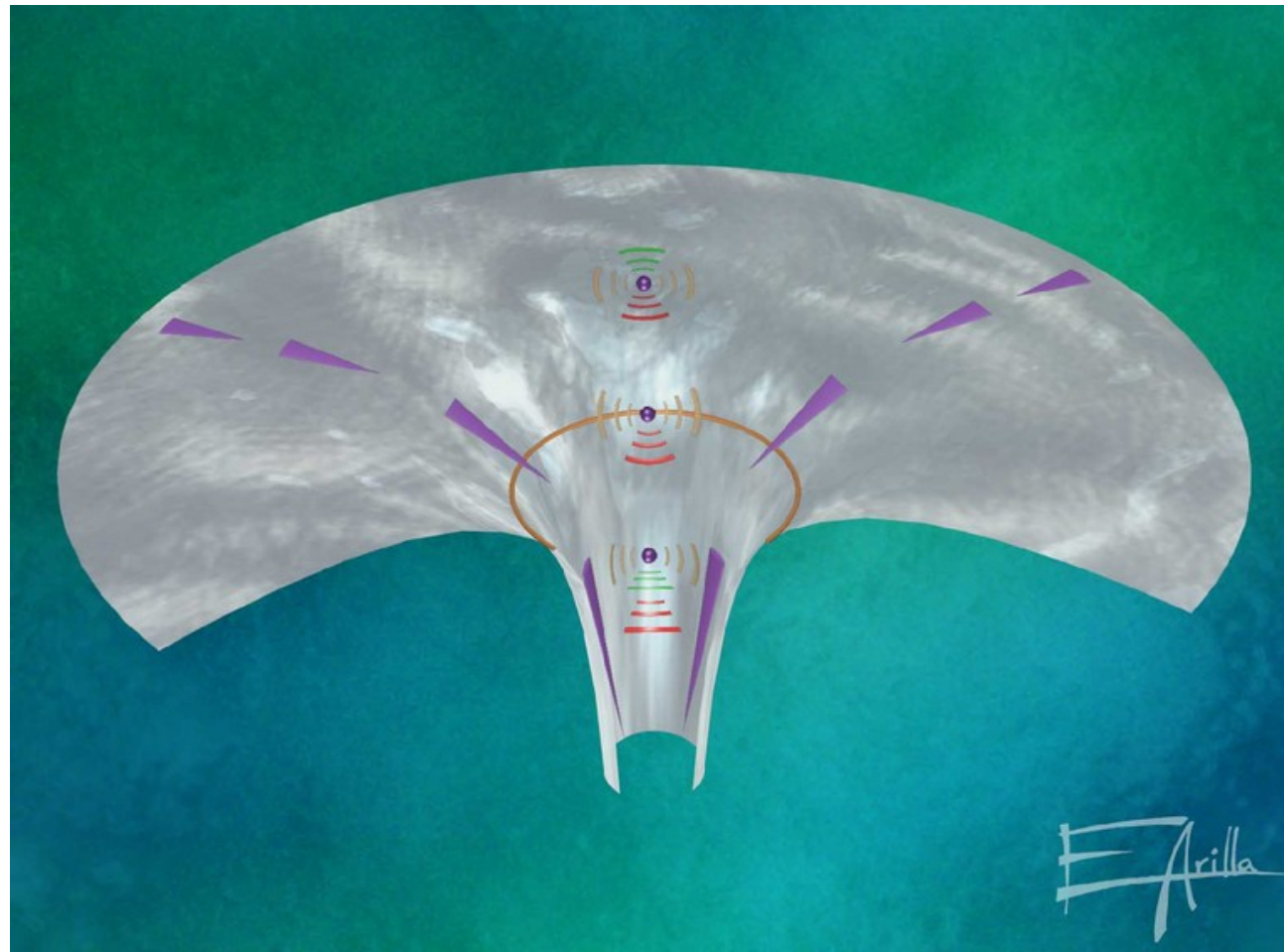
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Arilla

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in relativity

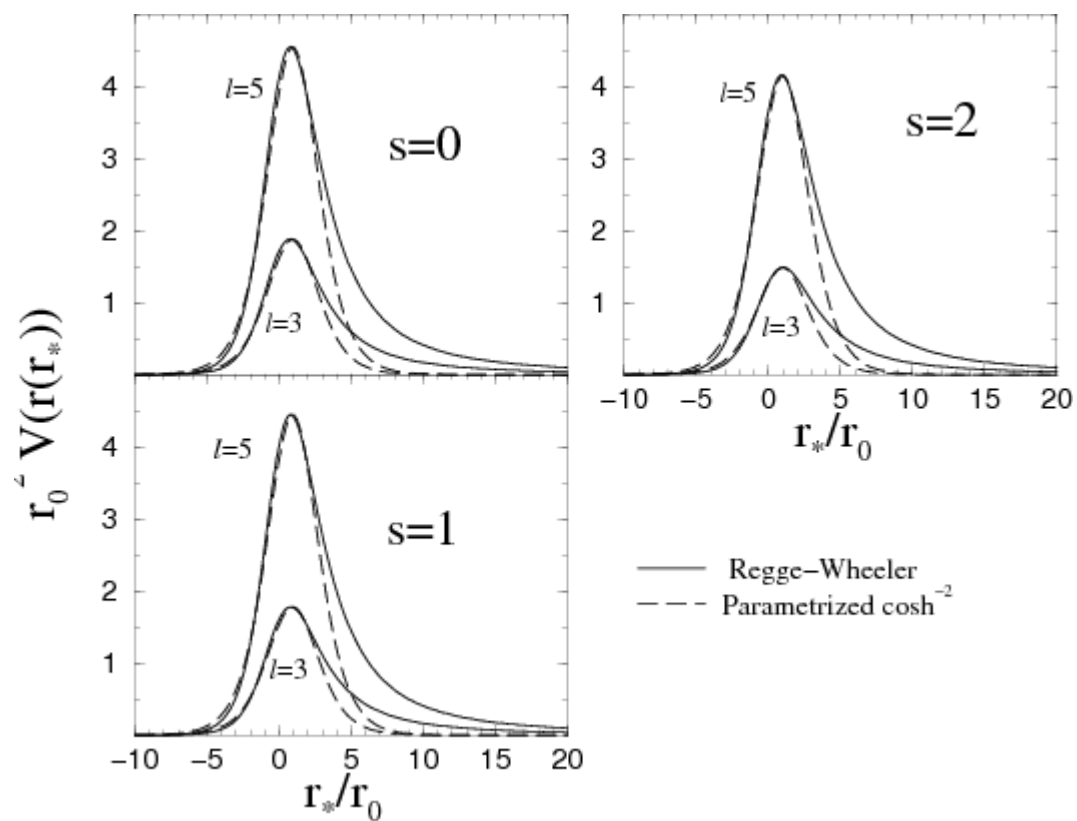
Vol. 14 (2011) > Irr-2011-3

Living Rev. Relativity 14 (2011), 3

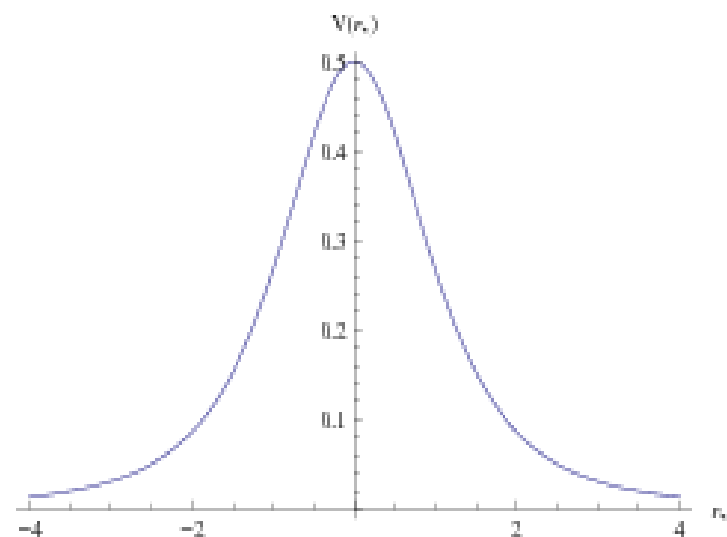
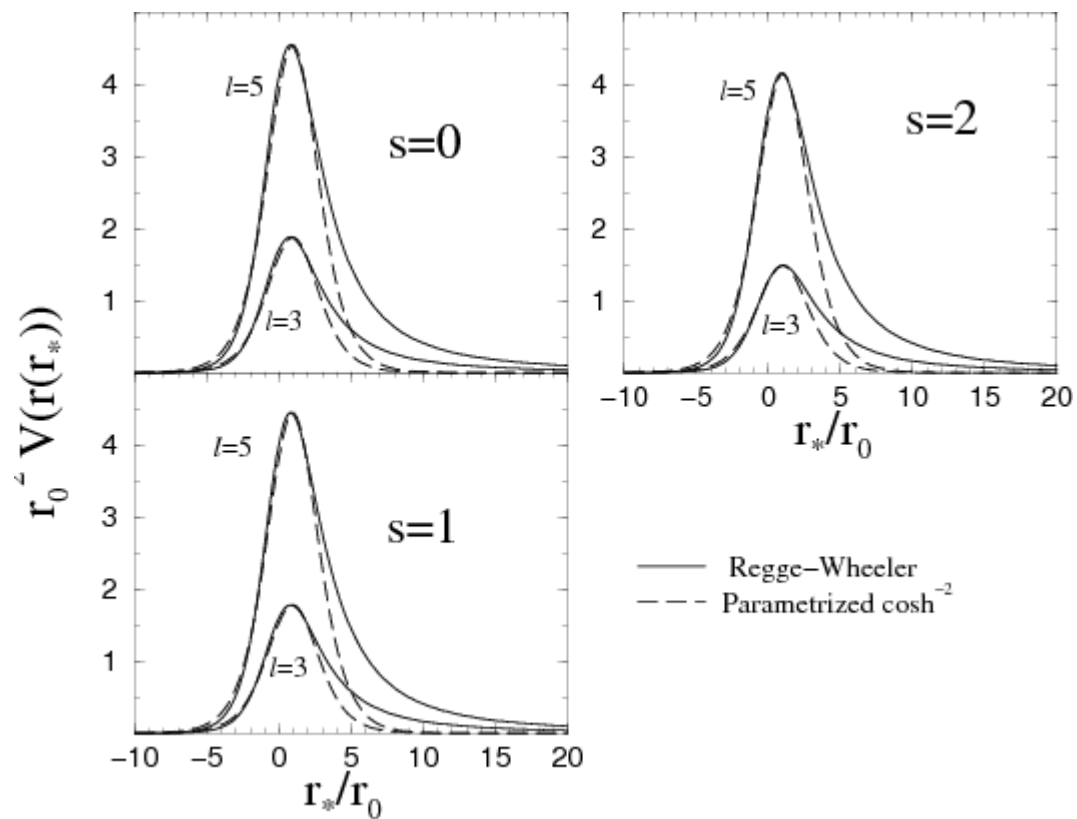
Analogue Gravity

Carlos Barceló and Stefano Liberati and Matt Visser

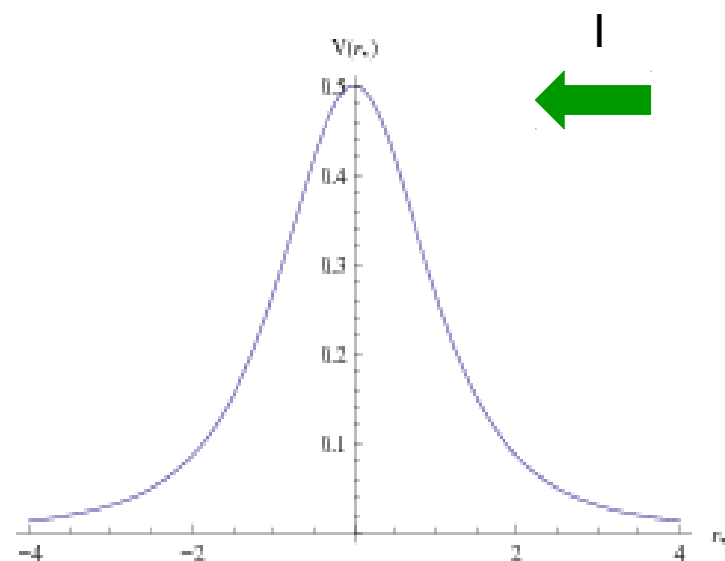
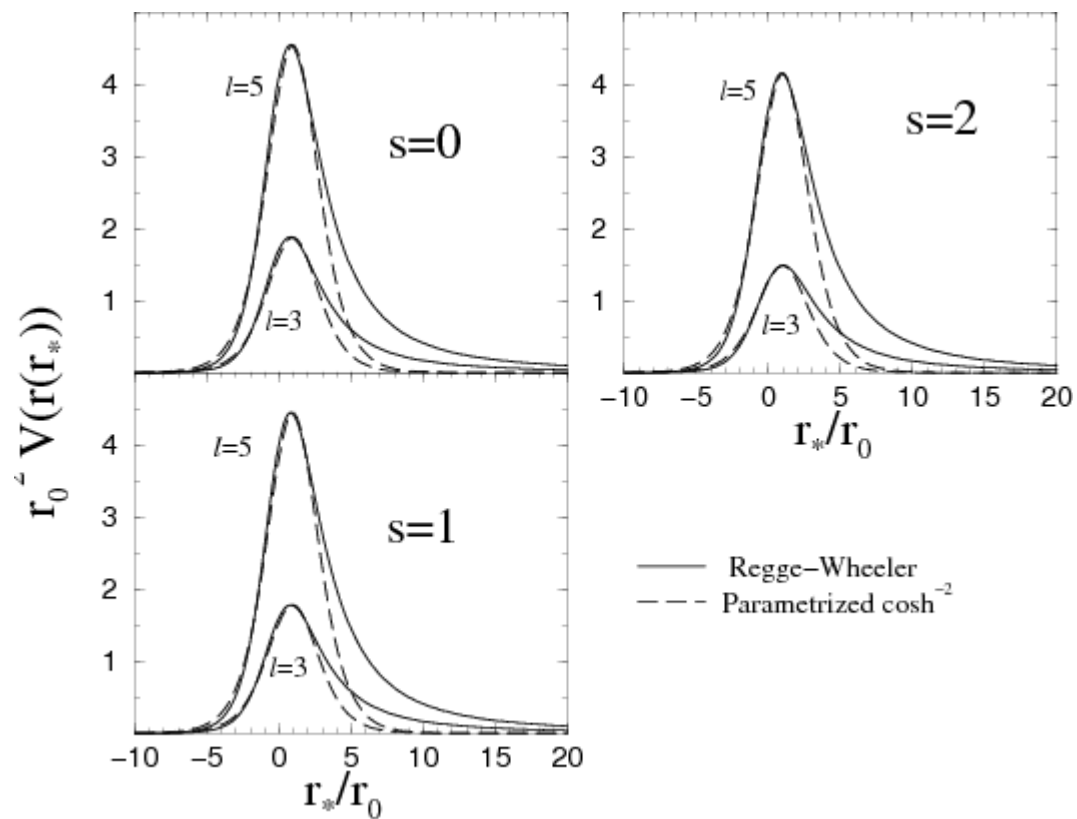
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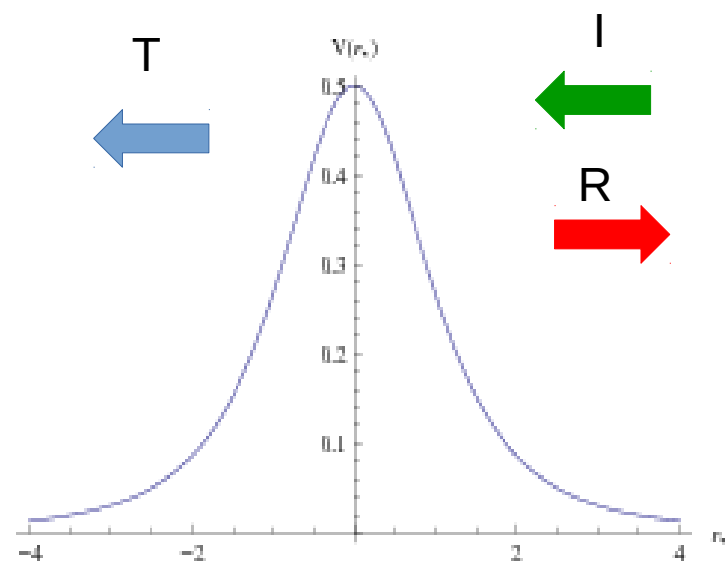
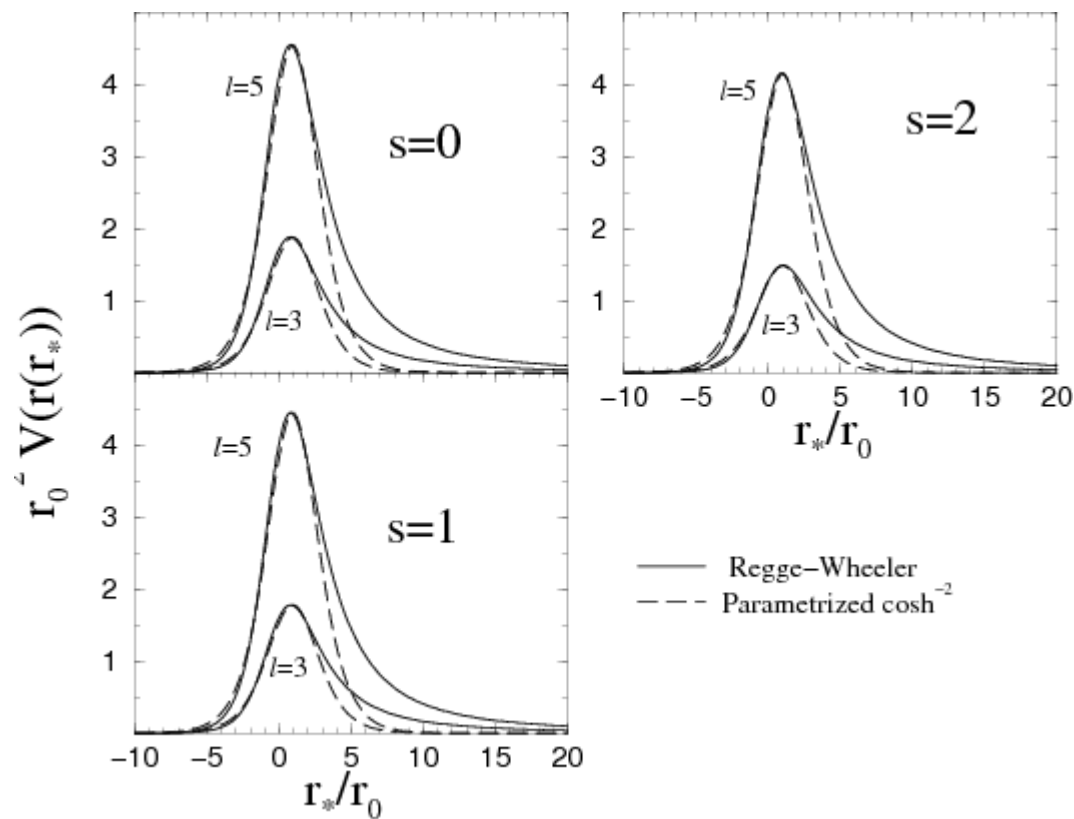
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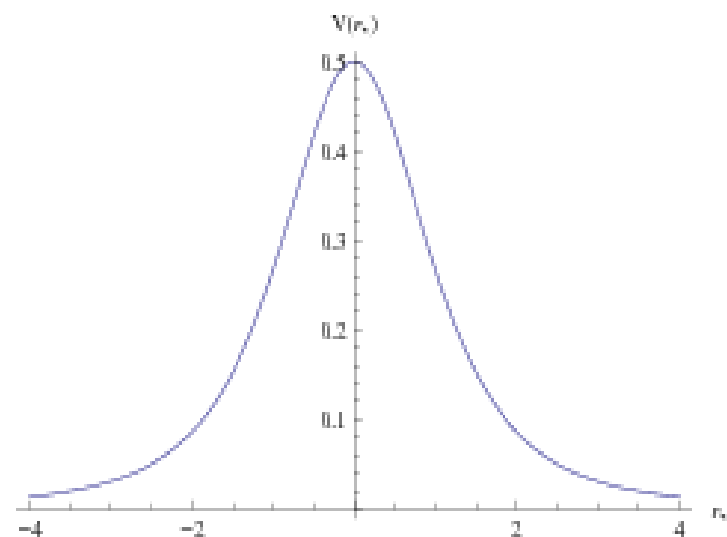
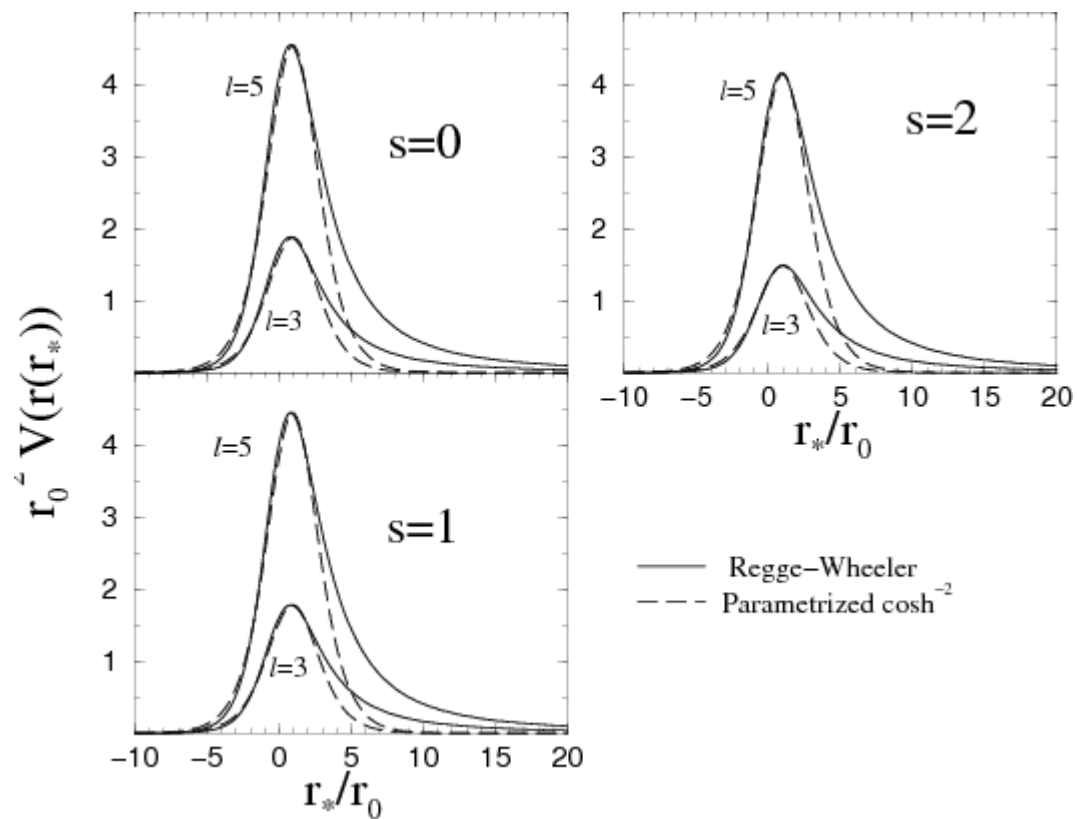
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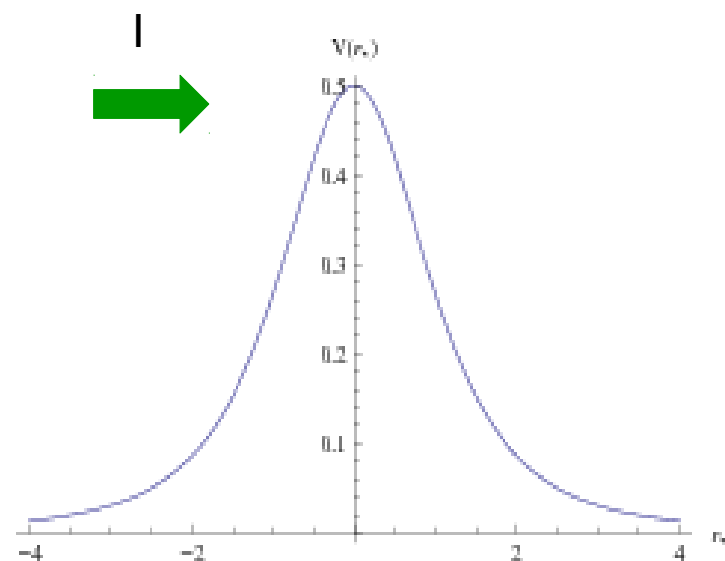
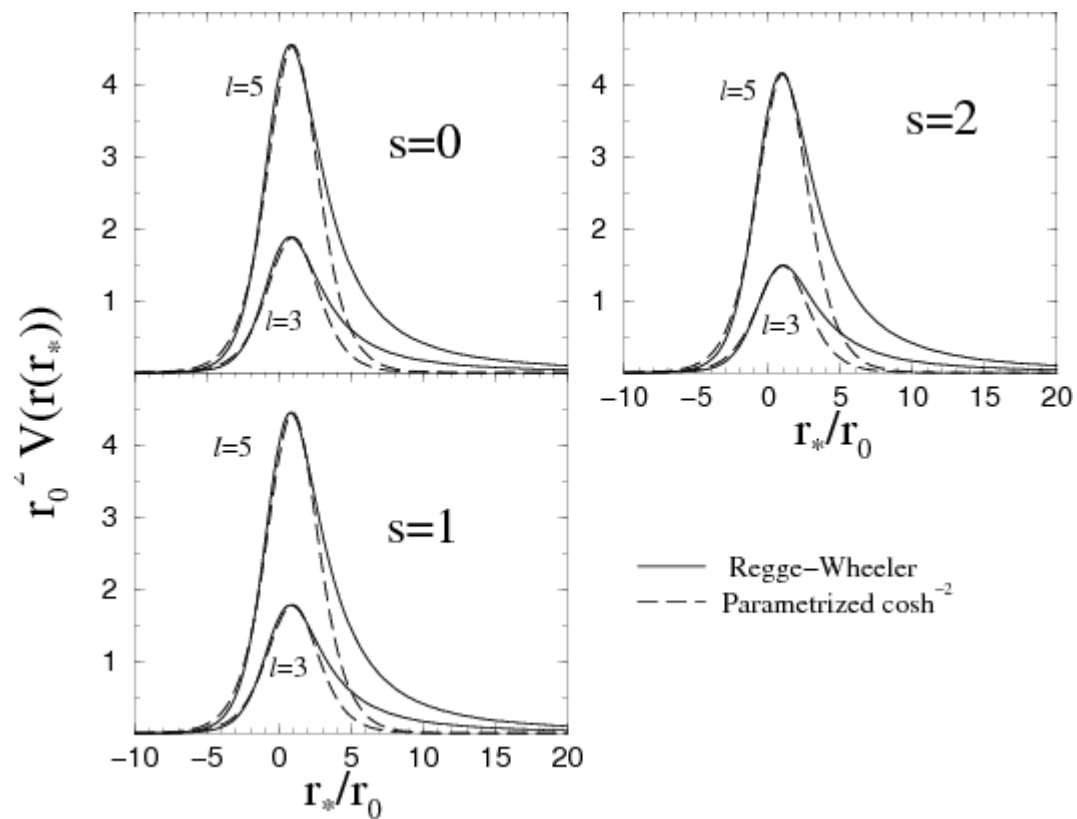
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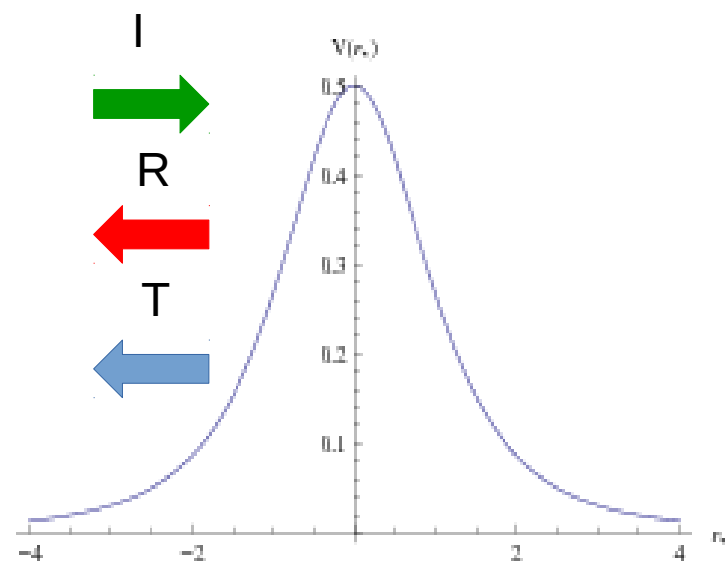
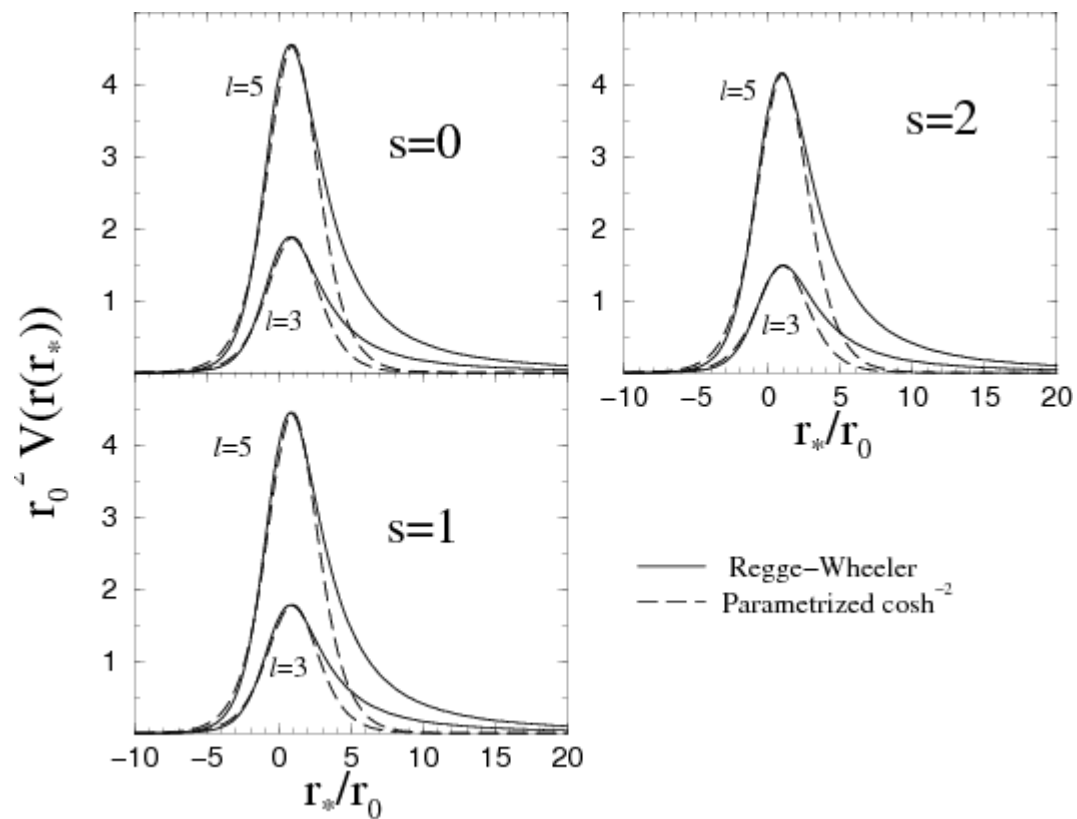
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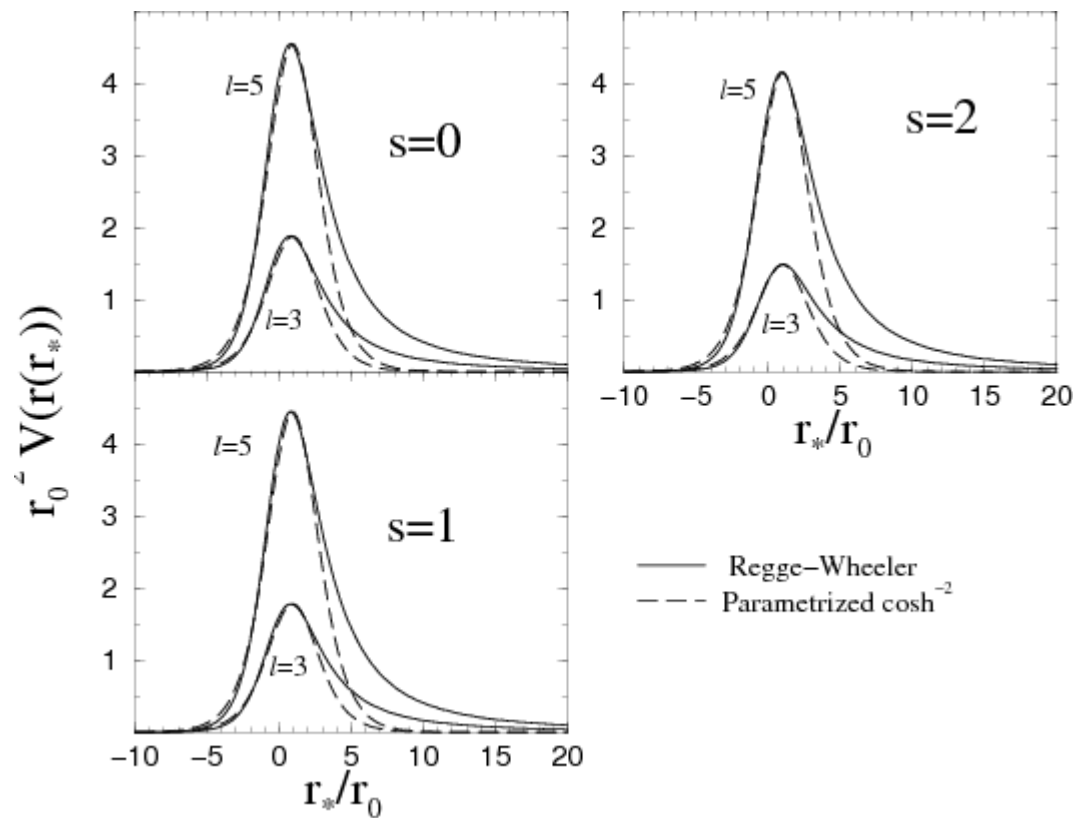
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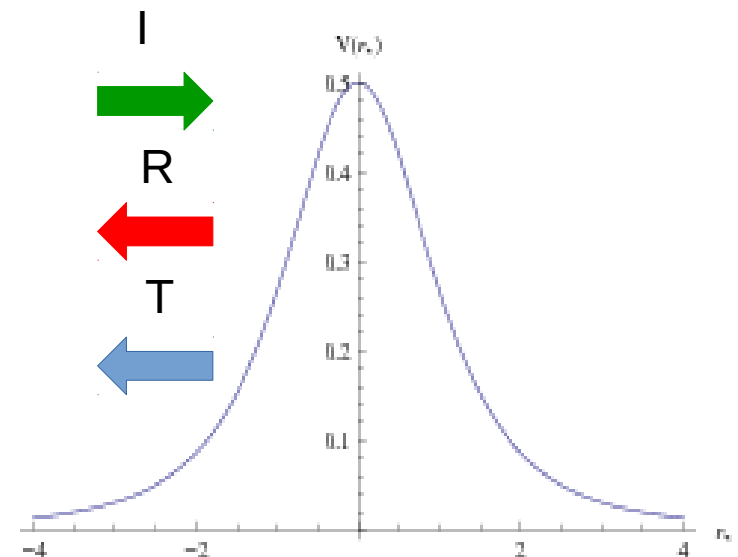


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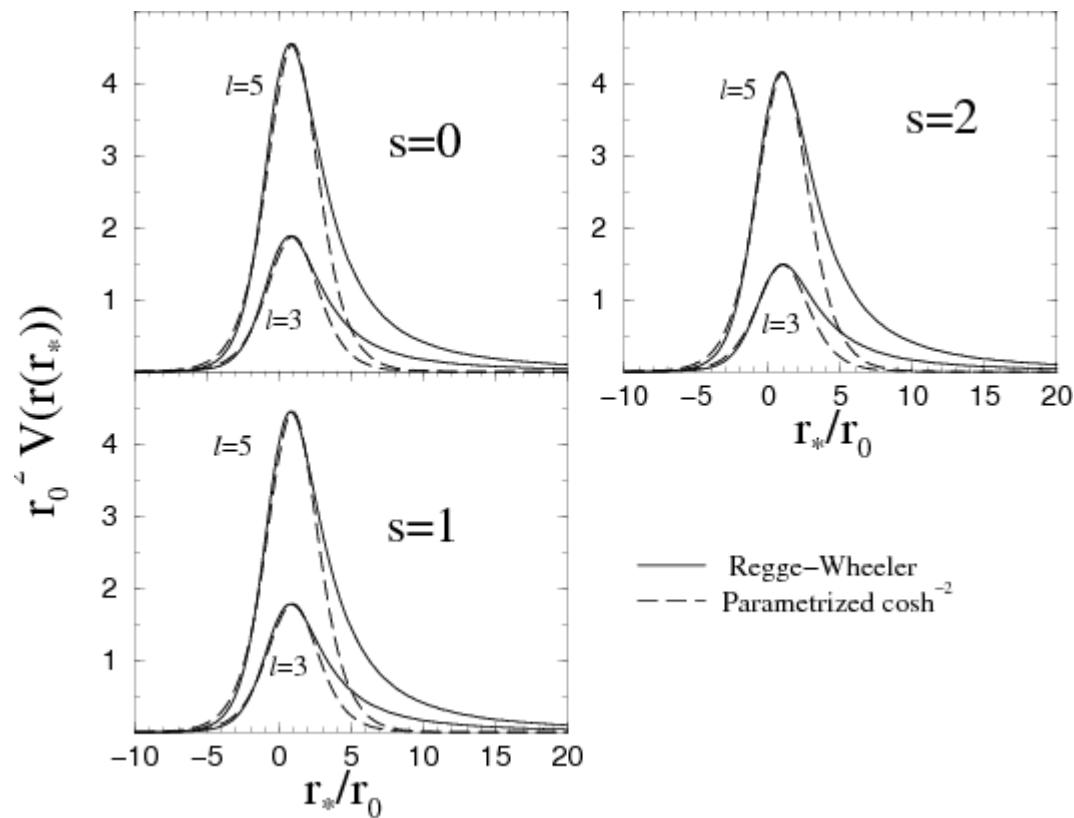


Transformação de Bogolubov

$$\frac{|\beta_f|^2}{|\alpha_f|^2} = \exp\left(\frac{-4\pi^2 f}{g_H}\right)$$



Espalhamento por BN

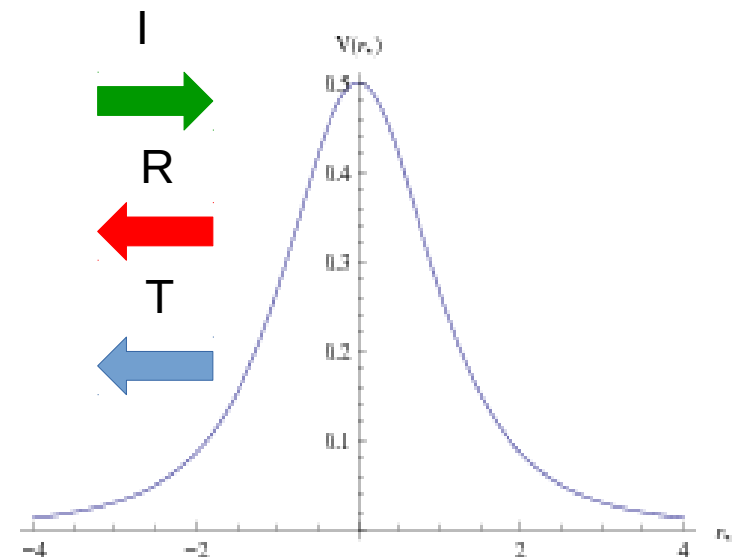


Radiação de Hawking

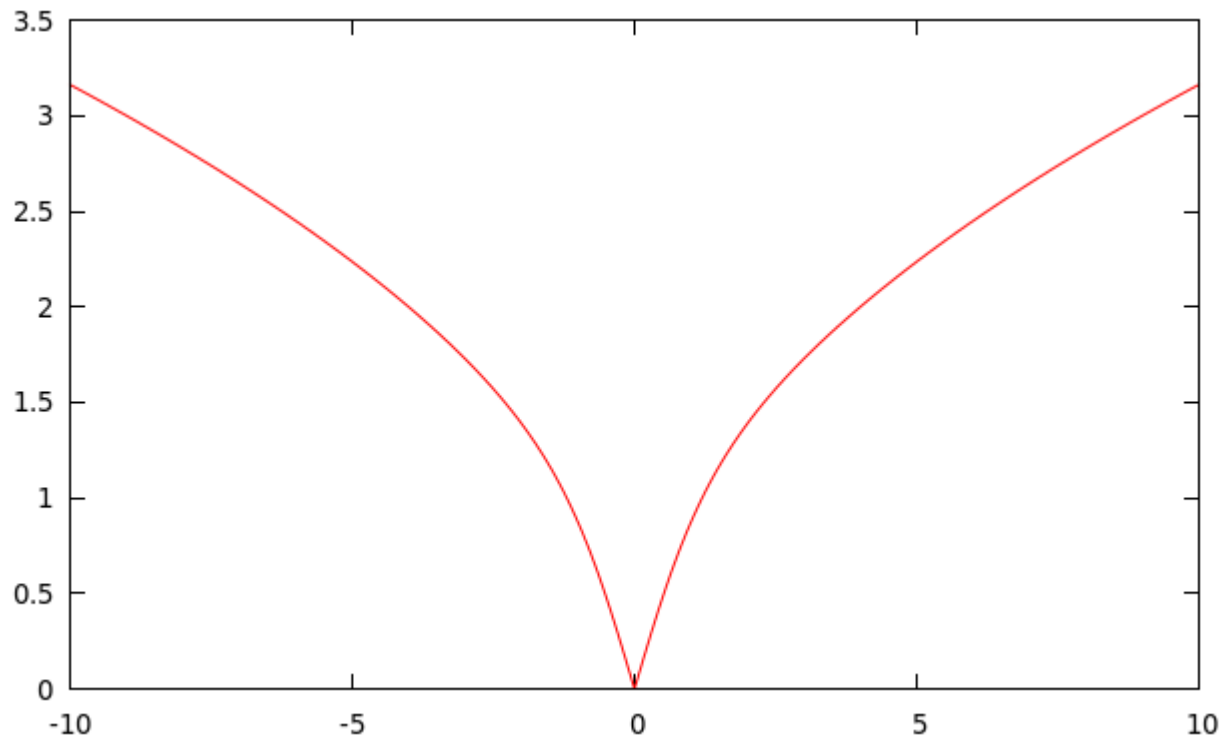


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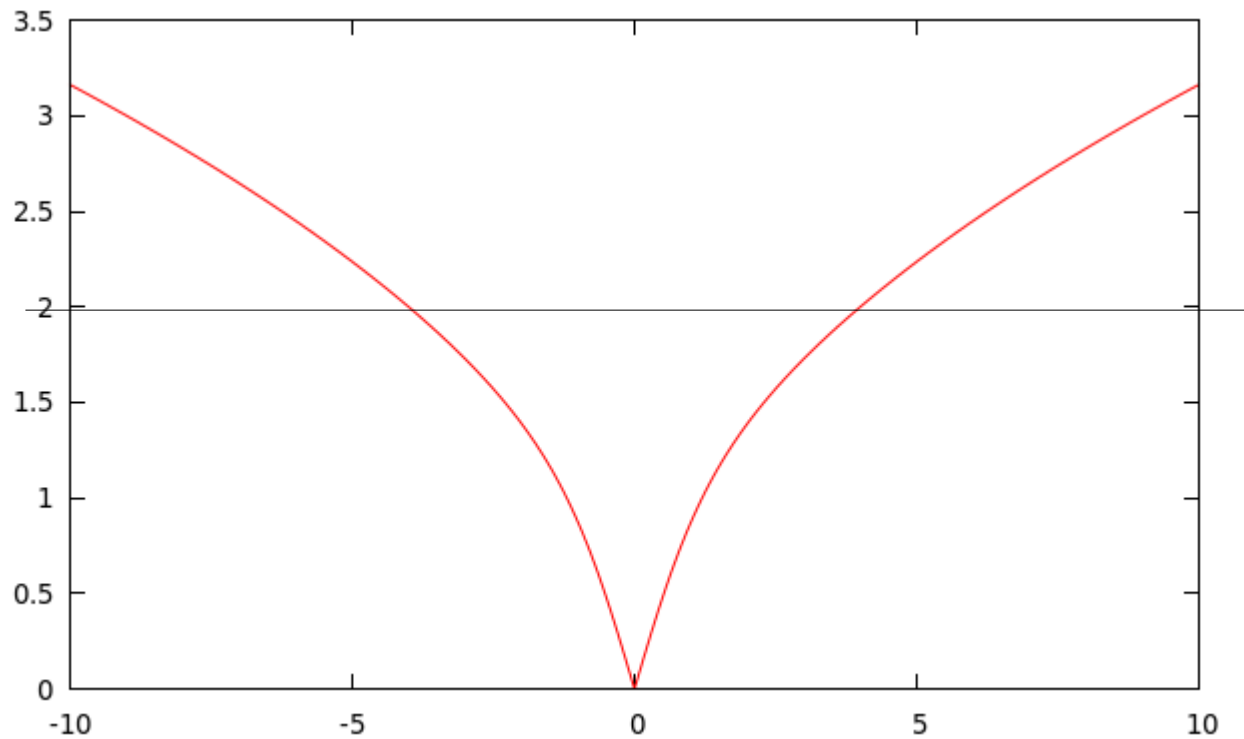


Ondas de superfície



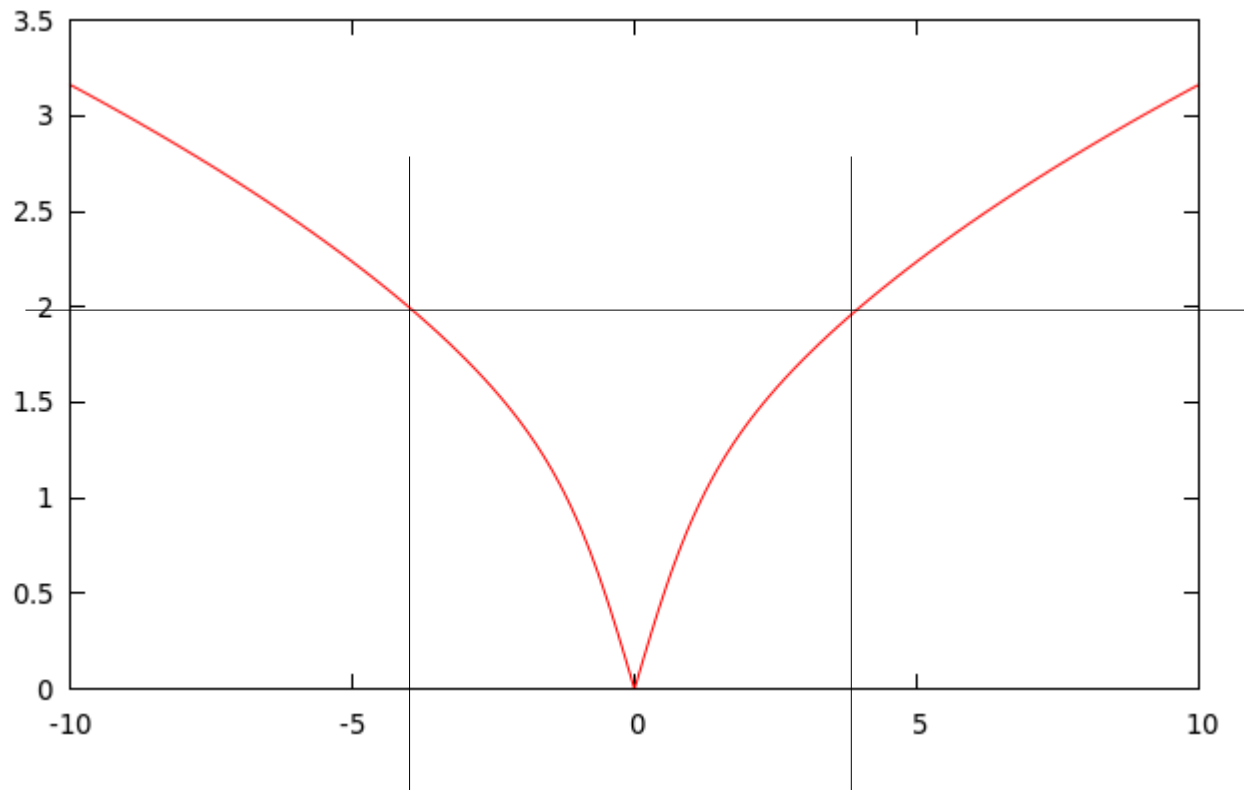
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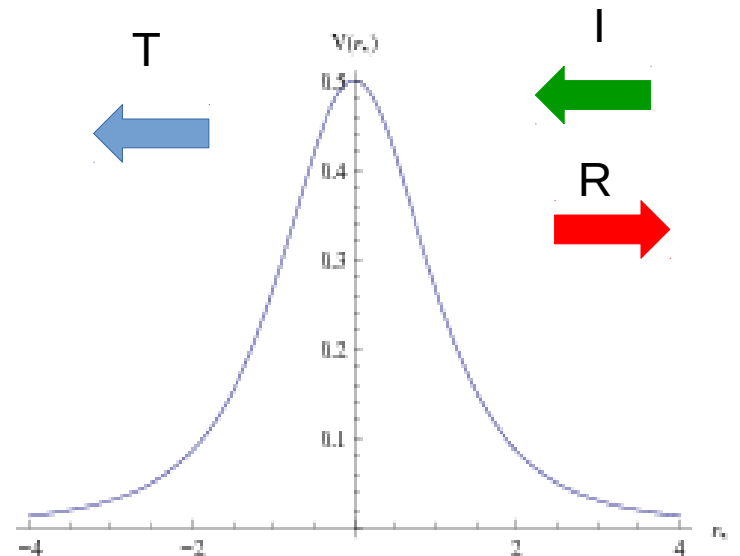
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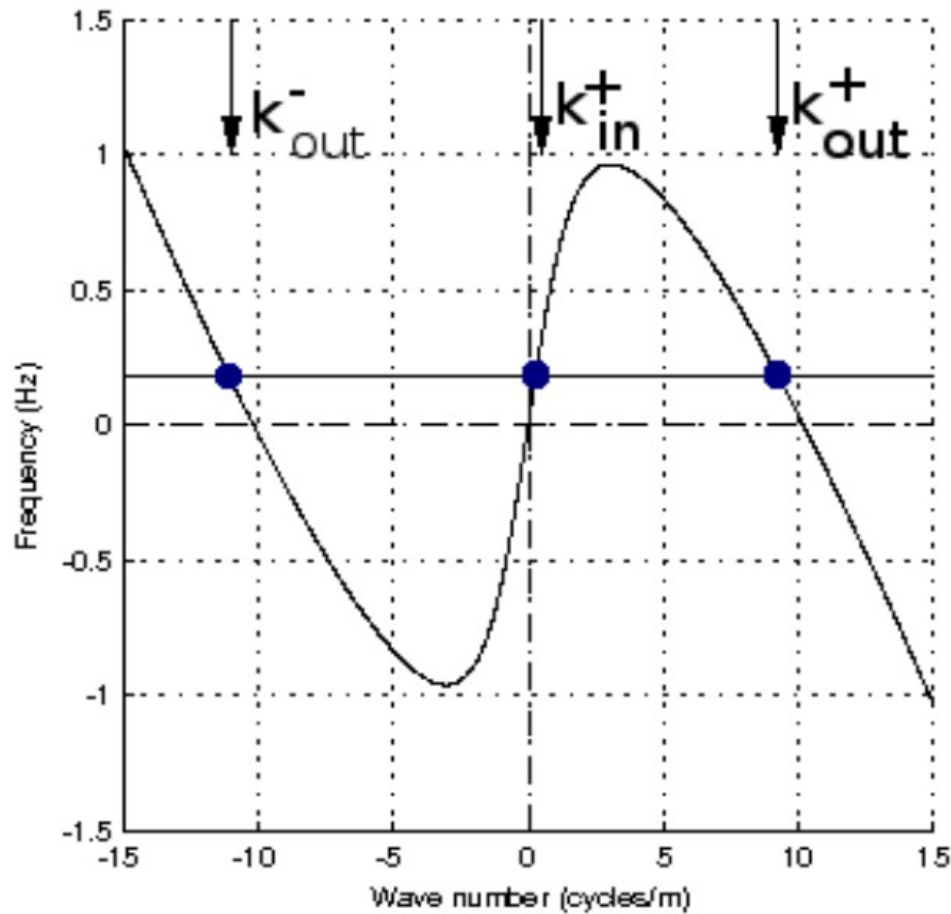
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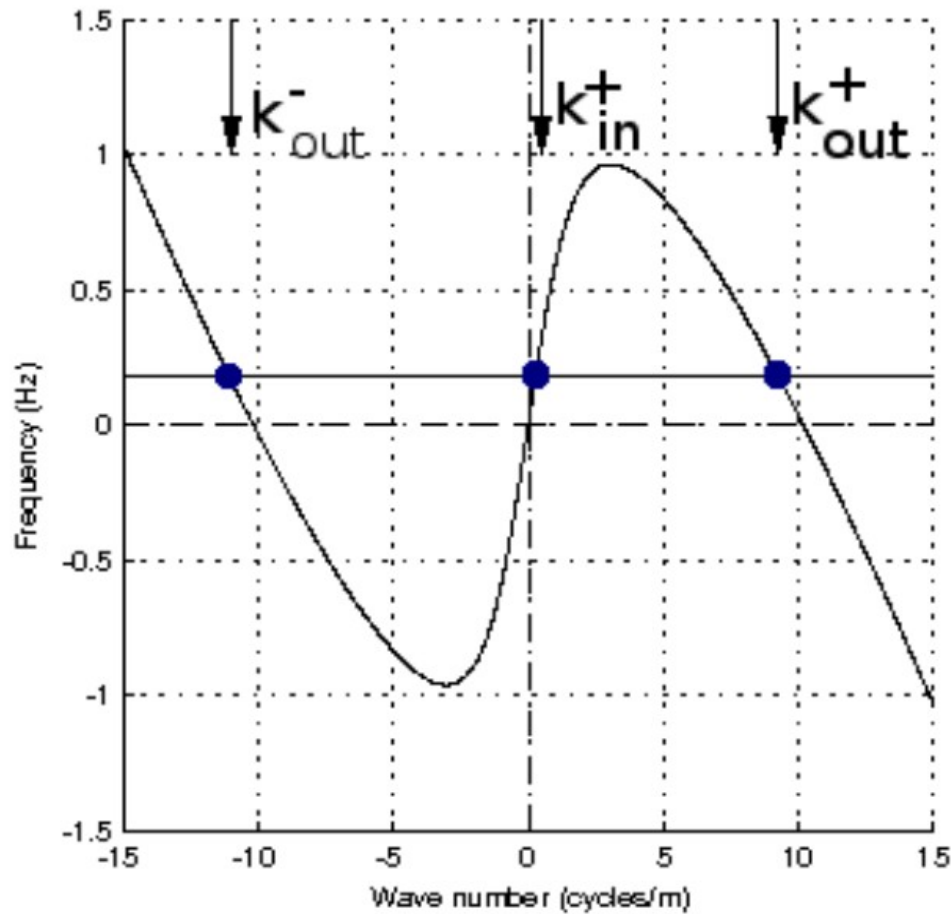


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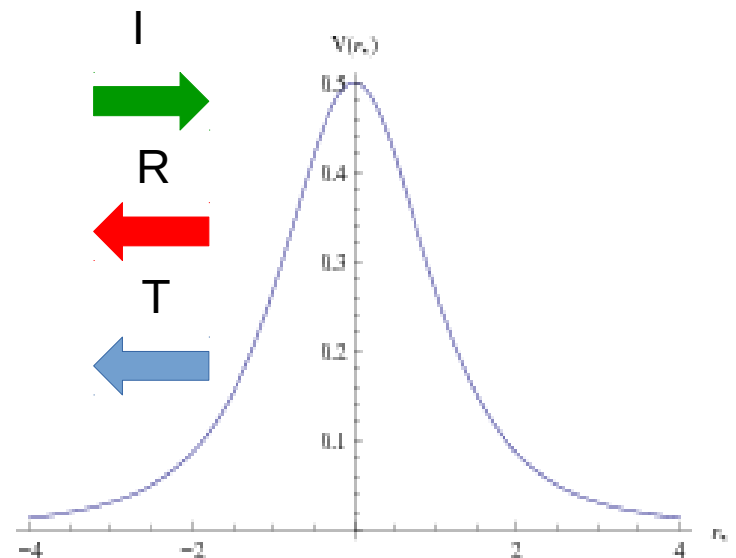


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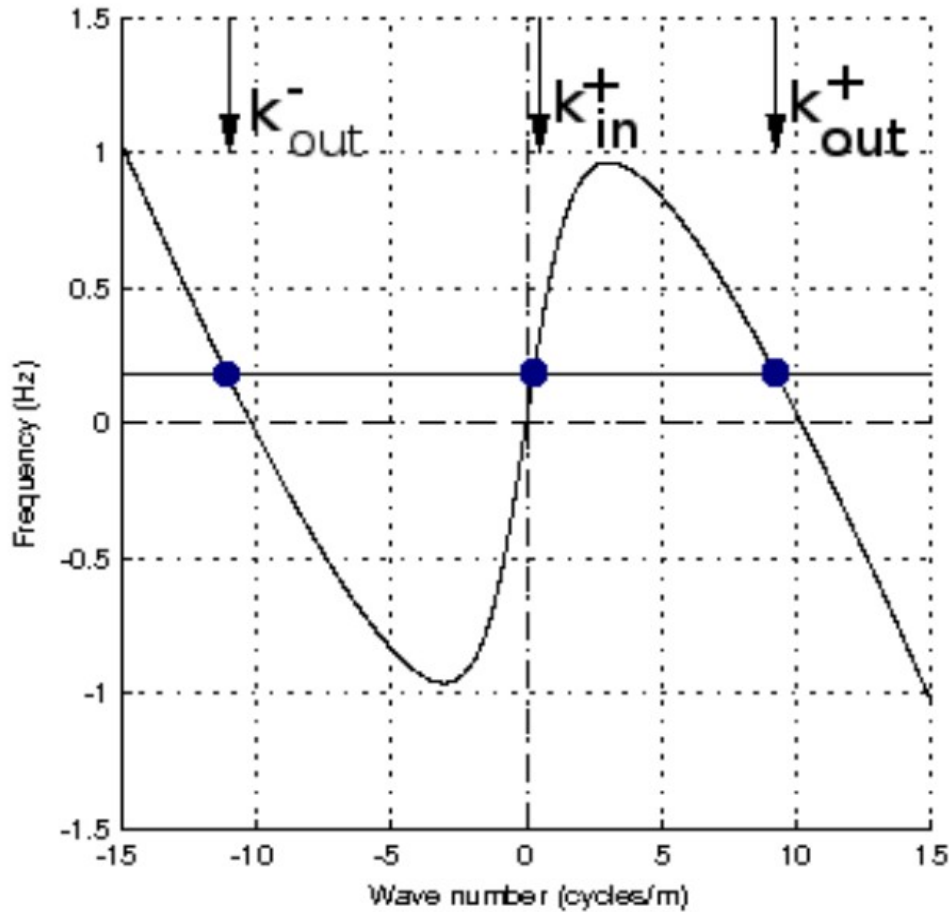
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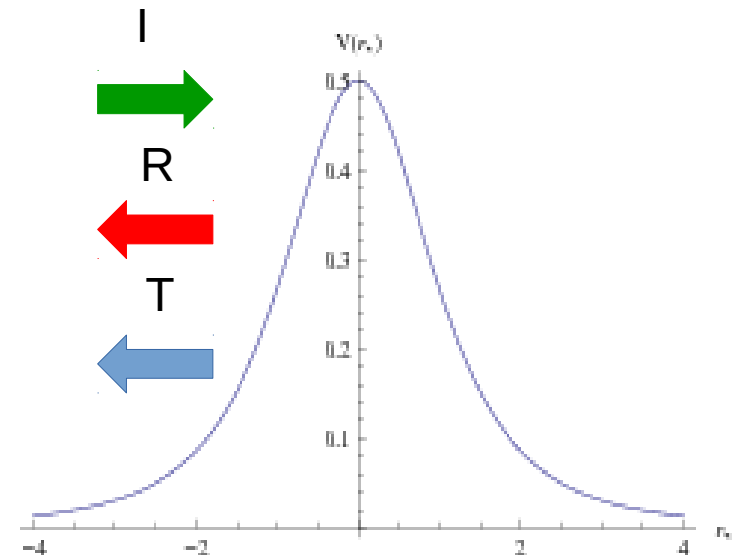
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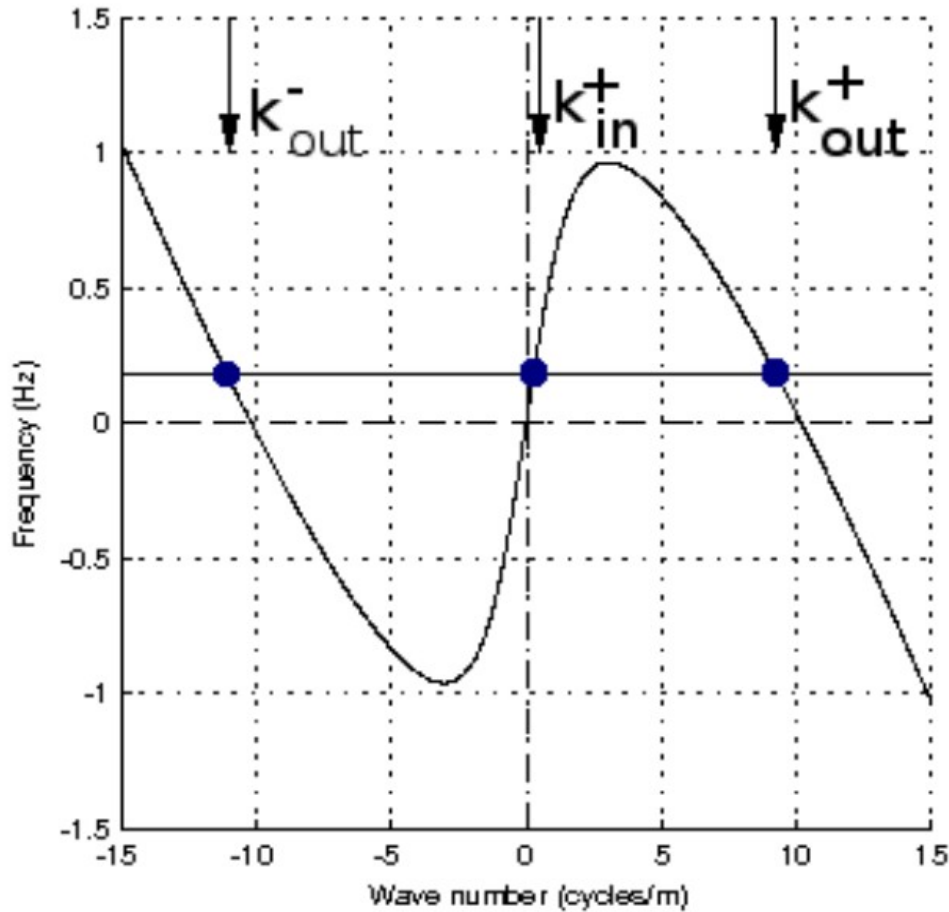
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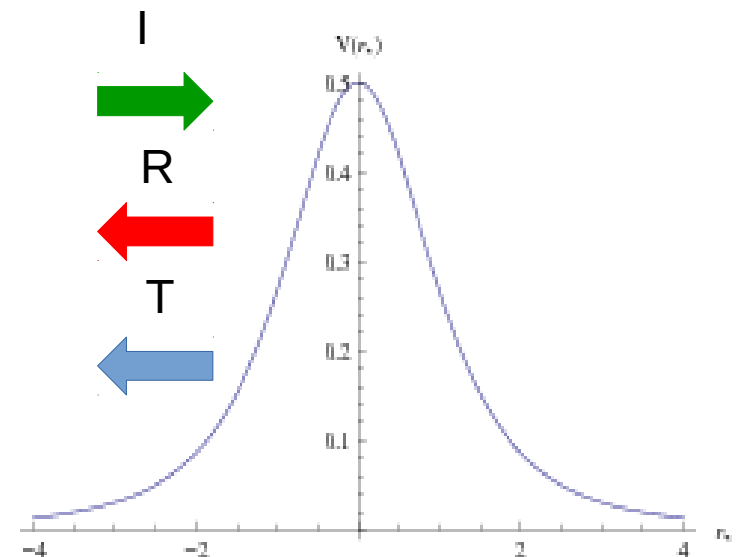
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Radiação de Hawking???



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Experimento

Experiment procedures

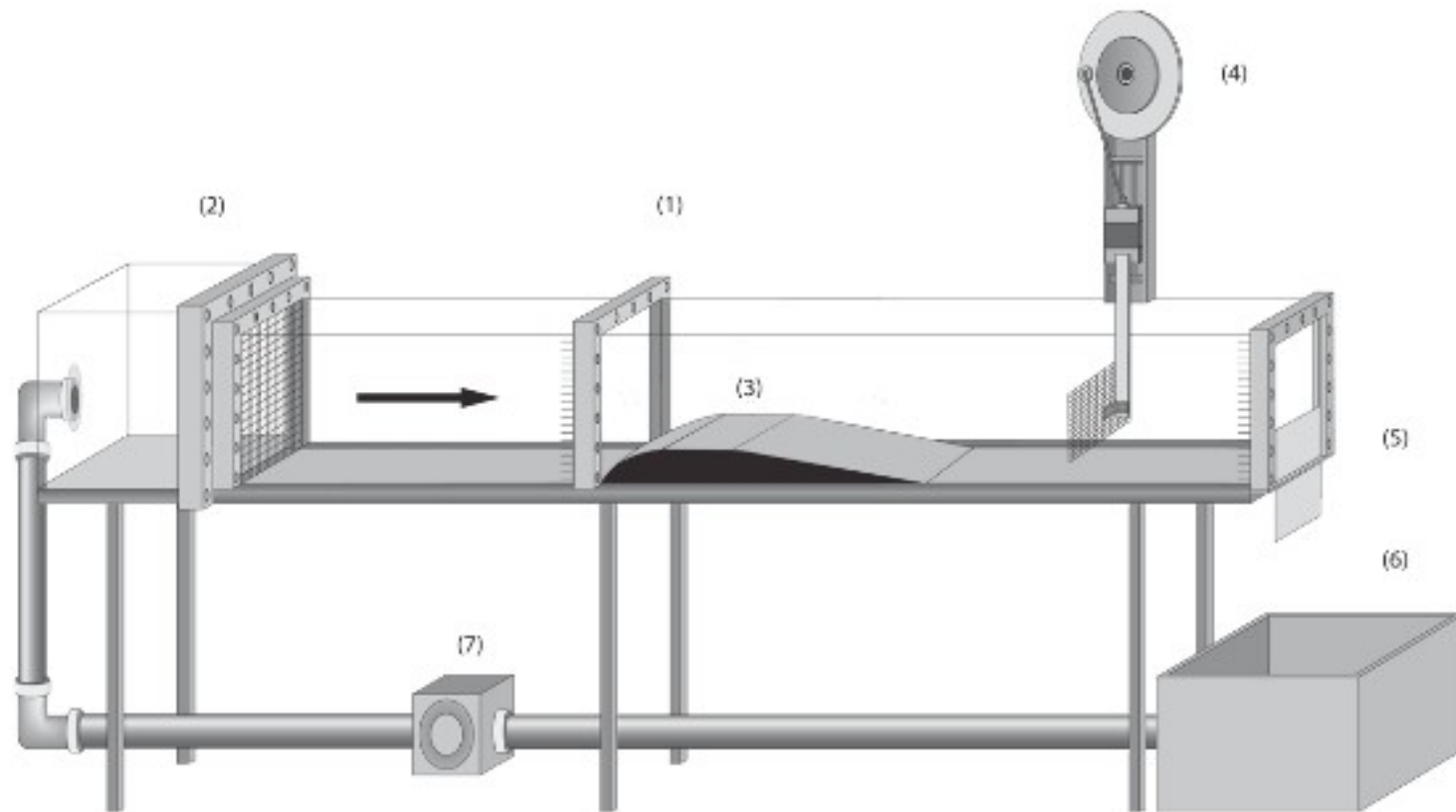


Figure 2 | Experimental apparatus. The experimental apparatus used in our experiments: (1) flume, (2) intake reservoir, (3) obstacle, (4) wave generator, (5) adjustable weir, (6) holding reservoir, and (7) pump and pump valve.

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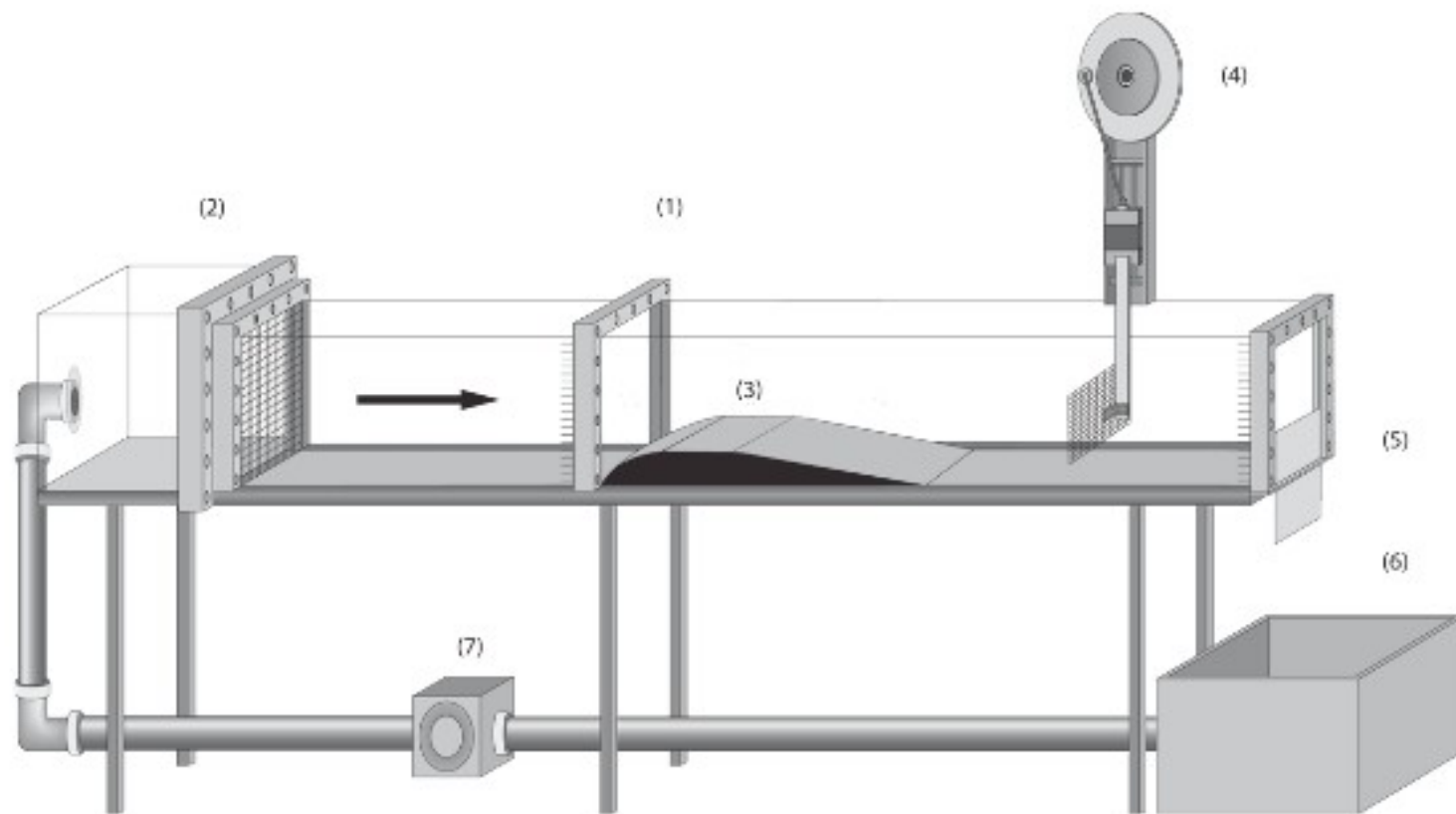


Figure 2 | Experimental apparatus. The experimental apparatus for the experiments: (1) flume, (2) intake reservoir, (3) obstacle, (4) pulley system, (5) adjustable weir, (6) holding reservoir, and (7) pump and pump valve.

Physical Review Letters

moving physics forward

Silke Weinfurter¹, Edmund W. Tedford², Matthew C. J. Penrice¹, William G. Unruh¹, and Gregory A. Lawrence²

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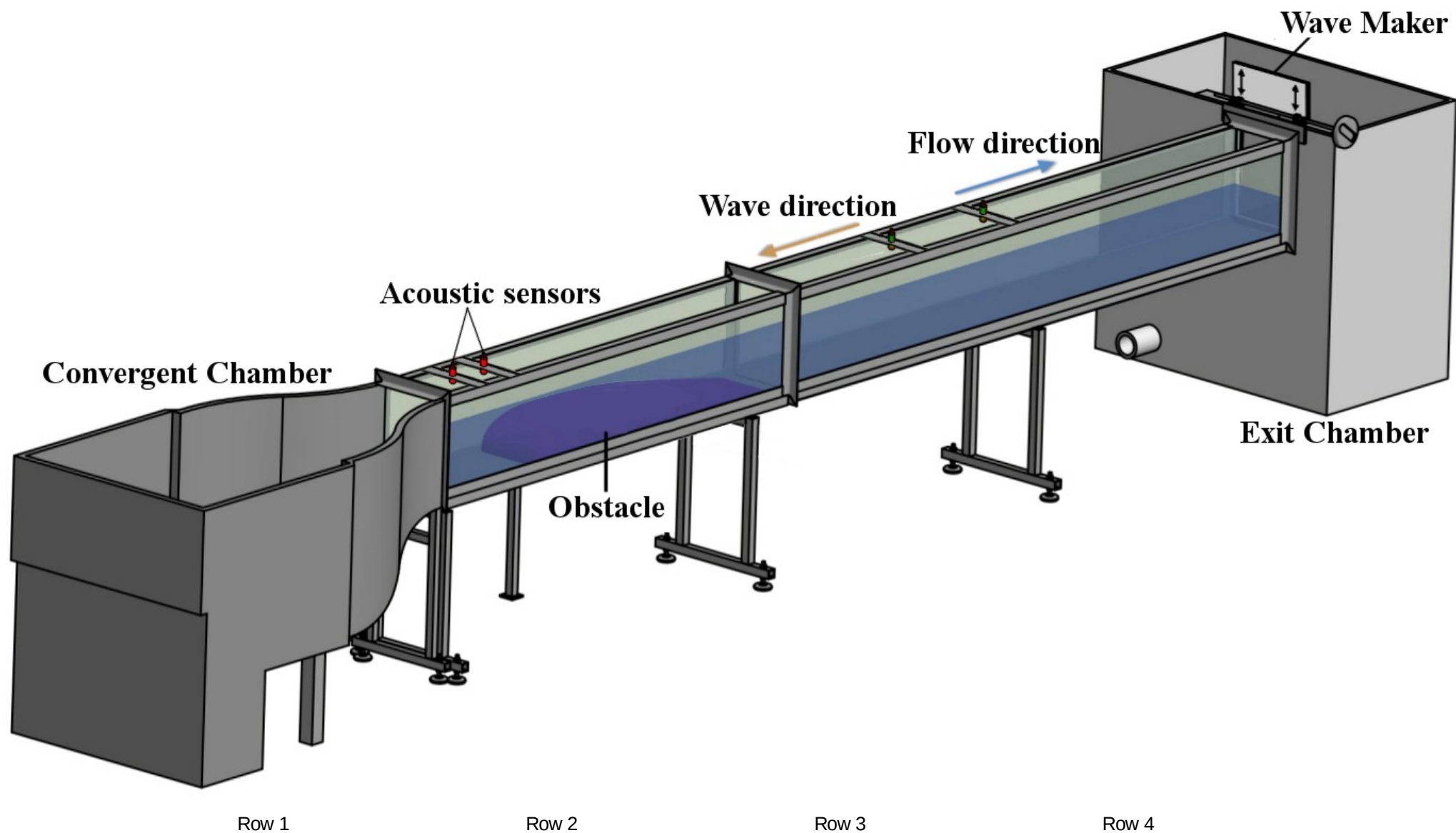
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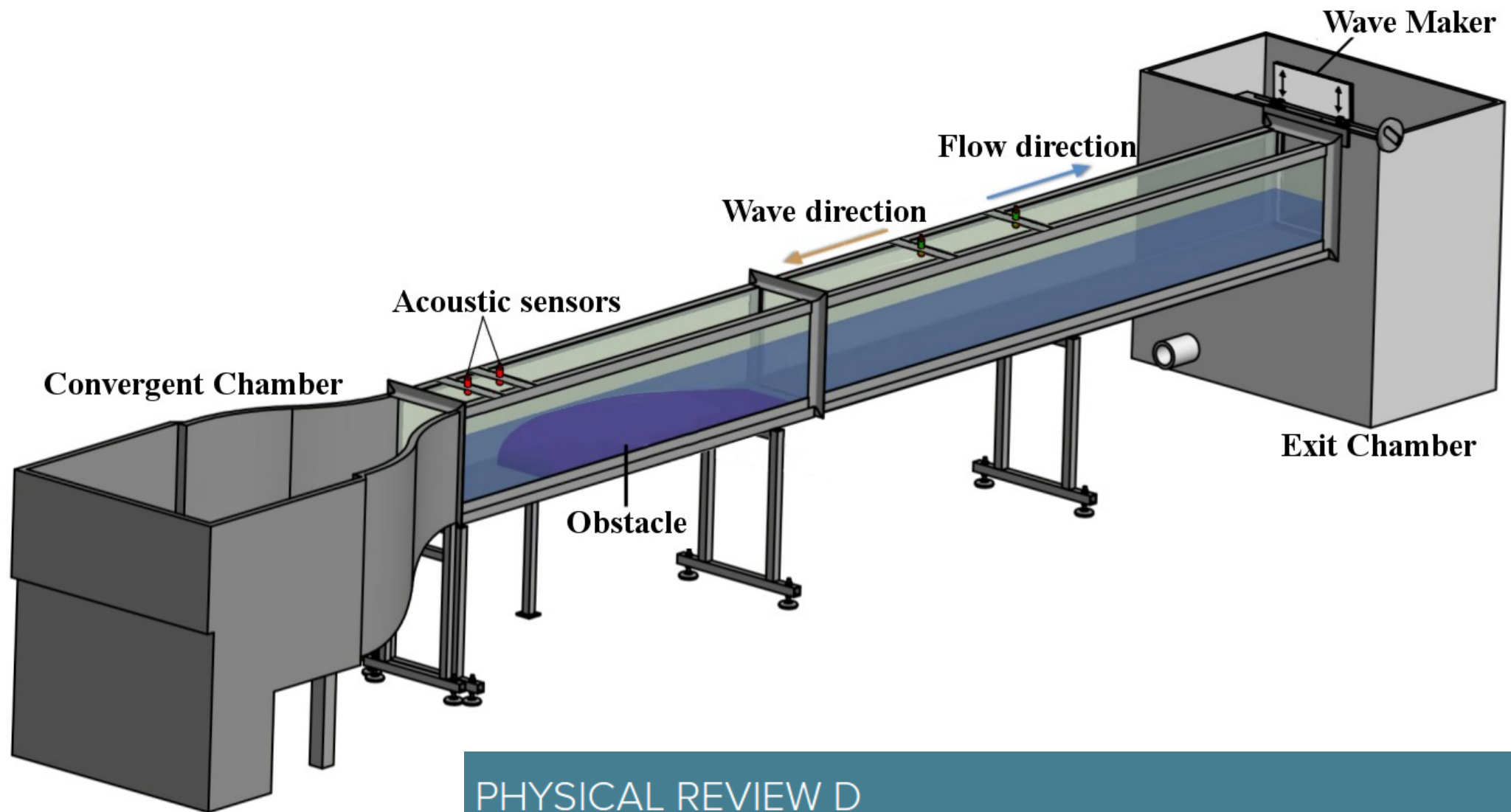
Experimento



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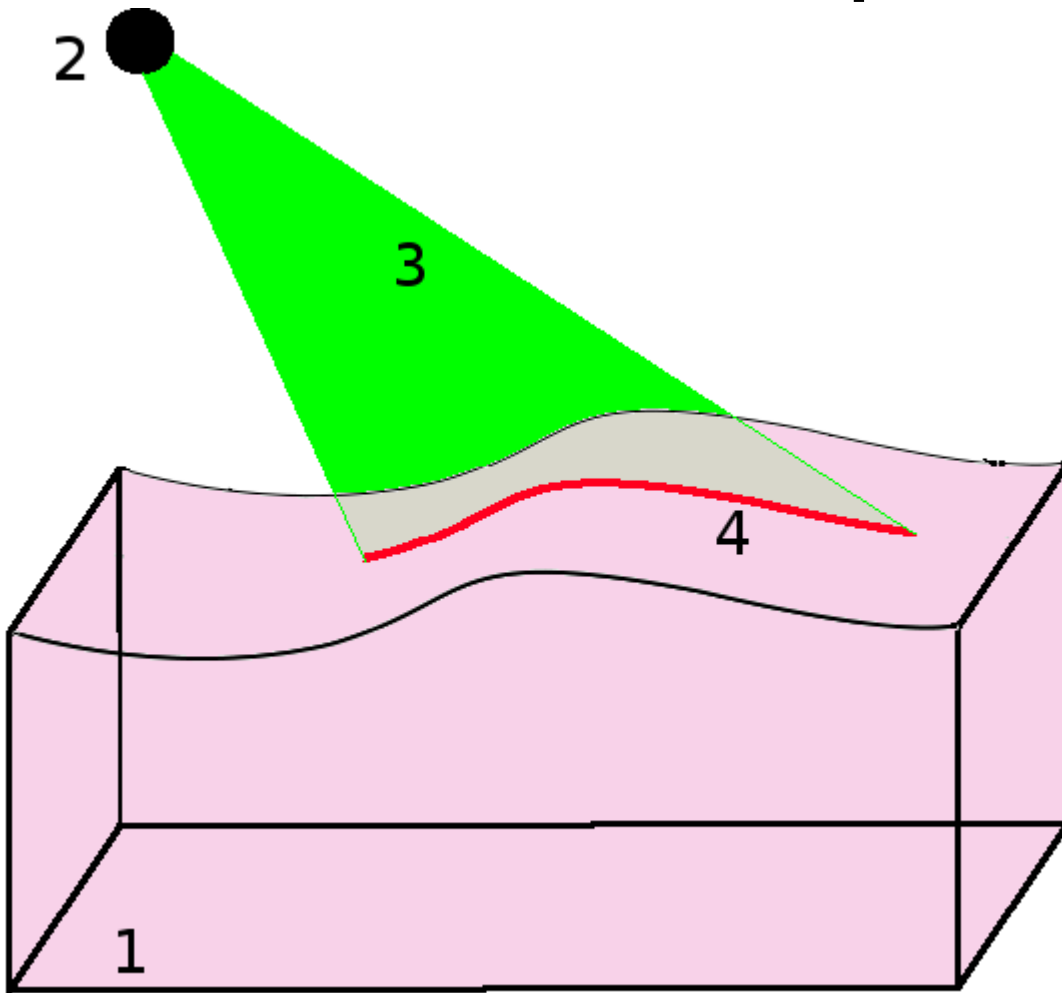


Wave blocking and partial transmission in subcritical flows over an obstacle

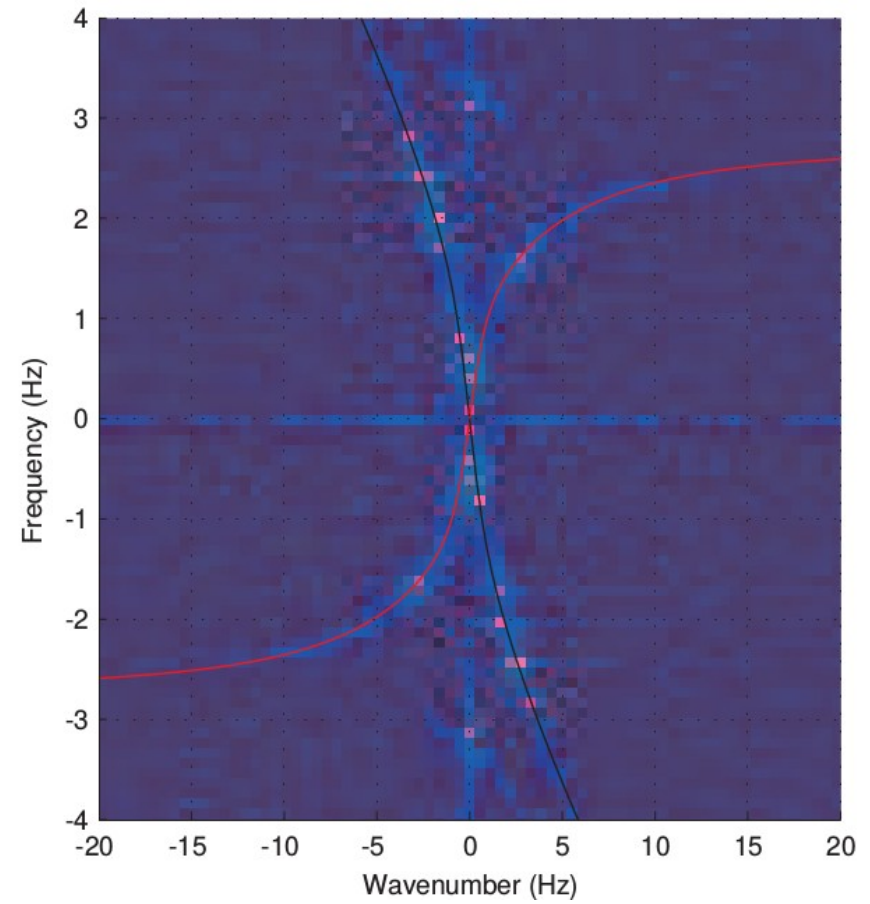
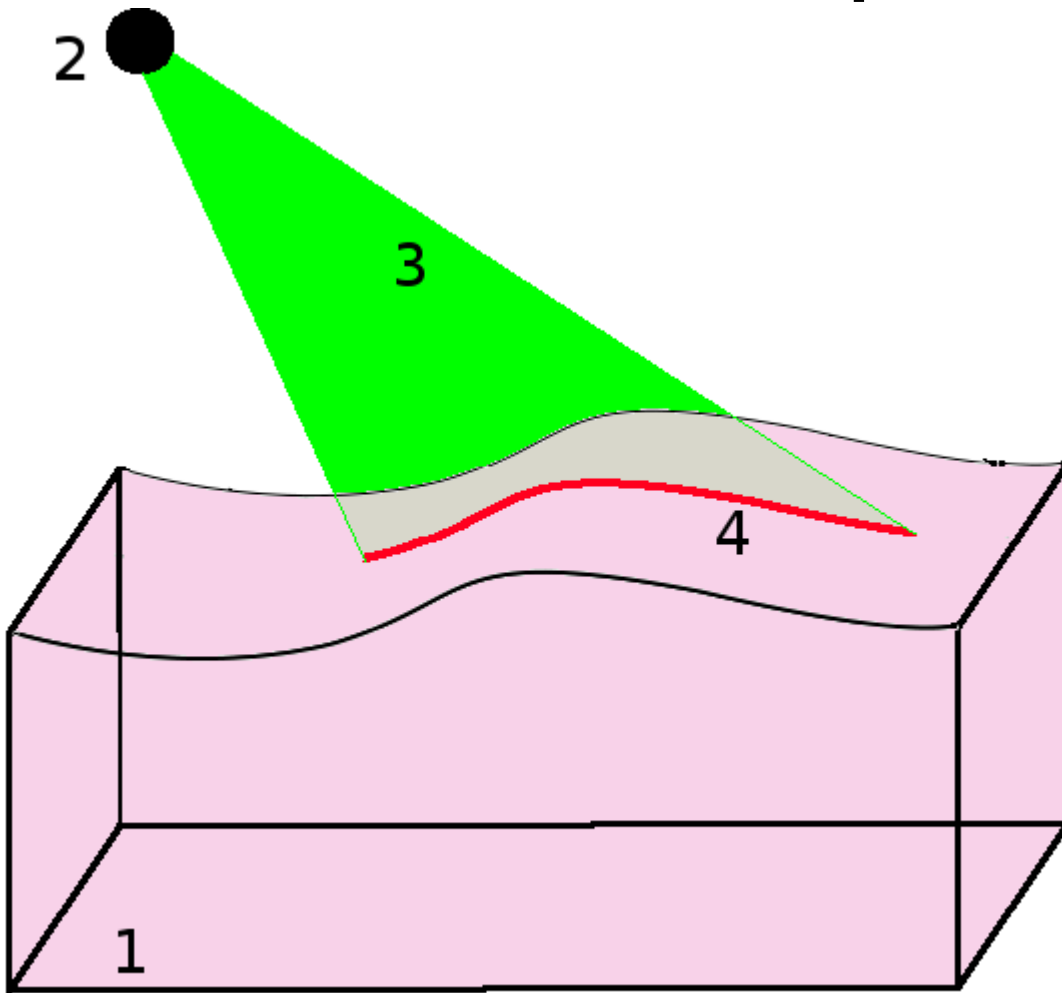
Léo-Paul Euvé, Florent Michel, Renaud Parentani, and Germain Rousseaux

Phys. Rev. D **91**, 024020 – Published 13 January 2015

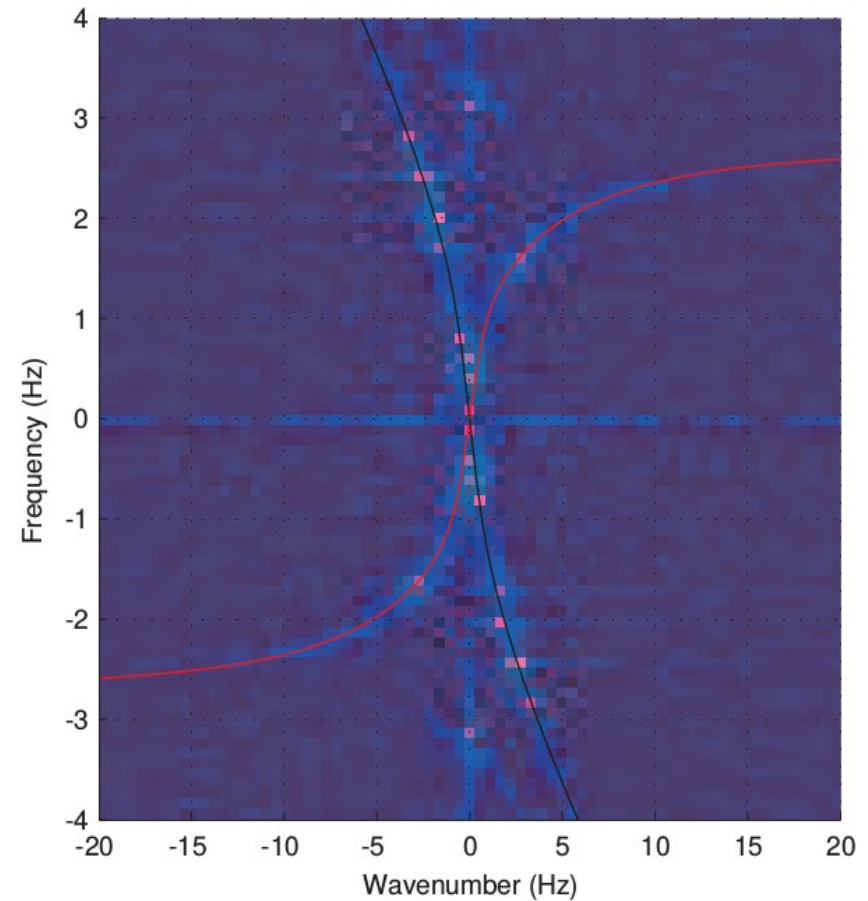
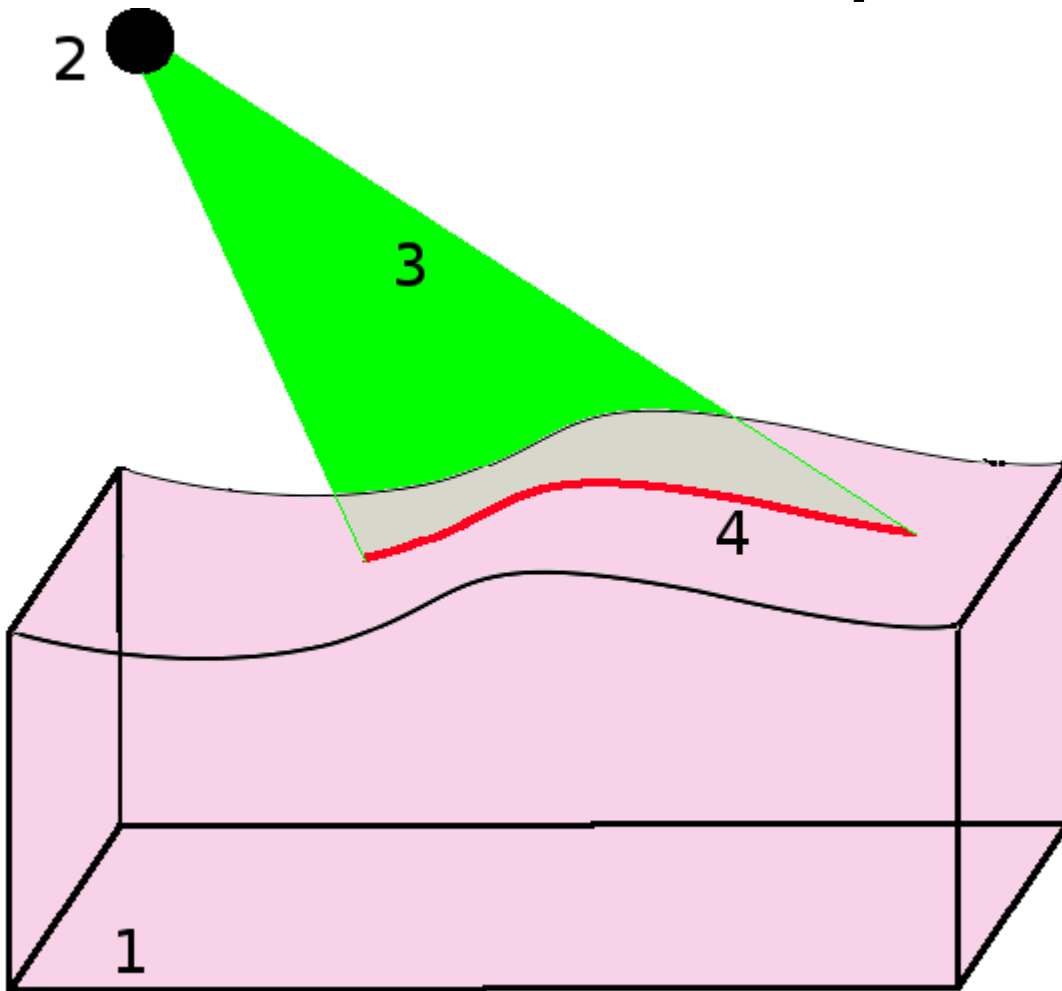
Esperimento



Experimento



Experimento

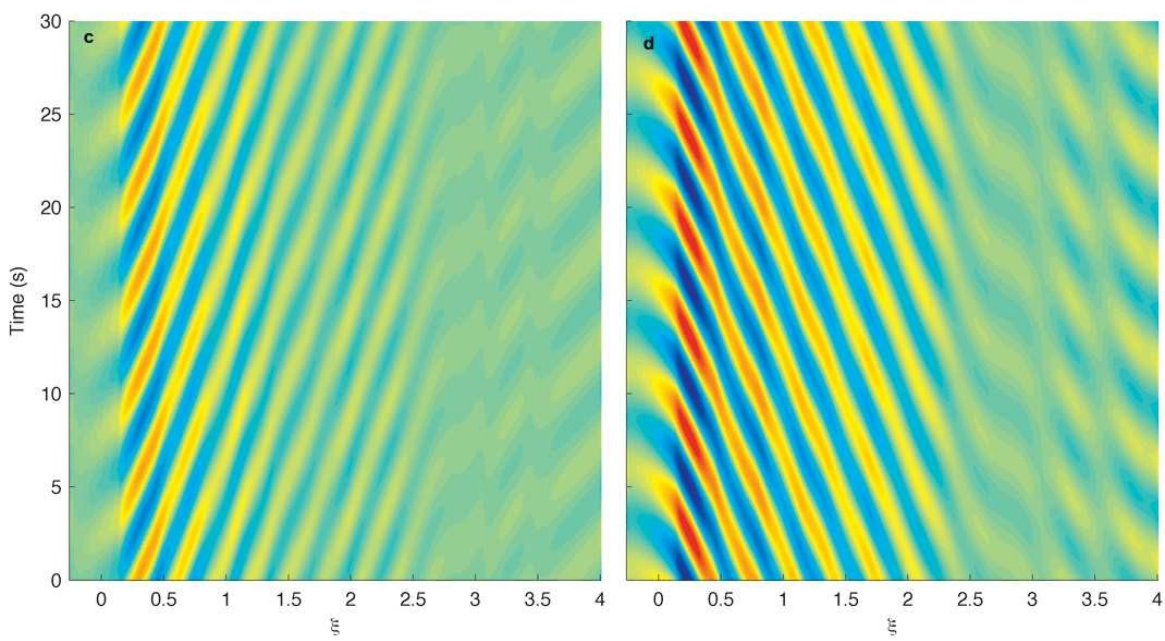
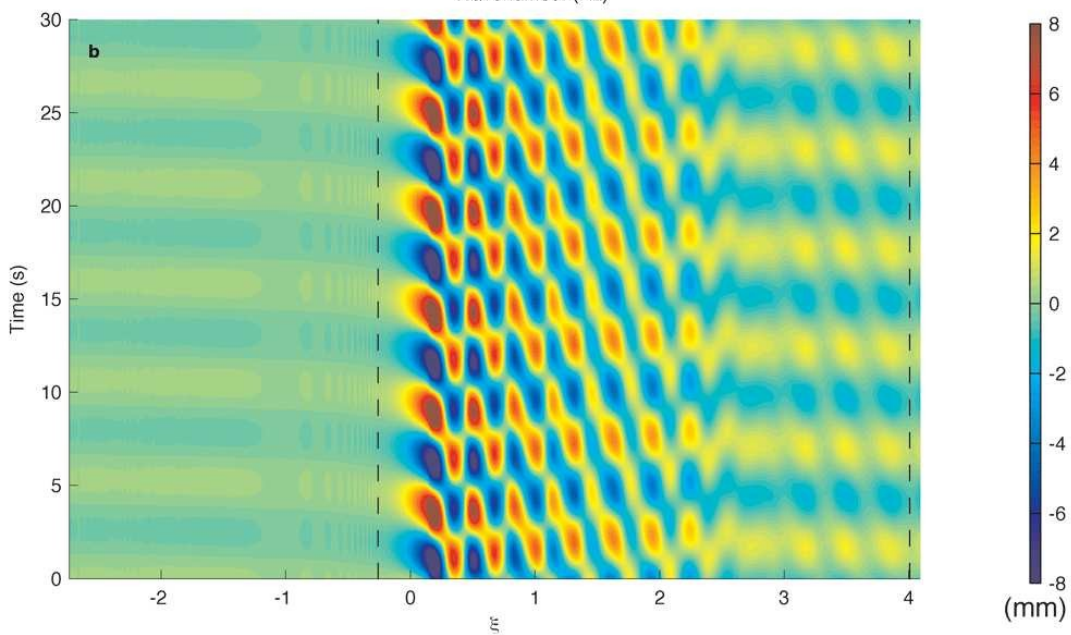
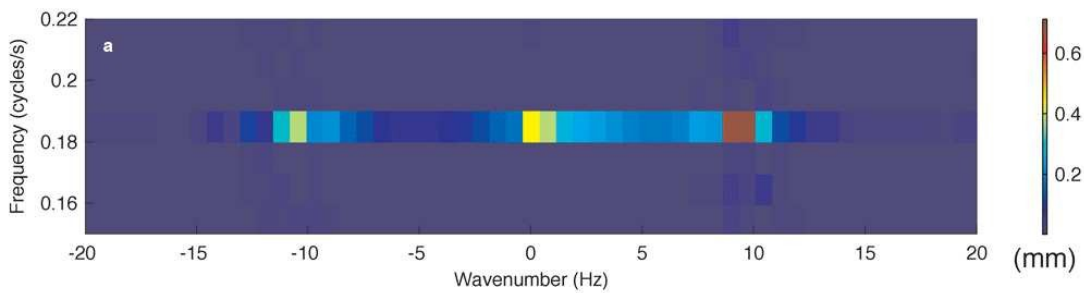


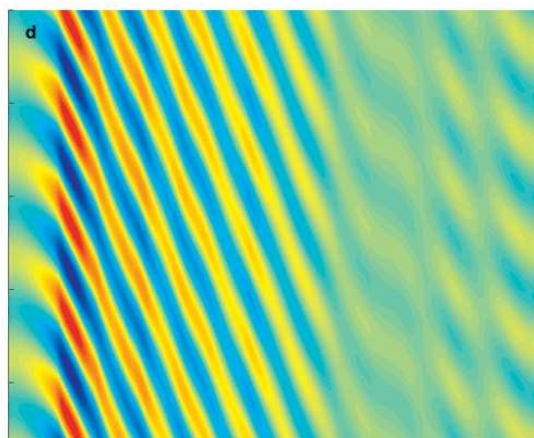
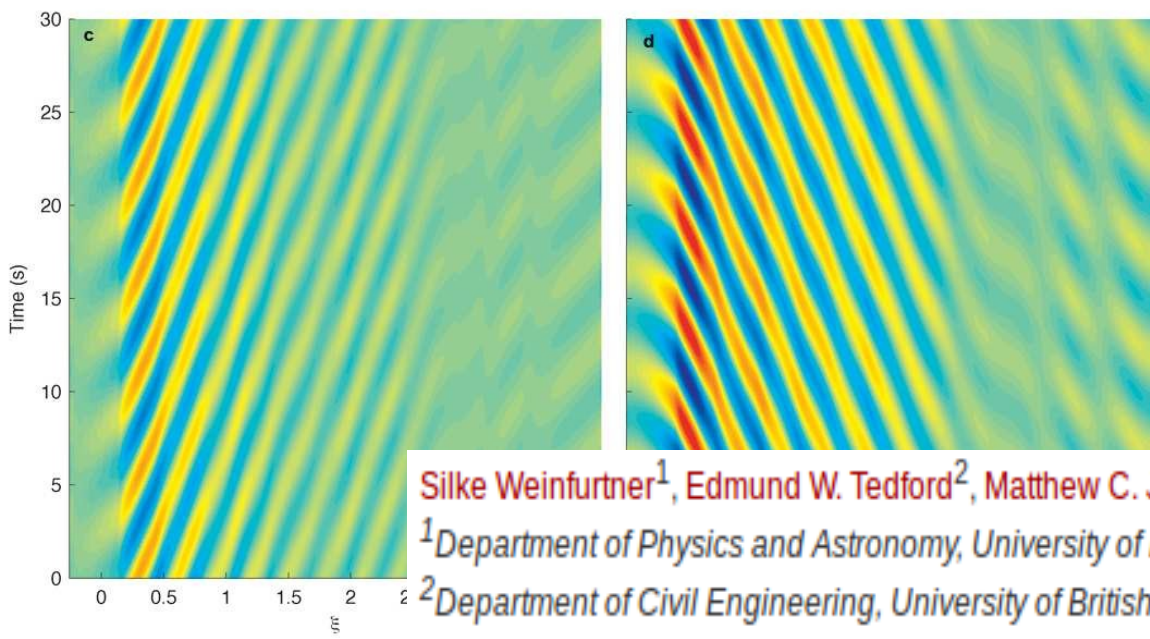
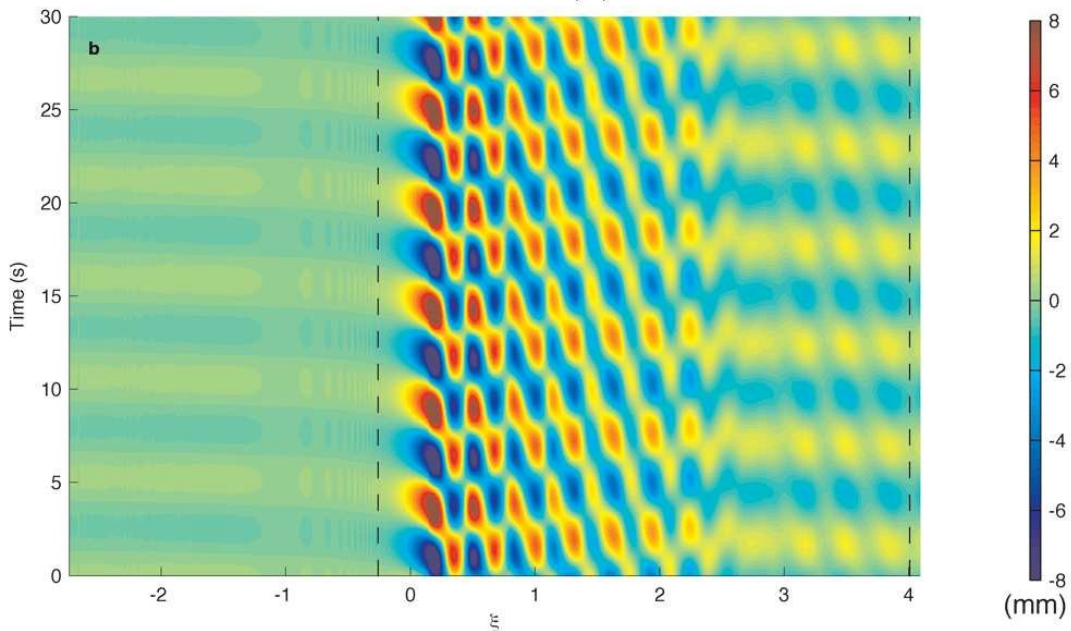
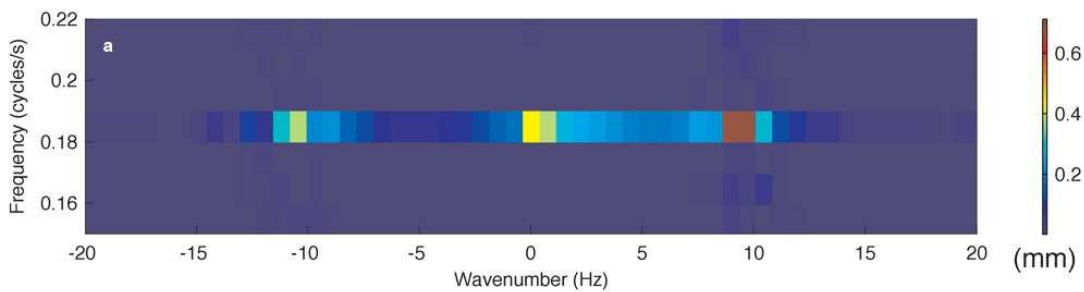
Physical Review Letters
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