

Mini-couse on Dark Matter



Quantum Summer 2025

Iriri, ES, Brazil. April 07-11, 2025.

Diana López Nacir



Outline

- **Lecture 1:** Evidence for Dark Matter (DM) and its properties
- **Lecture 2:** DM inhomogeneities in the standard CDM model and others (WDM, SI-WDM)
- **Lecture 3:** Ultralight DM (spin 0 and 1). Can the spin of ULDM be distinguished on cosmological scales?

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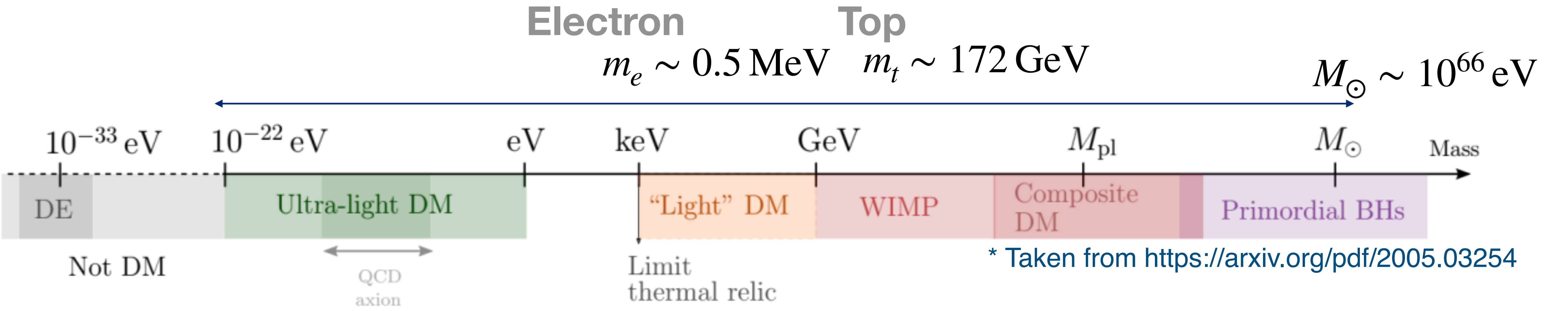
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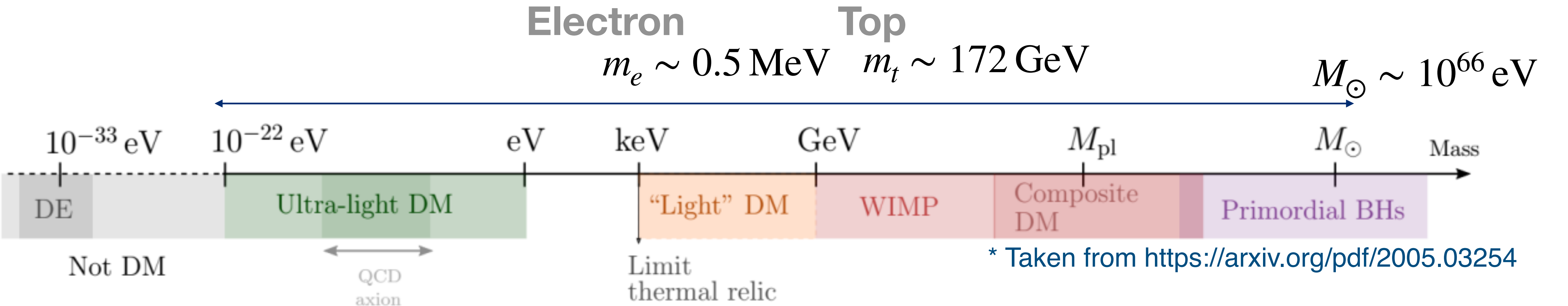


Sketch (not to scale) of the huge range of possible DM models that have been conceived *

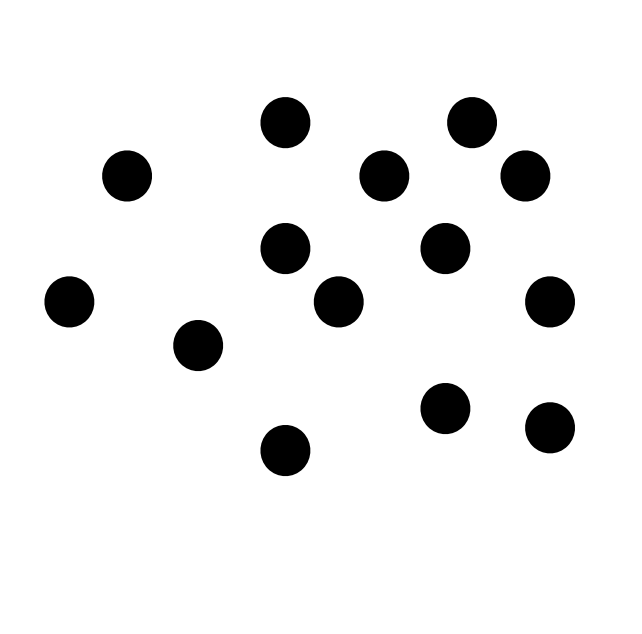


* Taken from <https://arxiv.org/pdf/2005.03254>

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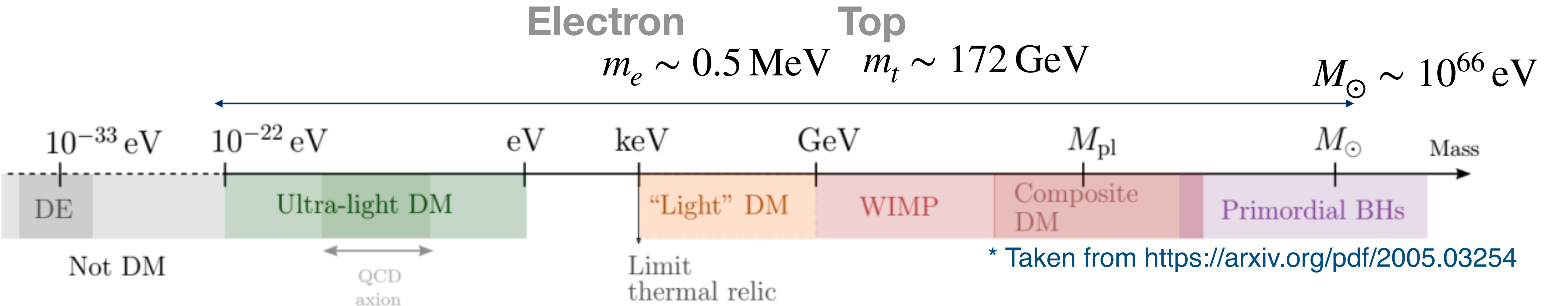


- Standard scenario: distribution of “cold” (small velocity dispersion) non-relativistic massive particles in an expanding FLRW universe



$$N = nV = na^3V_0 = \text{cte}$$
$$E \simeq m \rightarrow$$
$$\rho_{DM} \simeq mn \propto a^{-3}$$

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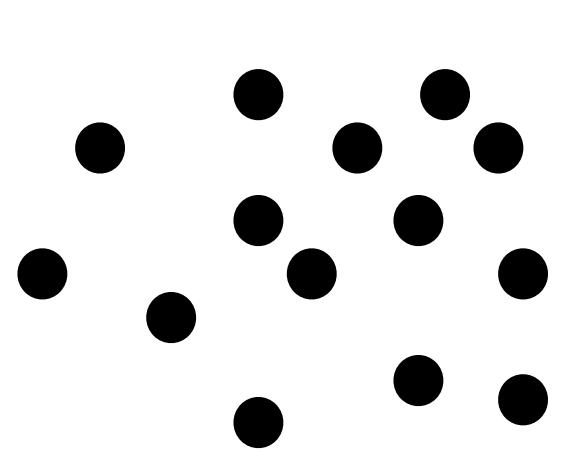
- An alternative scenario: ultralight DM (standard candidates are axion- like particles and dilatons, but can also be vectors or spin 2 tensors).

Very light DM with large $n = \rho_{DM}/m$

Classical field approximation

$$H_{eq} \sim 10^{-28} \text{eV} \ll m < \text{eV}$$

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ULDM as a classical scalar field

(spin 0)

$$S_{DM} = \frac{1}{2} \int d^4x \sqrt{-g} \left[-\partial_\mu \Phi \partial^\mu \Phi - m^2 \Phi^2 \right]$$

Background dynamics

$$ds^2 = -dt^2 + a^2(t) \delta_{ij} dx^i dx^j$$

$$\ddot{\Phi} + 3H\dot{\Phi} + m^2\Phi = 0$$

$$H = \frac{\dot{a}}{a}$$



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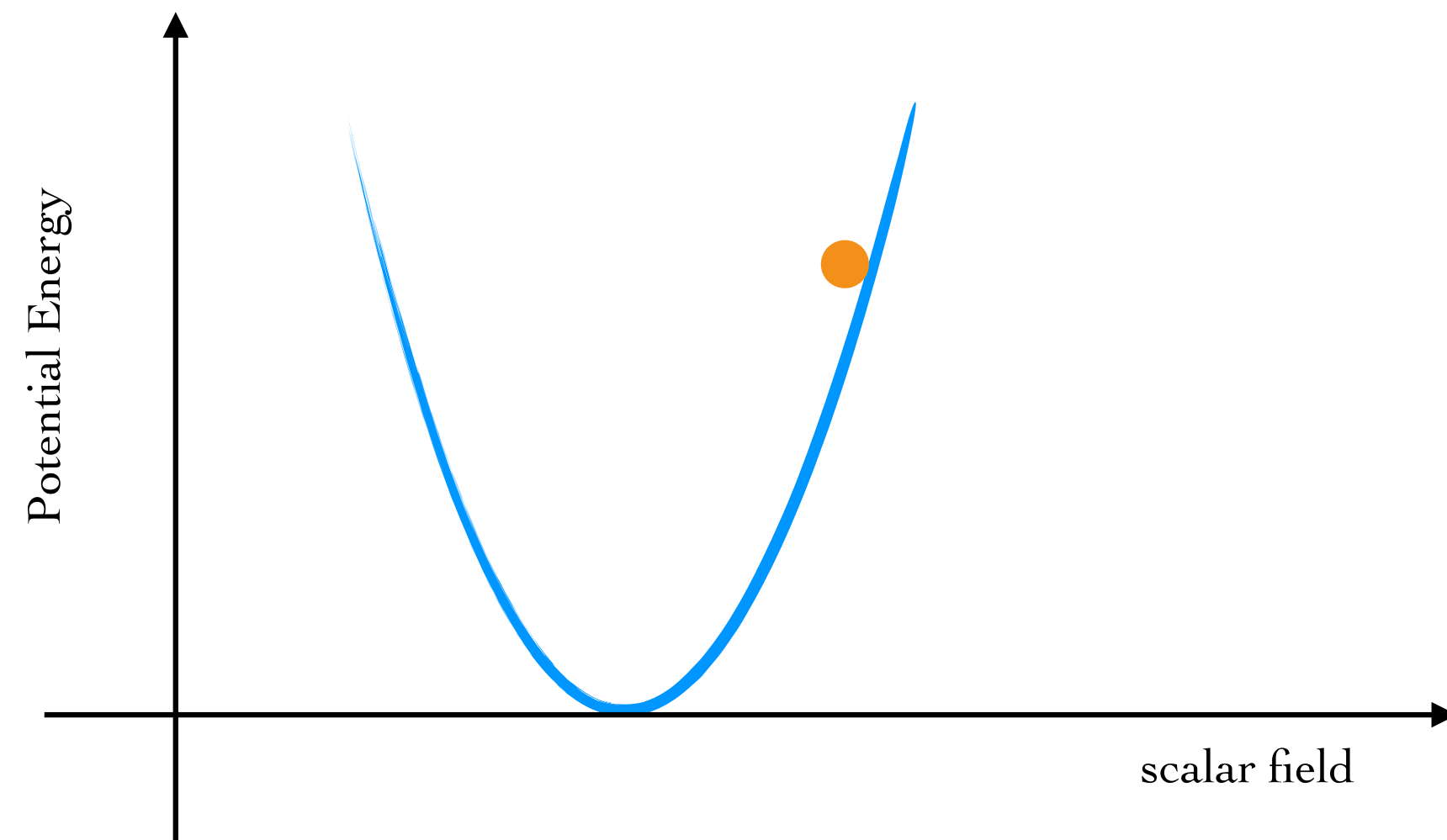
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Initial conditions set by inflation
(very homogeneous)



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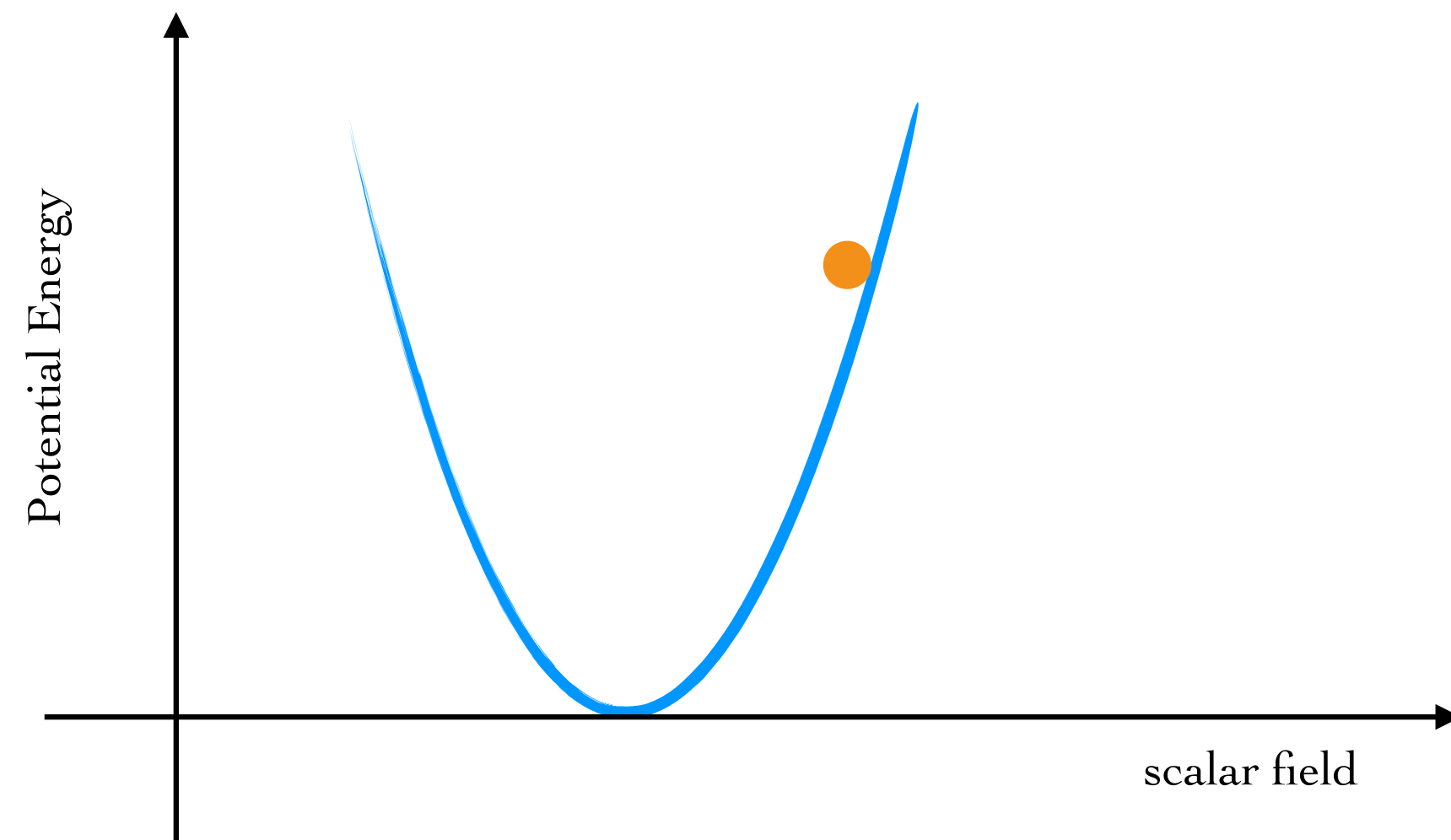
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$$H \gg m \longrightarrow \Phi \simeq \text{constant} \quad p_\Phi \simeq -\rho_\Phi$$

$$H \ll m \longrightarrow \Phi \sim \frac{\Phi_0}{a^{3/2}} \cos(mt + \Upsilon)$$

$$\rho_\Phi \simeq \frac{m^2 \Phi_0^2}{a^3} + \text{oscillations}$$

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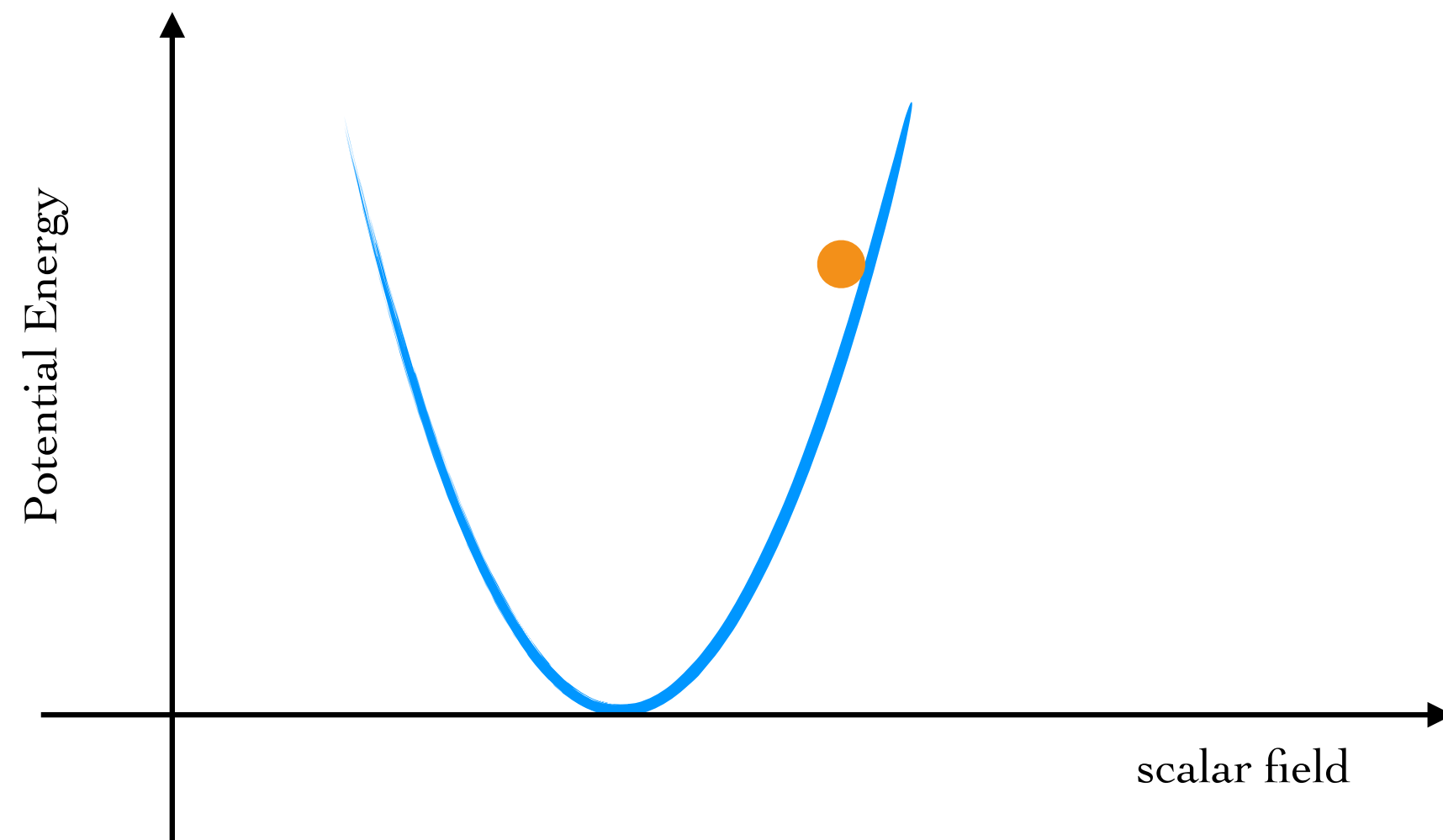
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Similar dynamics can arise for $s=1,2$ on cosmological scales once $H < m$

ULDM as a classical scalar field (on shorter scales)

$$a\dot{\rho}_{DM} \ll c |\nabla \rho_{DM}|$$

Collection of plane waves:

$$\Phi = e^{-ict/\lambda_c} \Psi + e^{ict/\lambda_c} \Psi^*$$

$$\Psi = \sqrt{\frac{c\rho_{DM}(\vec{x}, t)}{2}} \lambda_c \exp \left\{ -i \frac{\pi(\vec{x}, t)}{c\lambda_c} \right\}$$

$$\left(\lambda_c = \frac{\hbar}{mc} \right)$$

Reduced Compton wavelength

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$$|\partial_t \pi|, |\nabla \pi|^2 \ll c^2$$

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Oscillations relevant at time
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$T_{\mu\nu}$

<...> “Fast” oscillations
+ leading order in 1/c
($a = 1$)

$$\langle T_{00} \rangle \simeq c^2 \rho_{DM}$$

$$\langle T_{0i} \rangle \simeq c \rho_{DM} \partial_i \pi \rightarrow v_i = -\partial_i \pi / a$$

$$\langle T_{ij} \rangle \simeq \rho_{DM} \partial_i \pi \partial_j \pi + \frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_j \sqrt{\rho_{DM}}$$

$$- \frac{\delta_{ij}}{2} \left[\frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_i \sqrt{\rho_{DM}} + \rho_{DM} \partial_i \pi \partial_i \pi \right.$$

$$\left. + \rho_{DM} \phi_N - \rho_{DM} \dot{\pi} \right] \quad (\phi_N = c^2 \phi)$$

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$$\langle T_{ij} \rangle \simeq \rho_{DM} \partial_i \pi \partial_j \pi + \frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_j \sqrt{\rho_{DM}}$$

Gradients are relevant at length scales ~ De Broglie length

$$\lambda_{dB} = \frac{c}{v} \lambda_c = \frac{\hbar}{mv}$$

$$- \frac{\delta_{ij}}{2} \left[\frac{\hbar^2}{m^2} \partial_i \sqrt{\rho_{DM}} \partial_i \sqrt{\rho_{DM}} + \rho_{DM} \partial_i \pi \partial_i \pi + \rho_{DM} \phi_N - \rho_{DM} \dot{\pi} \right] \quad (\phi_N = c^2 \phi)$$

$$(\hbar = c = 1)$$

Effective fluid equations for ULDM

$$\nabla_\mu T^{\mu\nu} = 0 \rightarrow$$

$$\frac{1}{a^3} \frac{d}{d\tau} (a^3 \rho_{DM}) + \nabla \cdot (\rho_{DM} \vec{v}) = 0,$$

$$\frac{d}{d\tau} \vec{v} + \mathcal{H} \vec{v} + (\vec{v} \cdot \nabla) \vec{v} = -\nabla \phi_N + \nabla Q$$

“Quantum pressure”

$$Q = \frac{1}{2m^2 a^2} \frac{\nabla^2 \sqrt{\rho_{DM}}}{\sqrt{\rho_{DM}}}$$

$$\nabla \phi_N = 4\pi G a^2 \rho_{DM}$$

$$(\hbar = c = 1)$$

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Jeans suppression

$$\delta''_{DM} + 2\mathcal{H} \delta'_{DM} + \left(\frac{\nabla^4}{4m^2 a^2} - 4\pi G a^2 \bar{\rho}_{DM} \right) \delta_{DM} = 0$$

Using: $a^2 H^2 = \mathcal{H}^2 = 8\pi G \bar{\rho}_{DM}/3$

(MD era, neglecting baryons)

$$\delta''_{DM} + 2\mathcal{H} \delta'_{DM} + \left(\frac{k^4}{6k_J^4} - 1 \right) 4\pi G a^2 \bar{\rho}_{DM} \delta_{DM} = 0$$

$$k_J = a\sqrt{mH}$$

$k > k_J$ Oscillations

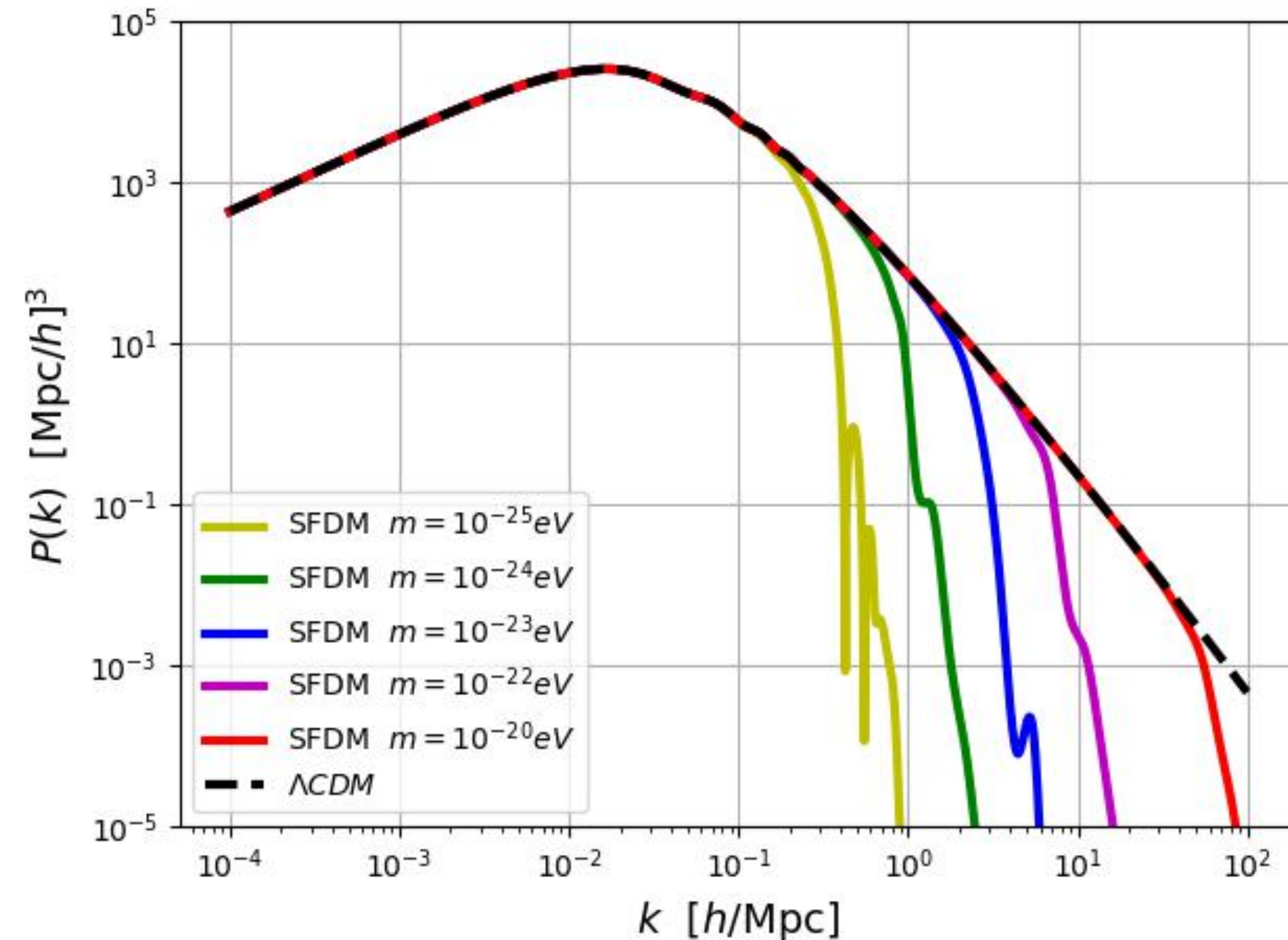
$k < k_J$ Gravitational growth

Scalar Ultralight DM models have been the most studied

- Public codes (e.g. AxionCamb^a, class.FreeSF^b), based on standard CAMB^c or CLASS^d.
- Different predictions from Λ CDM at **small scales**.
- Observables are highly dependant on boson mass.
- Precision cosmological data is used to set constraints on the models, mainly
 - CMB & LSS^e $m \gtrsim 10^{-25}\text{eV}$
 - Lyman-alpha forest^f $m > 2 \times 10^{-20}\text{eV}$

Scalar Ultralight Dark Matter

[Ureña-López & Gonzalez-Morales (2016)]



^aR. Hlozek, et al. 2015; ^bUreña-López&Gonzalez-Morales 2016; ^c<http://camb.info>; ^dhttps://lesgourg.github.io/class_public/class.html

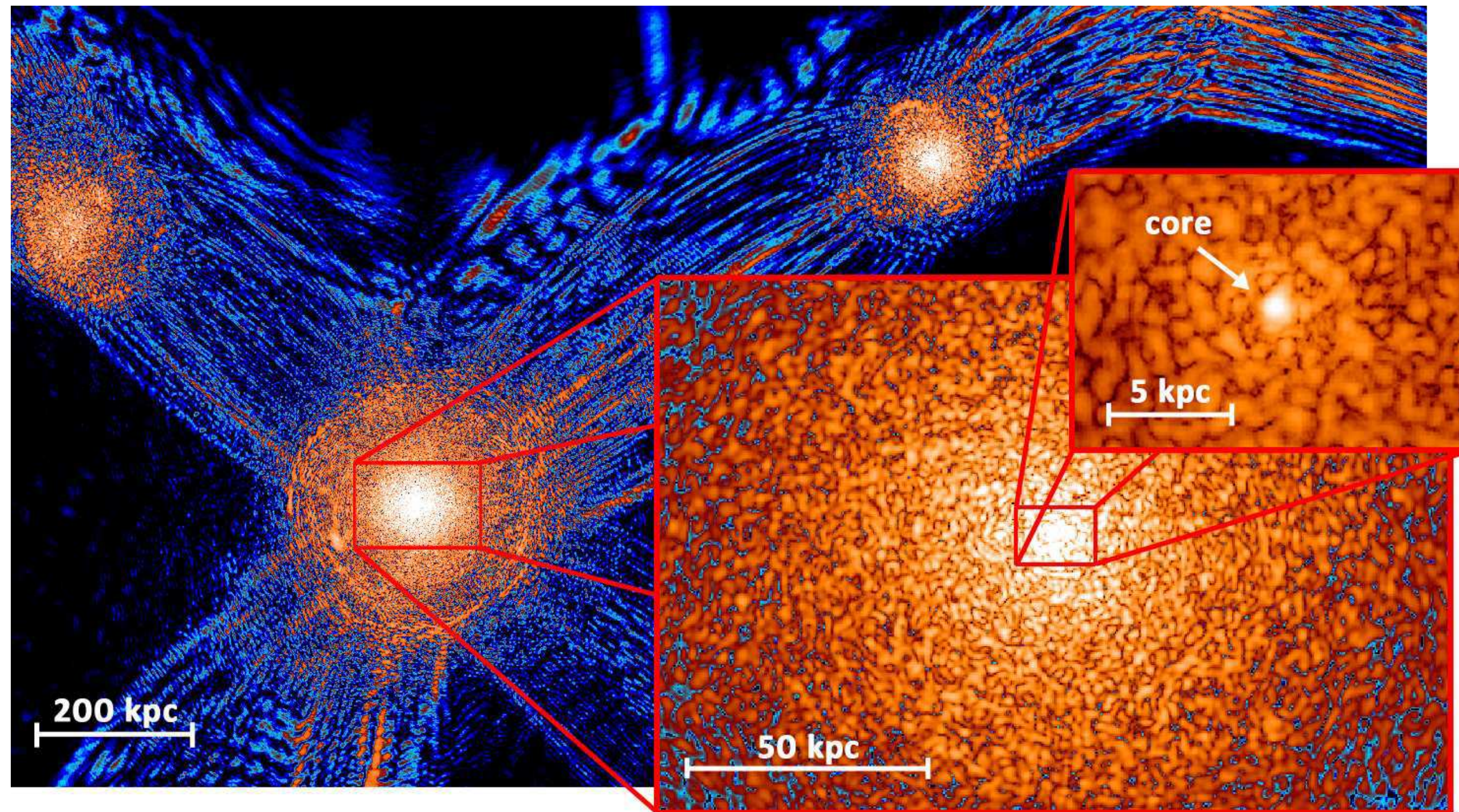
^esee for instance: Hlozek et al MNRAS 2018 & Laguë et al JCAP 2021 ^fRoger&Peiris PRL 2021.

Schrödinger-Poisson equations

$$\frac{i}{a^{3/2}} \frac{\partial}{\partial t} (a^{3/2} \Psi) = \left[\frac{-\nabla^2}{2a^2 m} + m\phi_N \right] \Psi$$

$$\frac{\nabla^2}{a^2} \phi_N = 4\pi G \rho_{\text{DM}} \quad \rho_{\text{DM}} = 2m^2 |\Psi|^2$$

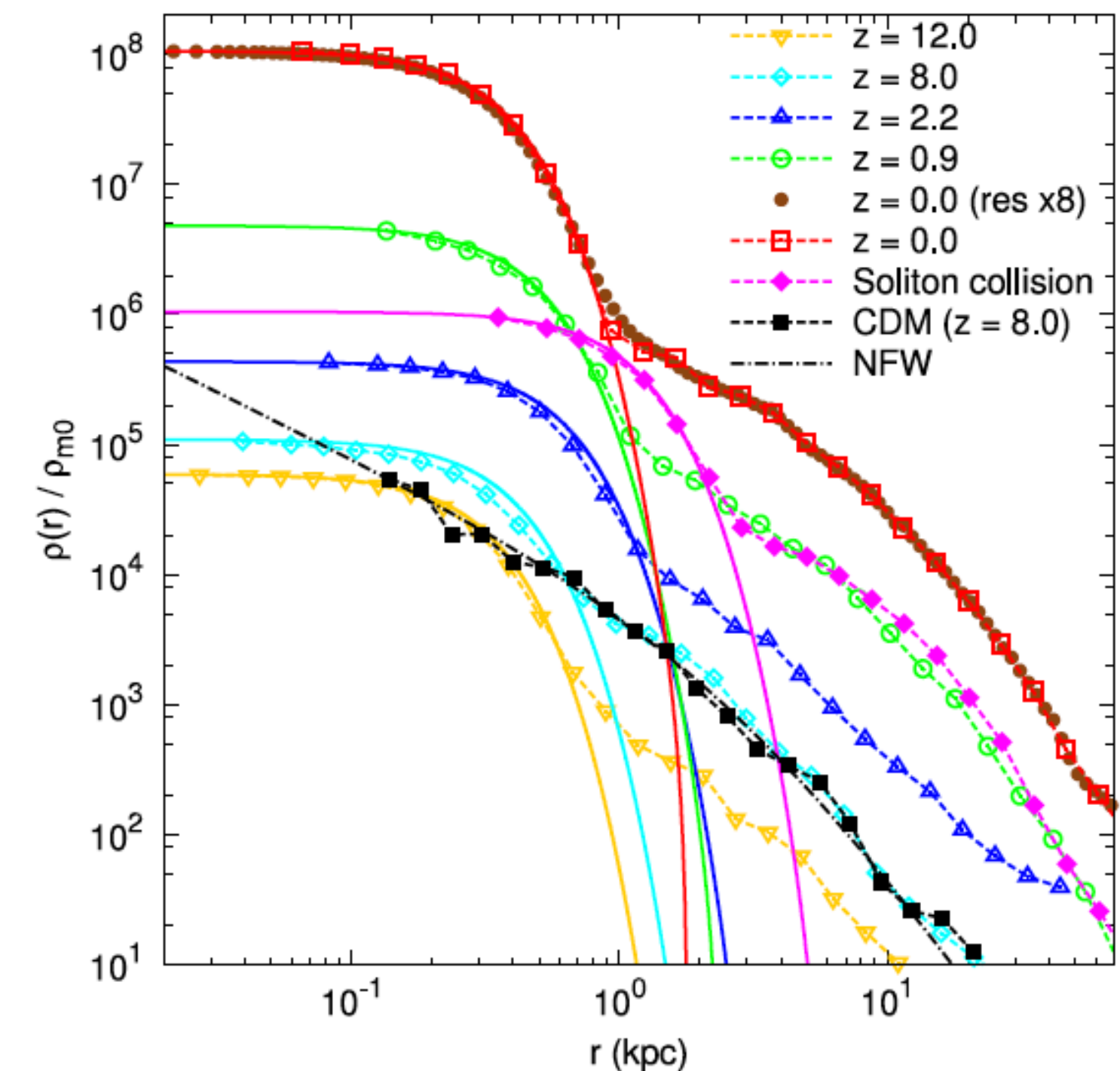
Schive, Chiueh, Broadhurst (2014) $m \sim 10^{-22} \text{eV}$



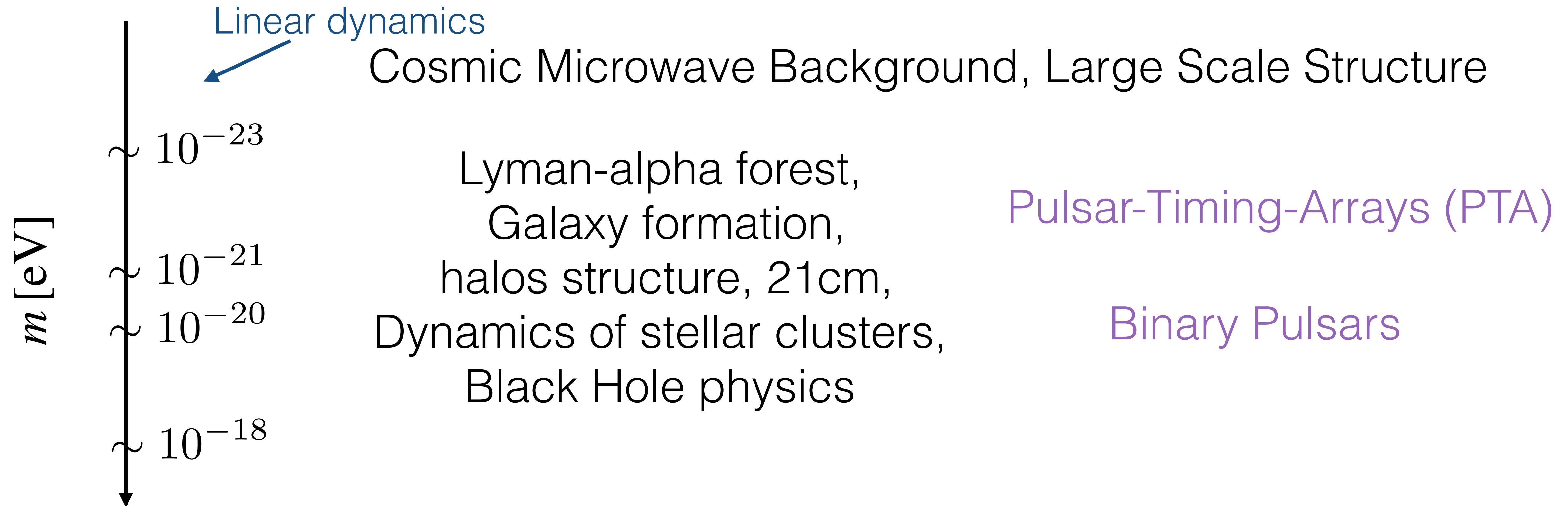
$$\lambda_{dB} = \frac{1}{mv} \sim 10^{16} \text{ km} \left(\frac{10^{-3} c}{v} \right) \left(\frac{10^{-22} \text{eV}}{m} \right)$$

$$\tau_{coh} \sim \frac{\lambda_{dB}}{2v} \sim 6.5 \times 10^5 \text{ years} \left(\frac{10^{-3} c}{v} \right)^2 \left(\frac{10^{-22} \text{eV}}{m} \right)$$

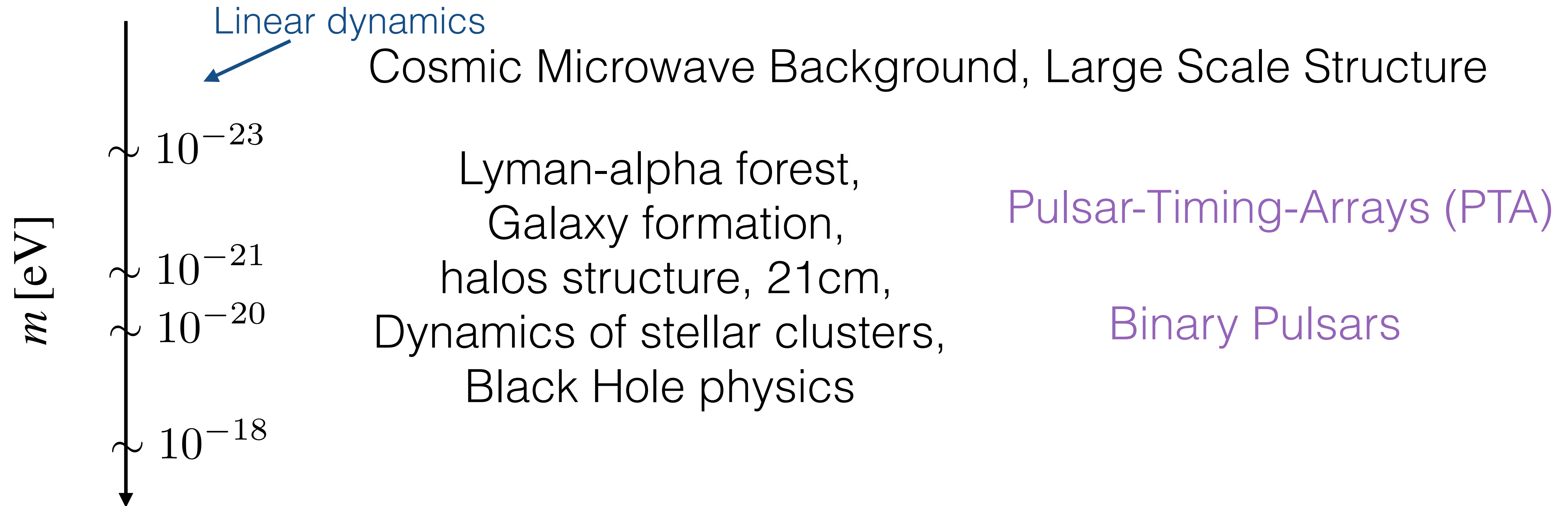
$$\tau_{osc} \simeq \frac{2\pi}{m} \sim 1.3 \text{ years} \left(\frac{10^{-22} \text{eV}}{m} \right)$$



Observation on diverse scales can probe different mass ranges



Observation on diverse scales can probe different mass ranges



- Robustness depends on the observable: theoretical uncertainties, modeling...
- These observations can probe ULDM interacting only through gravity
- If ULDM is directly coupled to the Standard Model -> many other (but model-dependent) possibilities: atomic clocks, accelerometers, resonant-mass detectors, laser and atom interferometry...

Vector Field Dark Matter - Setup

Can different spins of ULDM fields be distinguished on cosmological scales?

(*) *Based on:*

- Ferreira Chase and DLN, [Phys. Rev. D 109, 083521 \(2024\)](#)
- Ferreira Chase, Leizerovich, DLN, Landau, [arXiv:2408.12052](#)

Codes available at:

<https://github.com/classULDM/class.SFDM> (Spin 0) <https://github.com/classULDM/class.VFDM> (Spin 1)

Vector Field Dark Matter - Setup

Goals

- **Cosmological perturbations** with VFDM.
- **Anisotropic background metric.**
- Calculate cosmological **observables**.

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$$S = S_{Gravity} + S_{SM} - \int d\tau dx^3 \sqrt{-g} \left[\frac{1}{4} F^{\mu\nu} F_{\mu\nu} + \frac{m^2}{2} A^\mu A_\mu \right]$$
$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi G (T_{\mu\nu}^{Matter} + T_{\mu\nu}^A)$$
$$\nabla^\mu T_{\mu\nu}^{Matter} = 0$$
$$\nabla_\nu F^{\mu\nu} + m^2 A^\mu = 0$$
$$F_{\mu\nu} = \nabla_\mu A_\nu - \nabla_\nu A_\mu$$

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Anisotropic background dynamics

Conformal time

- Bianchi I metric:

$$ds^2 = a(\tau)^2 \left[-d\tau^2 + \gamma_{ij} dx^i dx^j \right]$$

$$dt = a d\tau$$

Metric shear:

$$\sigma_{ij} = \frac{1}{2} \gamma'_{ij}$$

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- SM & Λ :

$$P_I = w_I \rho_I$$

$$I = \Lambda, r, b$$

$$P'_I = -3\mathcal{H}(P_I + \rho_I)$$

$$\left(\mathcal{H} = \frac{a'}{a} = aH \right)$$

$$w_\Lambda = -1, w_r = 1/3, w_b = 0$$

Hubble rate

Anisotropic background dynamics

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$T^{A\mu}_\nu \rightarrow$ fluid variables: $\rho_A, P_A, \Sigma^{Aj}_i =$ traceless part of T^{Ai}_j

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$$\text{We assume: } A_i(\tau) = A(\tau) \hat{A}_i \quad \& \quad \rho_A(t_0) = \rho_{DM}(t_0)$$

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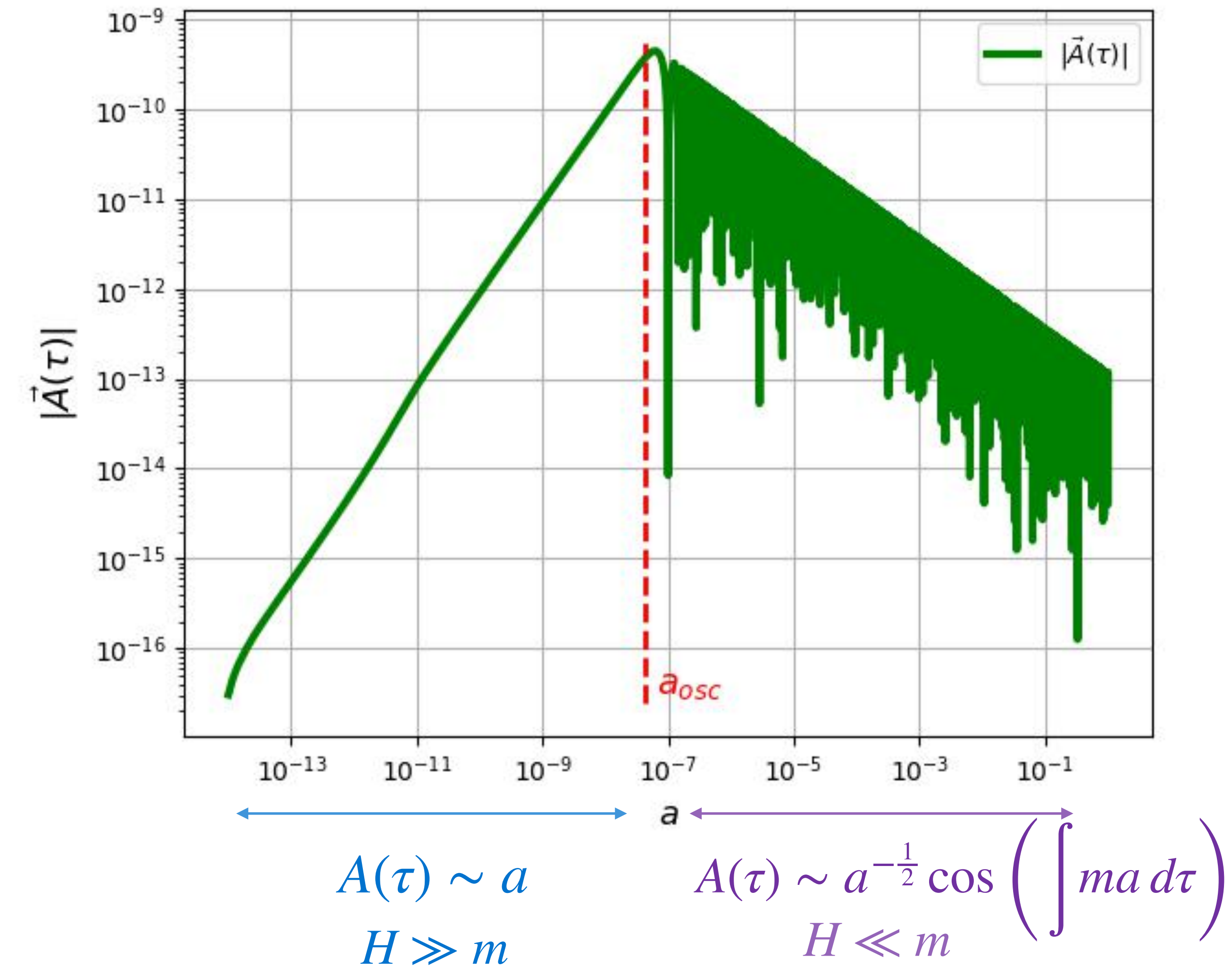
We solve perturbatively in the shear $|\sigma_{ij}| \ll \mathcal{H}$

Background evolution - VFDM

(Here and below we use Planck 2018 parameters)

$$A_i(\tau) = A(\tau) \hat{A}_i \quad \& \quad \rho_A(t_0) = \rho_{DM}(t_0)$$

$$\mathcal{H}(a_{osc}) = ma_{osc} \quad (H(a_{osc}) = m)$$



Background evolution - VFDM

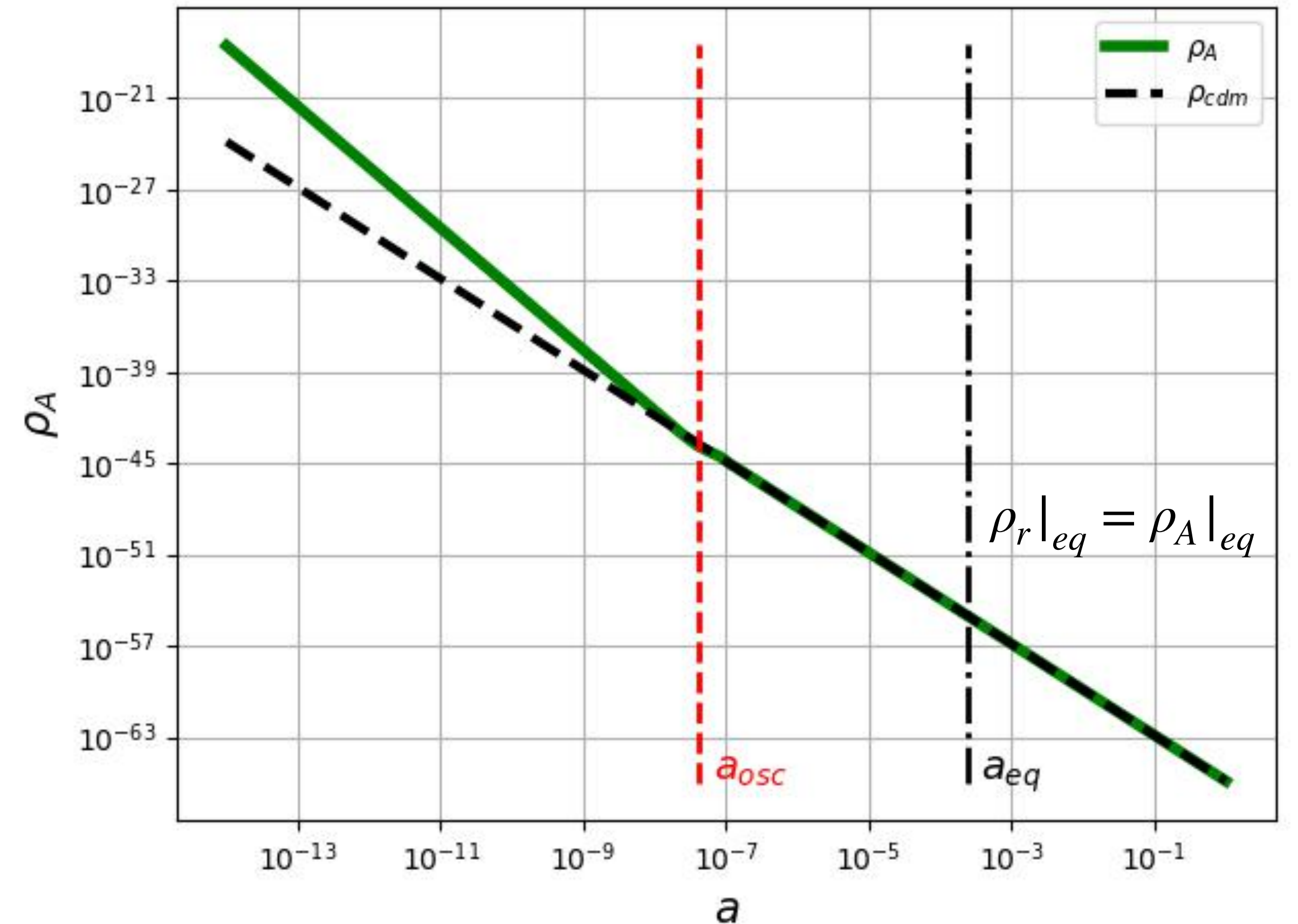
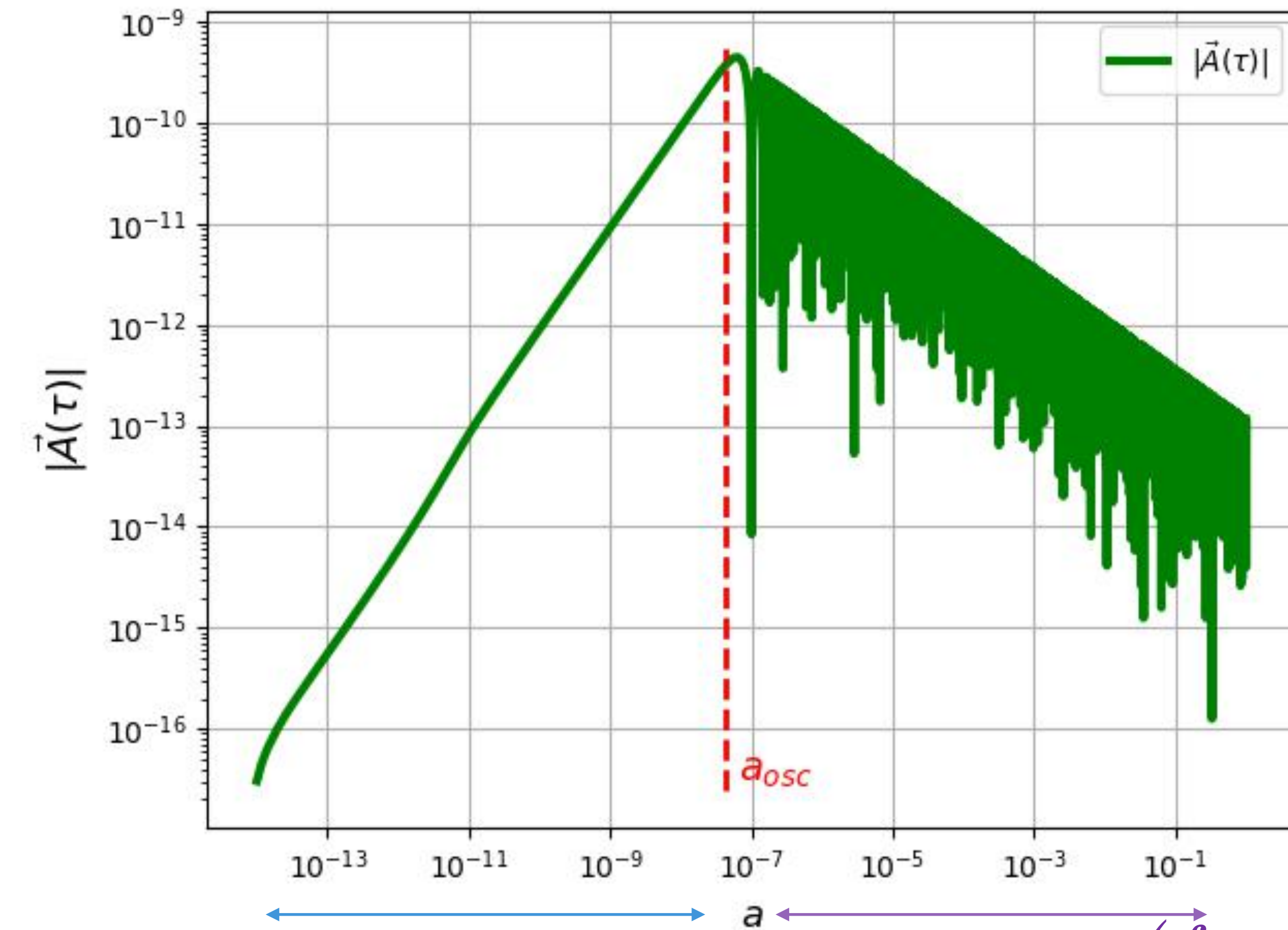
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$$H_{eq} \sim 10^{-28} \text{eV} \ll H(a_{osc}) = m$$

$$\rho_A \sim a^{-4}, P_A = \rho_A/3 \quad \rho_A \sim a^{-3}, \langle P_A \rangle \simeq 0$$



$$A(\tau) \sim a$$

$$H \gg m$$

$$A(\tau) \sim a^{-\frac{1}{2}} \cos \left(\int m a d\tau \right)$$

$$H \ll m$$

$$\Sigma_{ij}^A \simeq -2\rho_A \left(\hat{A}_i \hat{A}_j - \frac{\gamma_{ij}}{3} \right)$$

$$\langle \Sigma_{ij}^A \rangle \simeq 0$$

Background evolution - Einstein eqns and shear abundance

$$\mathcal{H}^2 - \frac{1}{6}\sigma^2 = \frac{a^2}{3m_P^2} \left(\sum_{I=\Lambda, r, b} \rho_I + \rho_A \right) \quad (\sigma^i_j)' + 2\mathcal{H} \sigma^i_j = \frac{a^2}{m_P^2} \Sigma^A{}^i_j$$

Shear abundance:

$$\Omega_\sigma = \frac{\sigma^2}{6\mathcal{H}^2} \quad (\sigma^2 = \sigma^{ij}\sigma_{ij})$$

Background evolution - Einstein eqns and shear abundance

$$\mathcal{H}^2 - \frac{1}{6}\sigma^2 = \frac{a^2}{3m_P^2} \left(\sum_{I=\Lambda, r, b} \rho_I + \rho_A \right) \quad (\sigma^i_j)' + 2\mathcal{H} \sigma^i_j = \frac{a^2}{m_P^2} \Sigma^A{}^i_j$$

Shear abundance:

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For $a_{\text{ini}} \ll a \ll a_{\text{osc}}$:

$$\sigma_{ij} \simeq -6R_A \mathcal{H} \left(\hat{A}_i \hat{A}_j - \frac{\gamma_{ij}}{3} \right), \quad R_A = \frac{\rho_A}{\rho_r} \ll 1 \quad (\text{RD})$$

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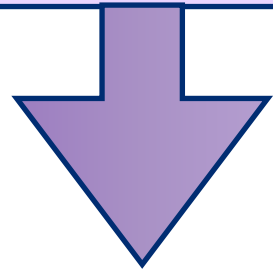
For $a_{\text{osc}} \ll a$ ($H \ll m$) $\rightarrow \langle \Sigma^{Aj}_i \rangle \simeq 0$

Background evolution - BBN constrains

$$\Omega_\sigma \propto \begin{cases} m^{-1} & a < a_{osc} \\ a^{-2} & a_{osc} < a < a_{eq} \\ a^{-3} & a_{eq} < a \end{cases}$$

BBN constrains [Akarsu et al 2019]

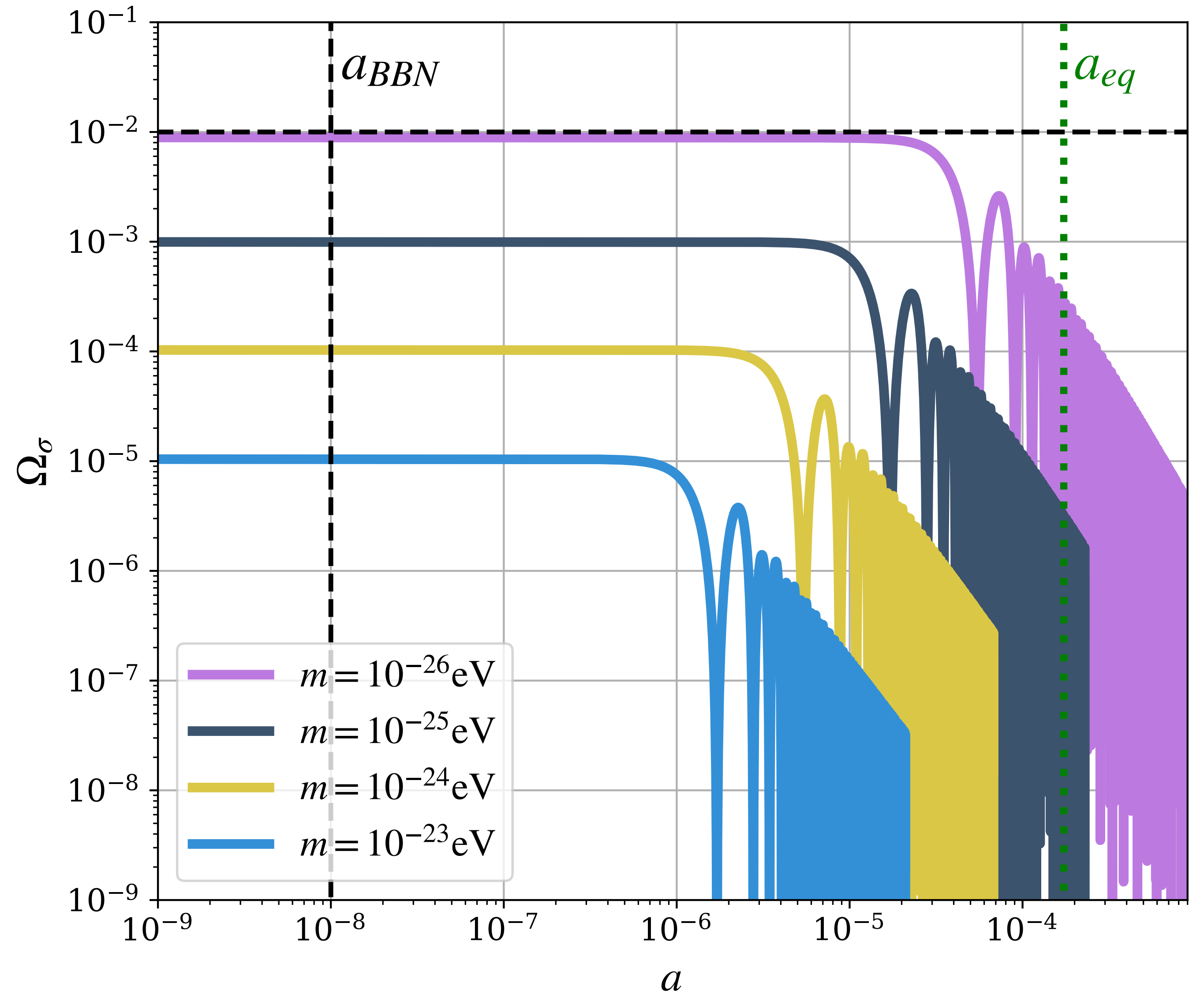
$$\Omega_\sigma|_{BBN} \lesssim 10^{-2}$$



$$m \gtrsim 10^{-26} \text{eV}$$

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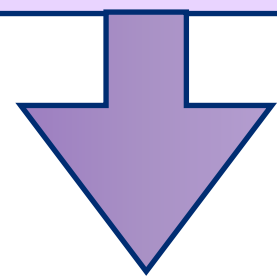


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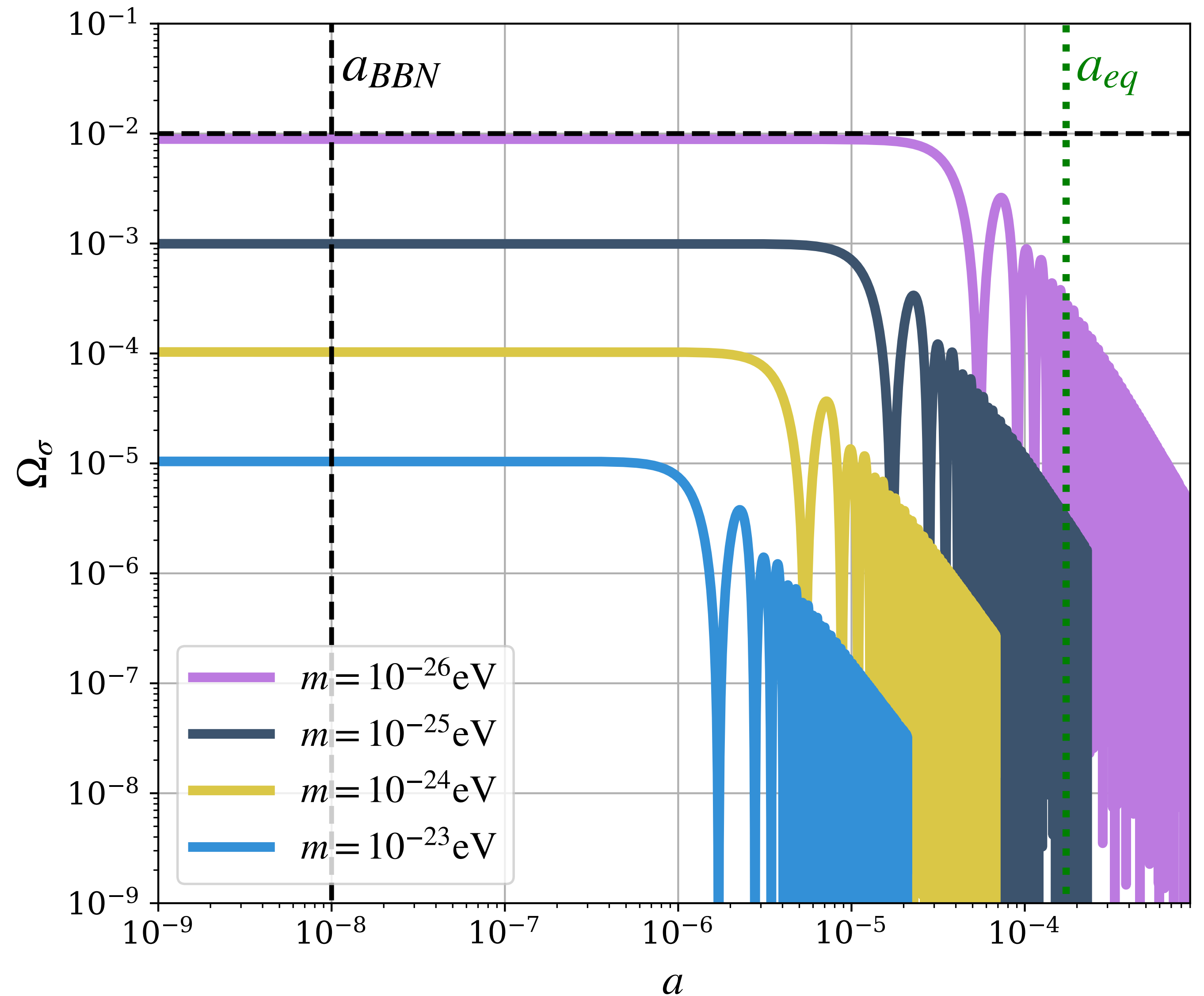


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We expect stronger bounds from the analysis of the perturbations....

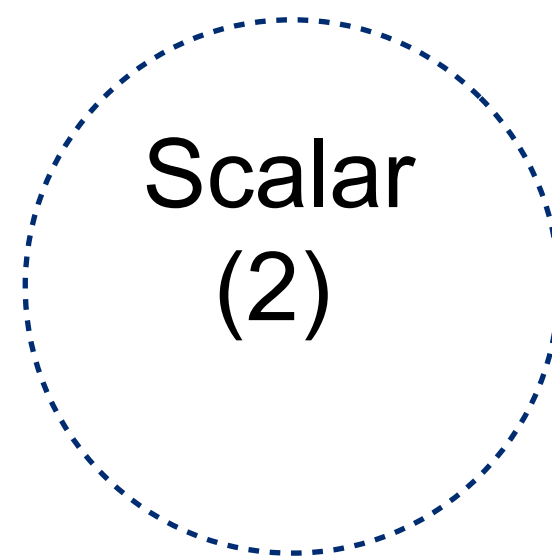
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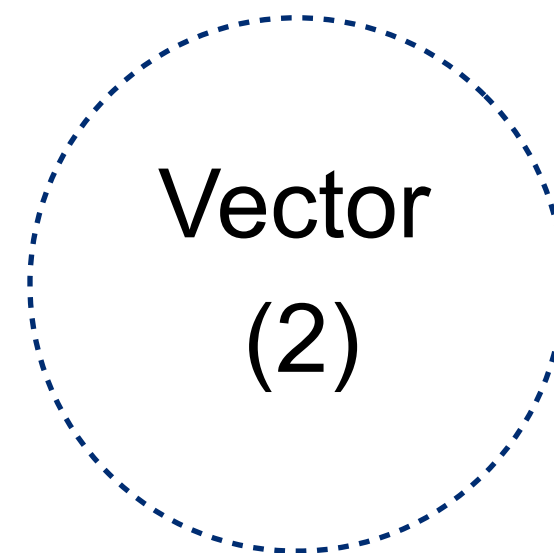
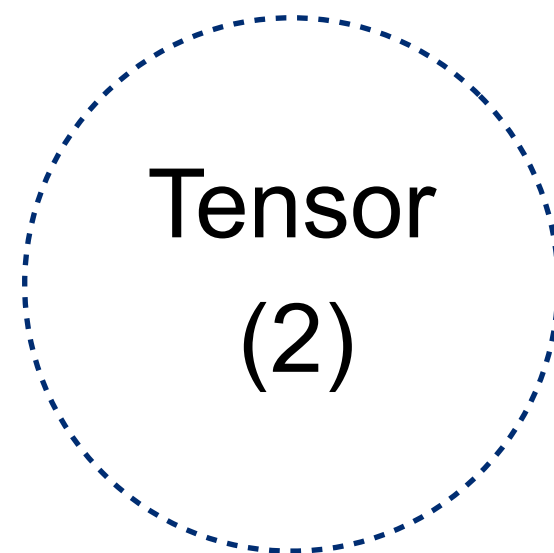


Scalar-Vector-Tensor decomposition

Isotropic FLRW background

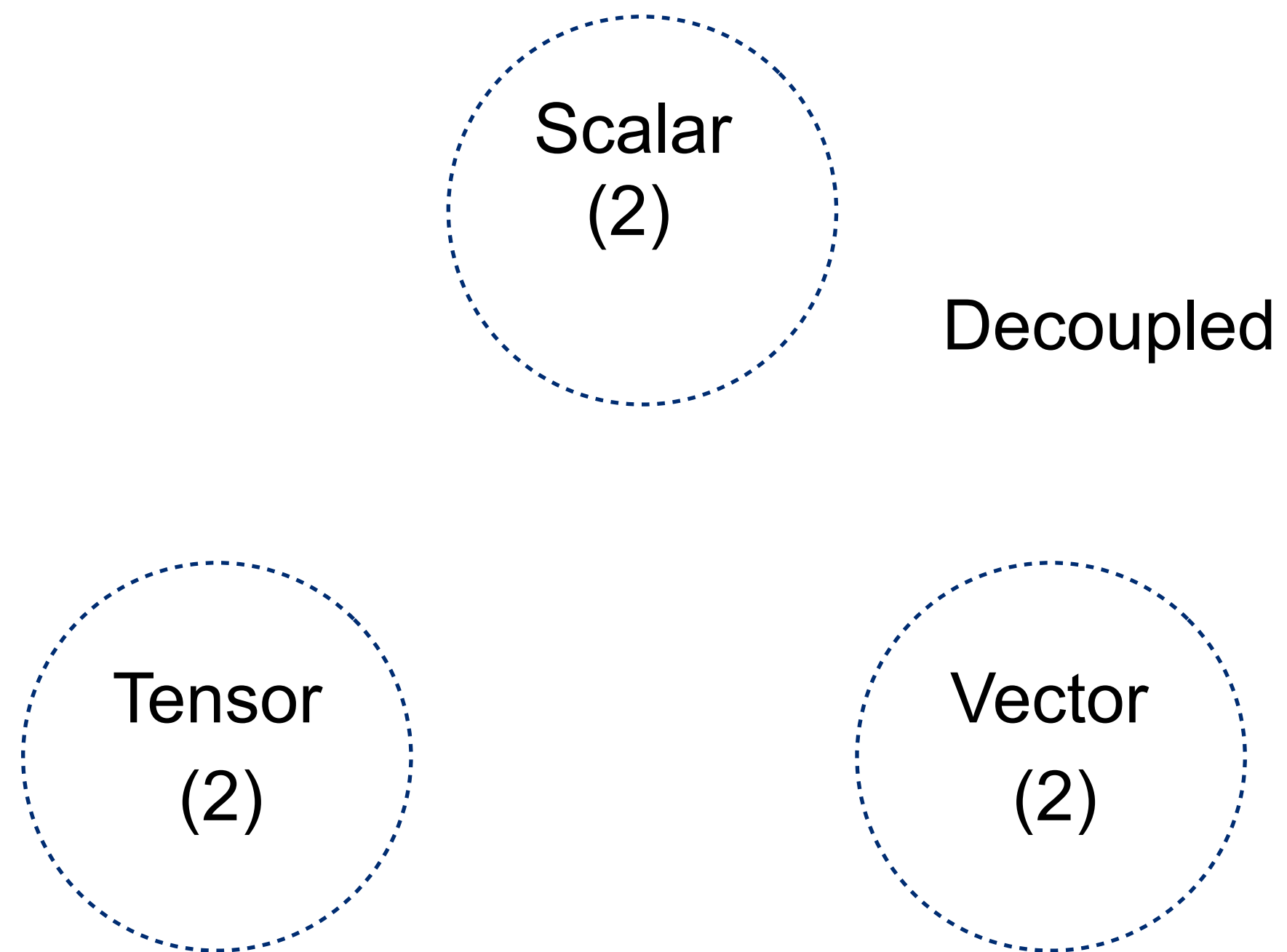


Decoupled

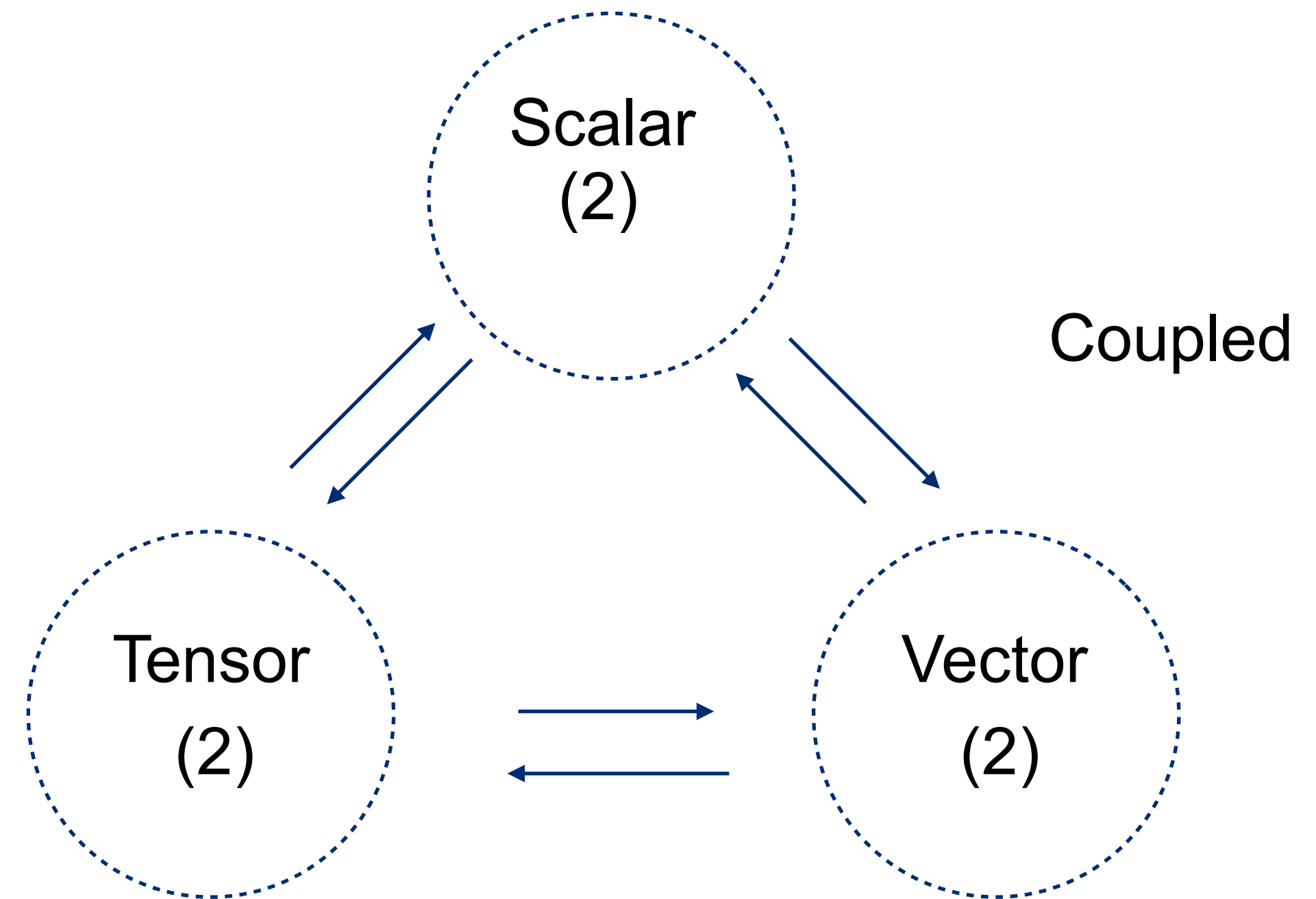


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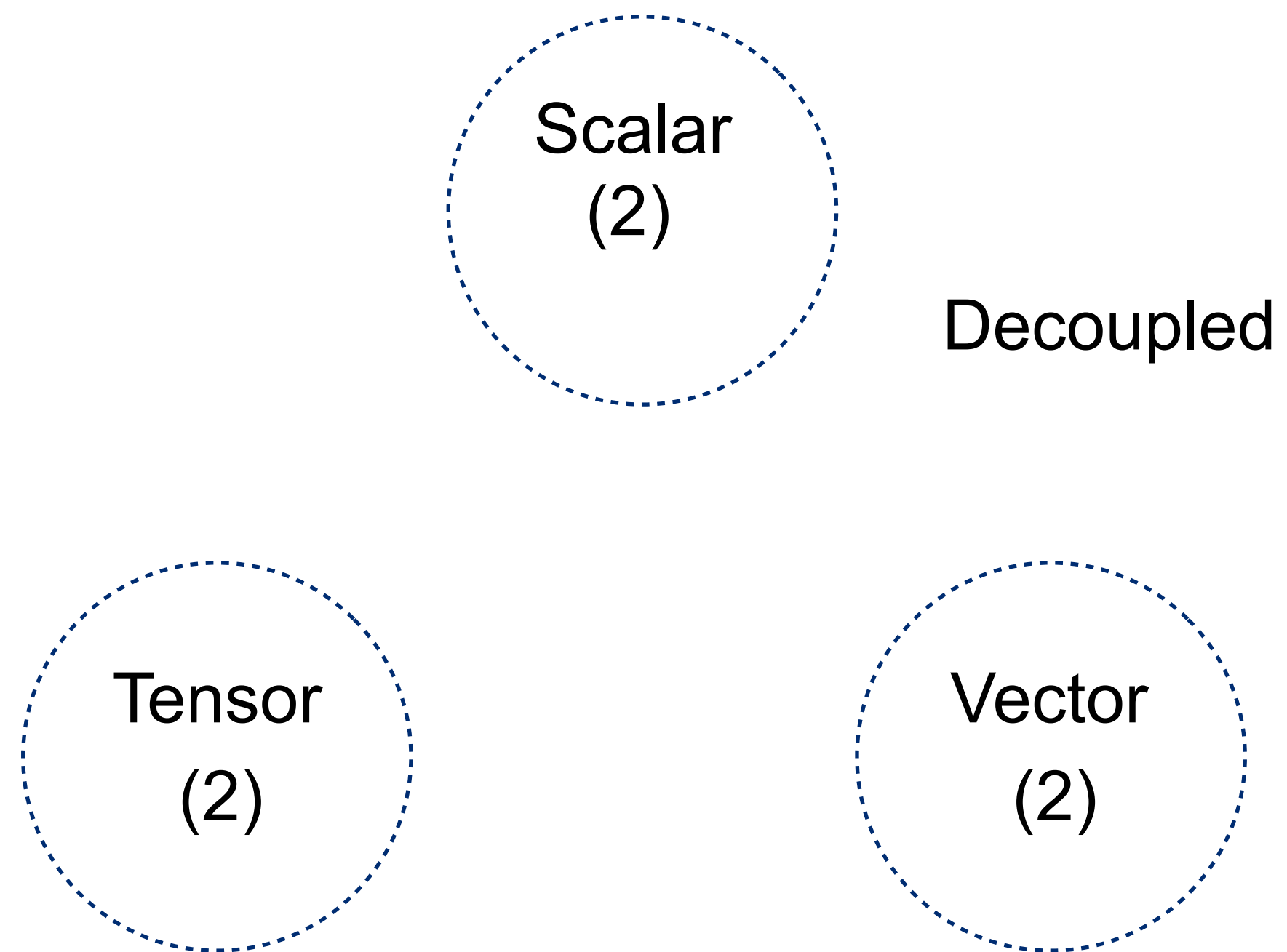


Anisotropic background

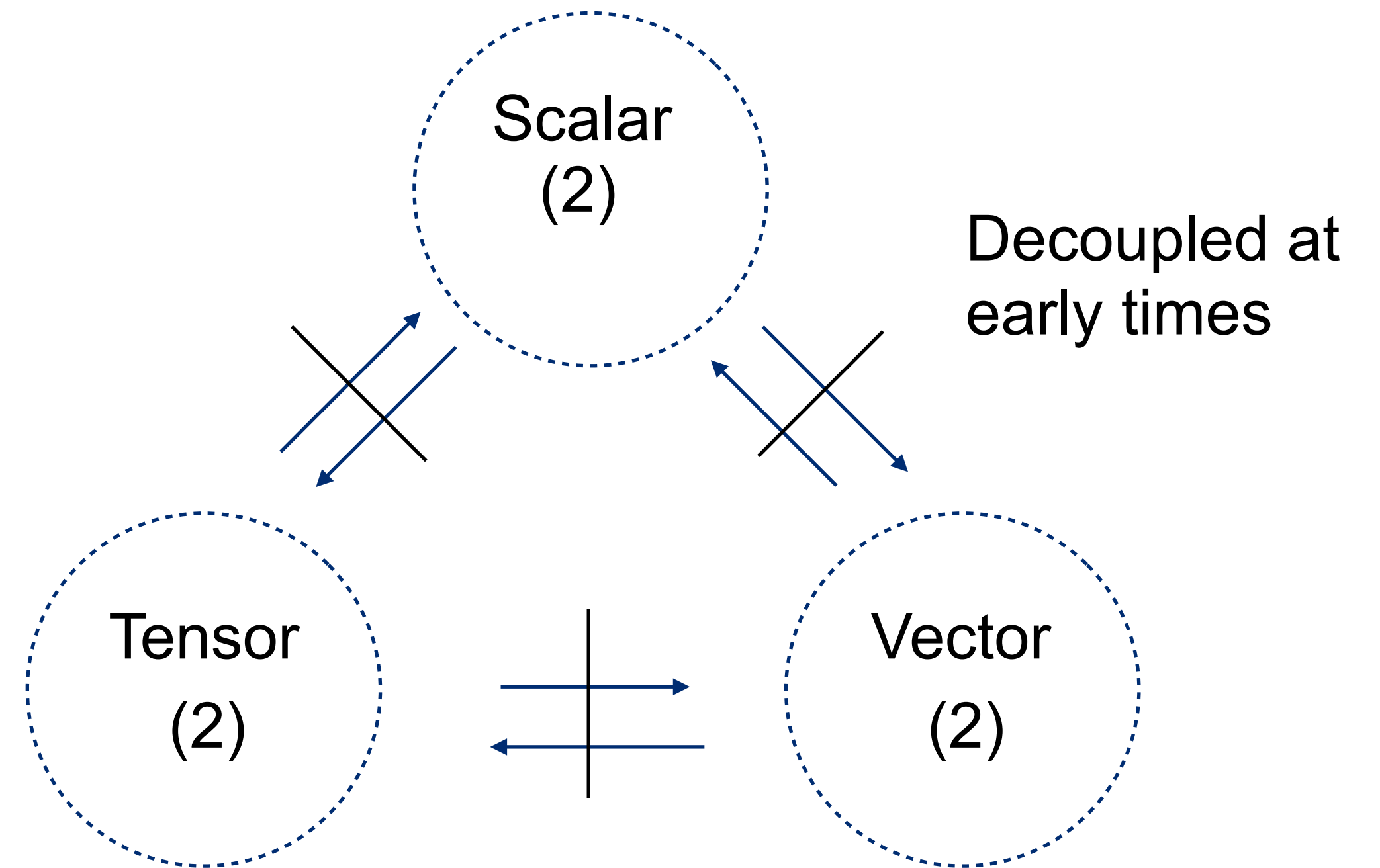


Scalar-Vector-Tensor decomposition

Isotropic FLRW background



Anisotropic background



Linear regime - Scalar sector

- **Cosmological perturbation theory:** $S(\tau, \vec{x}) = S(\tau) + \delta S(\tau, \vec{x})$

Vector Field: $A_i(\tau, \vec{x}) = A(\tau)\hat{A}_i + \delta A_i(\tau, \vec{x})$

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- **Linearized Einstein eqns. in Fourier space:** $\delta G^\mu{}_\nu = 8\pi G \delta T^\mu{}_\nu$

$$\delta G^\mu{}_\nu = \delta G^\mu{}_\nu(\delta g_{00}, \delta g_{i0}, \delta g_{ij}) \qquad \delta T^\mu{}_\nu = \delta T^\mu{}_\nu(\delta \rho, \delta P, \delta \Sigma_j^i)$$

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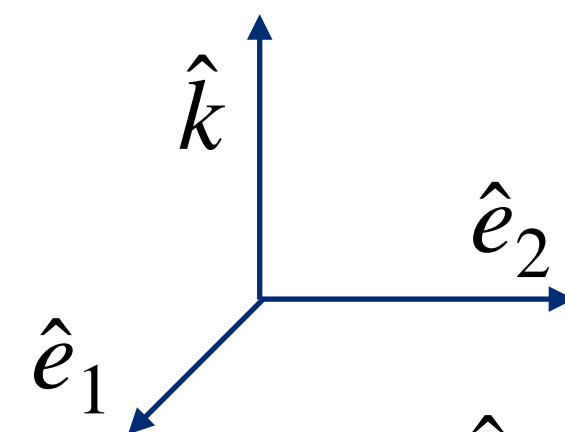
Synchronous gauge:

$$\delta g_{00} = \delta g_{0i} = 0$$

Two scalar perturbations

$$\delta g_{ij} = a^2 \left[-2 \left(\gamma_{ij} + \frac{\sigma_{ij}}{\mathcal{H}} \right) \eta + \hat{k}_i \hat{k}_j (h + 6\eta) \right]$$

Orthogonal basis



$$\hat{e}_1 = \hat{k} \times \hat{e}_2$$

$$\hat{e}_2 = \hat{k} \times \hat{A}$$

Newtonian gauge:

Two scalar perturbations

$$\delta g_{00} = -2a^2\phi, \quad \delta g_{0i} = 0, \quad \delta g_{ij} = -2a^2 \left(\gamma_{ij} + \frac{\sigma_{ij}}{\mathcal{H}} \right) \psi$$

Adiabatic initial conditions (IC) during radiation domination (RD) era: Synchronous gauge

- Imposed when $k\tau \ll 1$
($k \ll \mathcal{H}$, $k/a \ll H$)

$$\delta G_{\nu}^{\mu} = 8\pi G \delta T_{\nu}^{\mu}$$

$$\frac{\delta\rho_I}{\rho_I'} = \frac{\delta\rho_{\gamma}}{\rho_{\gamma}'}$$

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$\mathcal{O}(k^4)$ $\mathcal{O}(k^2)$ $\mathcal{O}(k^4)$

Exactly cancel

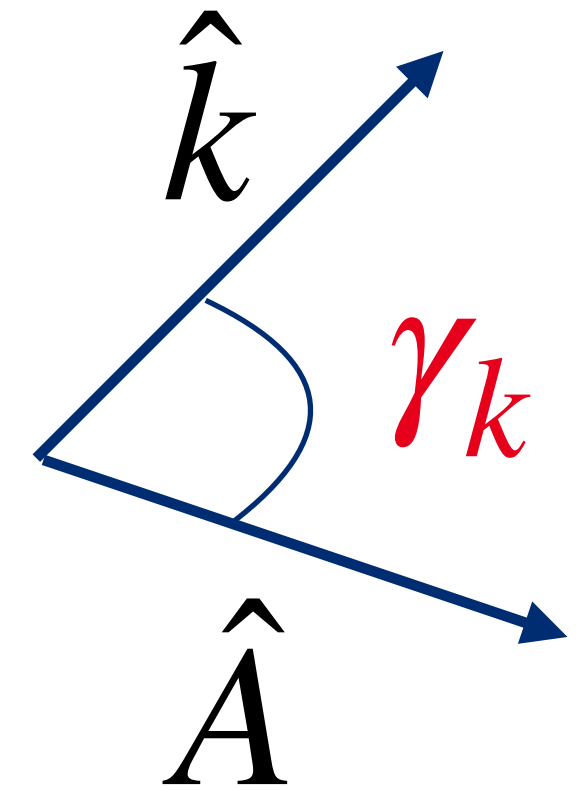
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For attractor adiabatic IC $\delta \vec{A} = A' \left[2(\hat{A} \cdot \hat{k}) \hat{k} - (\hat{e}_1 \cdot \hat{k}) \hat{e}_1 \right] \tau \eta_0 \rightarrow \delta T^0_{Ai} = -\frac{3m_P^2}{a^2} k^2 \sigma_{\parallel} \tau$

Matter Power spectra - Implementation in CLASS

$$\langle \delta(\tau, \vec{k}) \delta^*(\tau, \vec{k}') \rangle = (2\pi)^3 \delta^3(\vec{k} - \vec{k}') P_\delta(k, \gamma_k)$$

$\delta = \delta\rho/\rho$

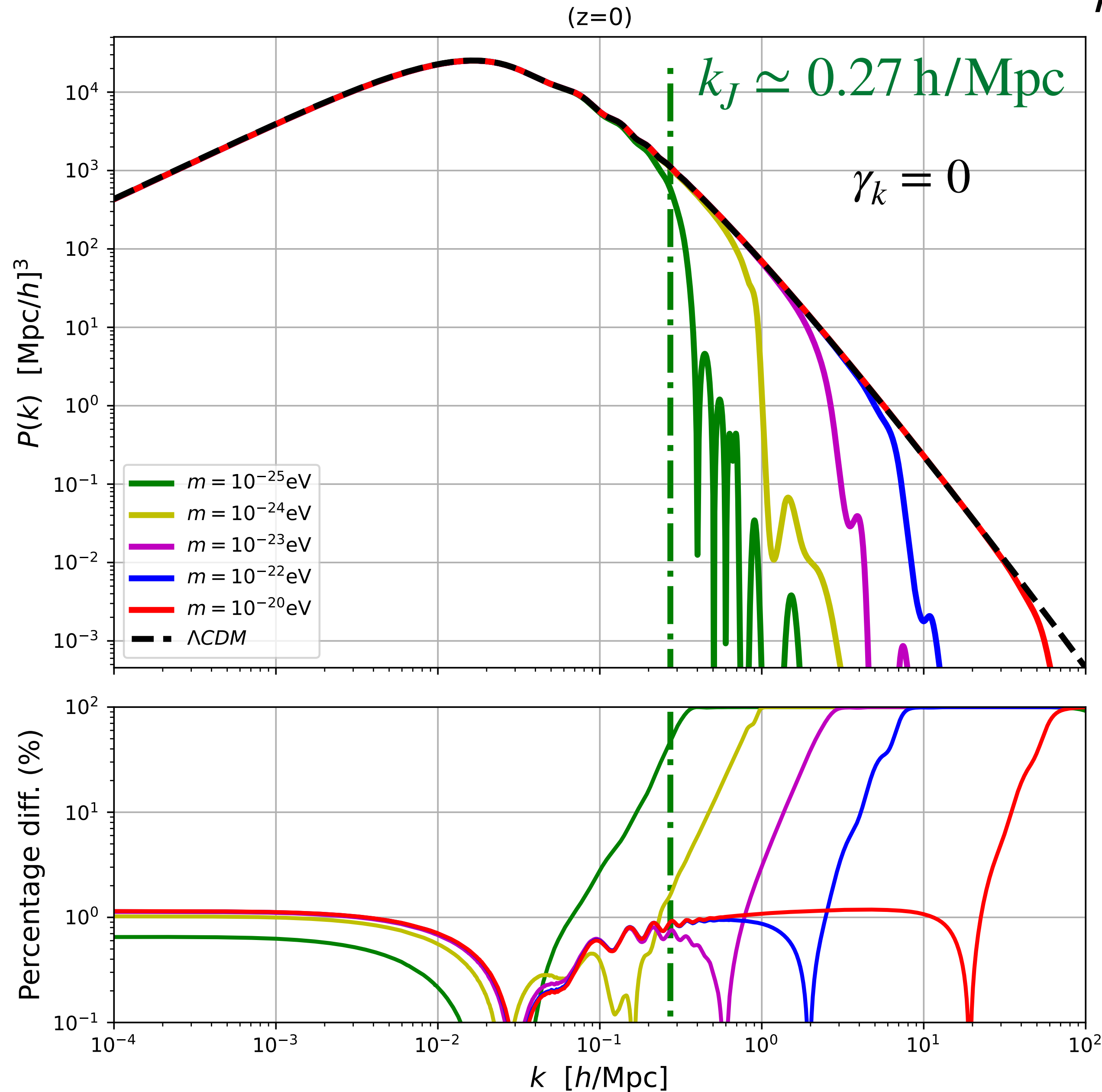


CLASS

- Assumes **background isotropy** $\vec{k} \rightarrow k$
- **Solves for** the evolution of each k

We implemented the equations in CLASS- we can solve them for any γ_k -

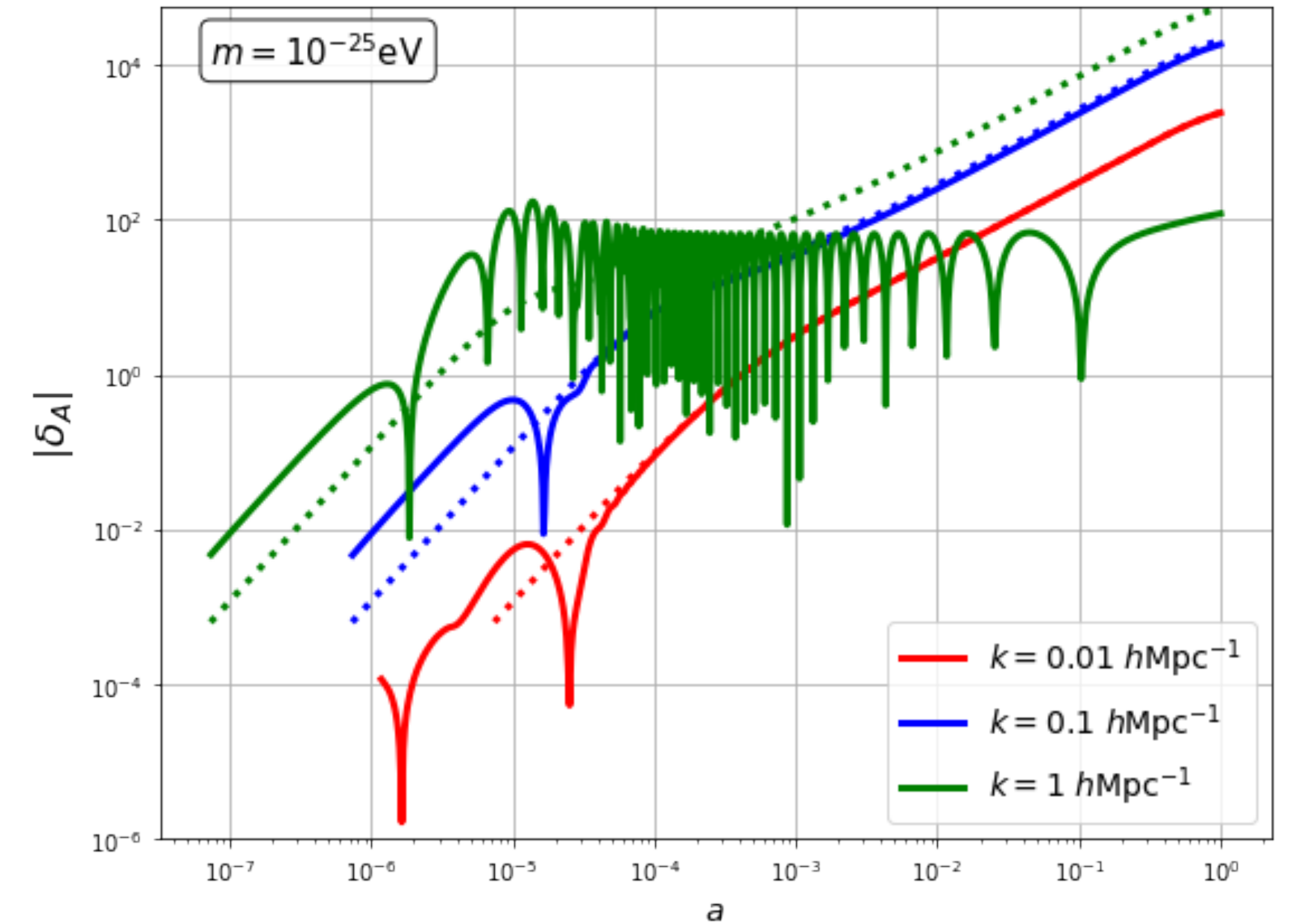
Matter Power spectra



Combining Einstein & VFDM equations in MD for $k \gg \mathcal{H}$:

$$\delta_A'' + \frac{\delta_A'}{2} + \left(\frac{k^4}{k_J^4} - \frac{3}{2} \right) \delta_A = 2 \frac{k^2}{\mathcal{H}^2} \eta$$

$$k_J = \sqrt{ma\mathcal{H}} \begin{cases} k \gg k_J \rightarrow \delta_A \sim \text{oscillate} \\ k \ll k_J \rightarrow \delta_A \sim a \end{cases}$$



Code available at: <https://github.com/classULDM/class.VFDM>

The Jeans wavevector

$$k_J = \sqrt{ma\mathcal{H}} = a\sqrt{mH}$$

$$k_J \propto \begin{cases} \sim \text{constant} & \text{RD } (a < a_{eq}) \\ \sim a^{1/4} & \text{MD } (a > a_{eq}) \end{cases}$$

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- Modes with $k = k_J$ enter the horizon in RD when the field starts oscillating, that is

$$k = \mathcal{H}_* = \sqrt{ma_*\mathcal{H}_*} \rightarrow ma_* = \mathcal{H}_* \rightarrow a_* = a_{osc} \quad (\text{note } k = ma_*)$$

Horizon crossing
at $a = a_*$

k_J

Condition for the field to start oscillating

The Jeans wavevector

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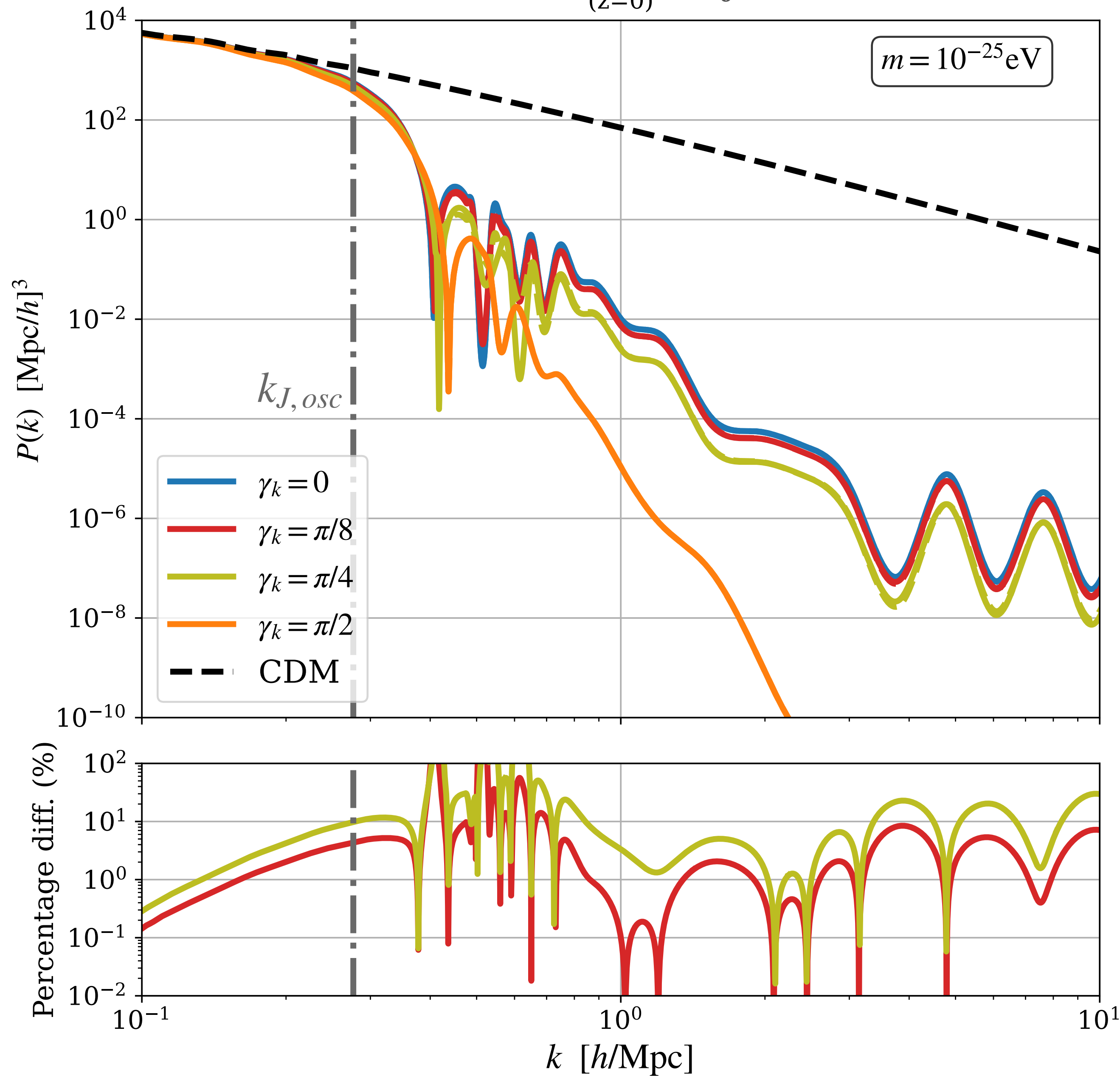
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Horizon crossing at $a = a_*$ k_J Condition for the field to start oscillating

- Modes with $k < k_J$ ($k > k_J$) enter the horizon being non-relativistic ($k < ma_*$) (relativistic $k > ma_*$)

Angular dependence

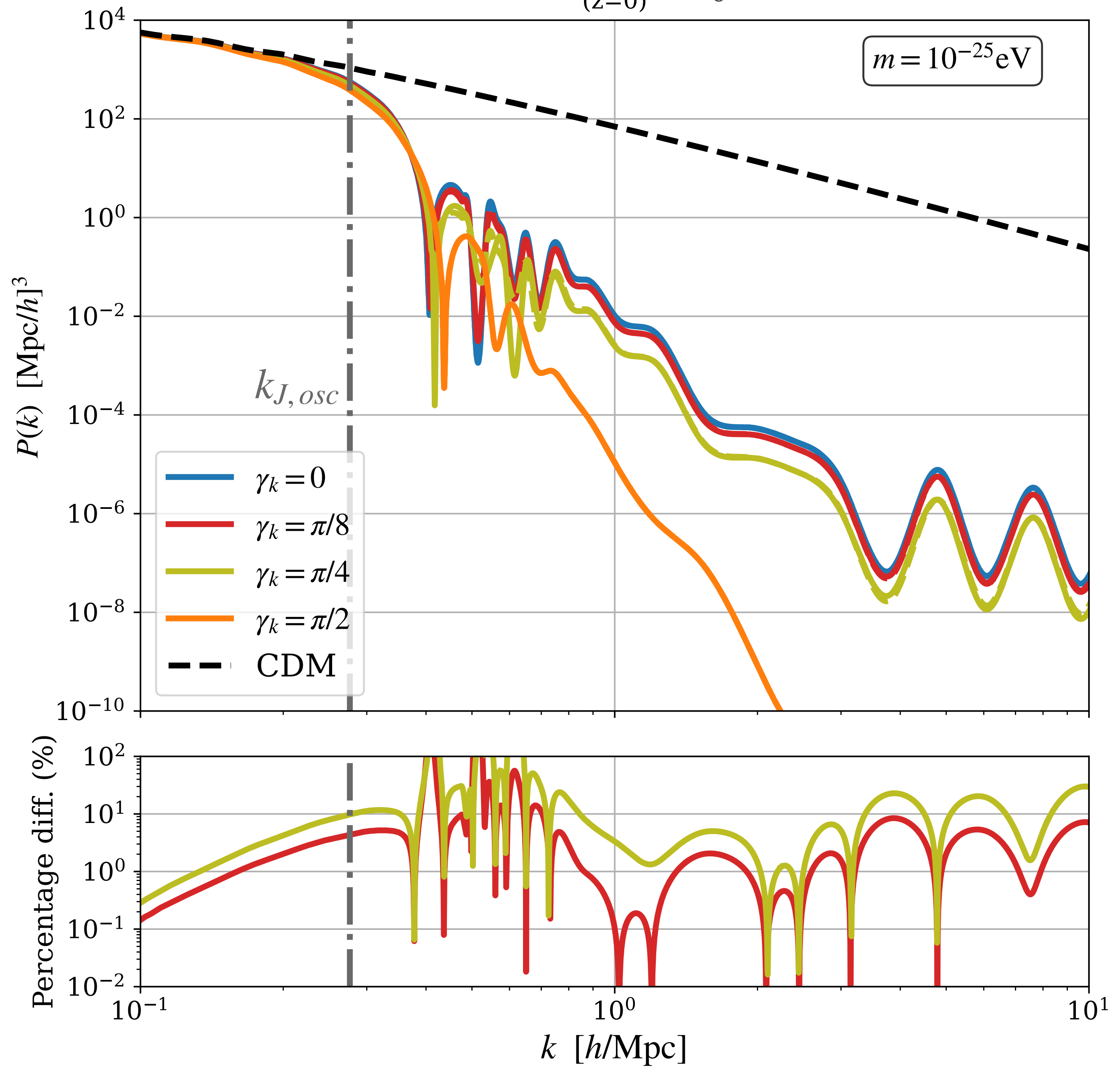
$(z=0) \quad k_J \simeq 0.27 \text{ h/Mpc}$



$$\% \text{Diff} = 100 \times \left(\frac{P(k, \gamma_k) - P(k, 0)}{P(k, 0)} \right)$$

Angular dependence

$k_J \simeq 0.27 \text{ h/Mpc}$



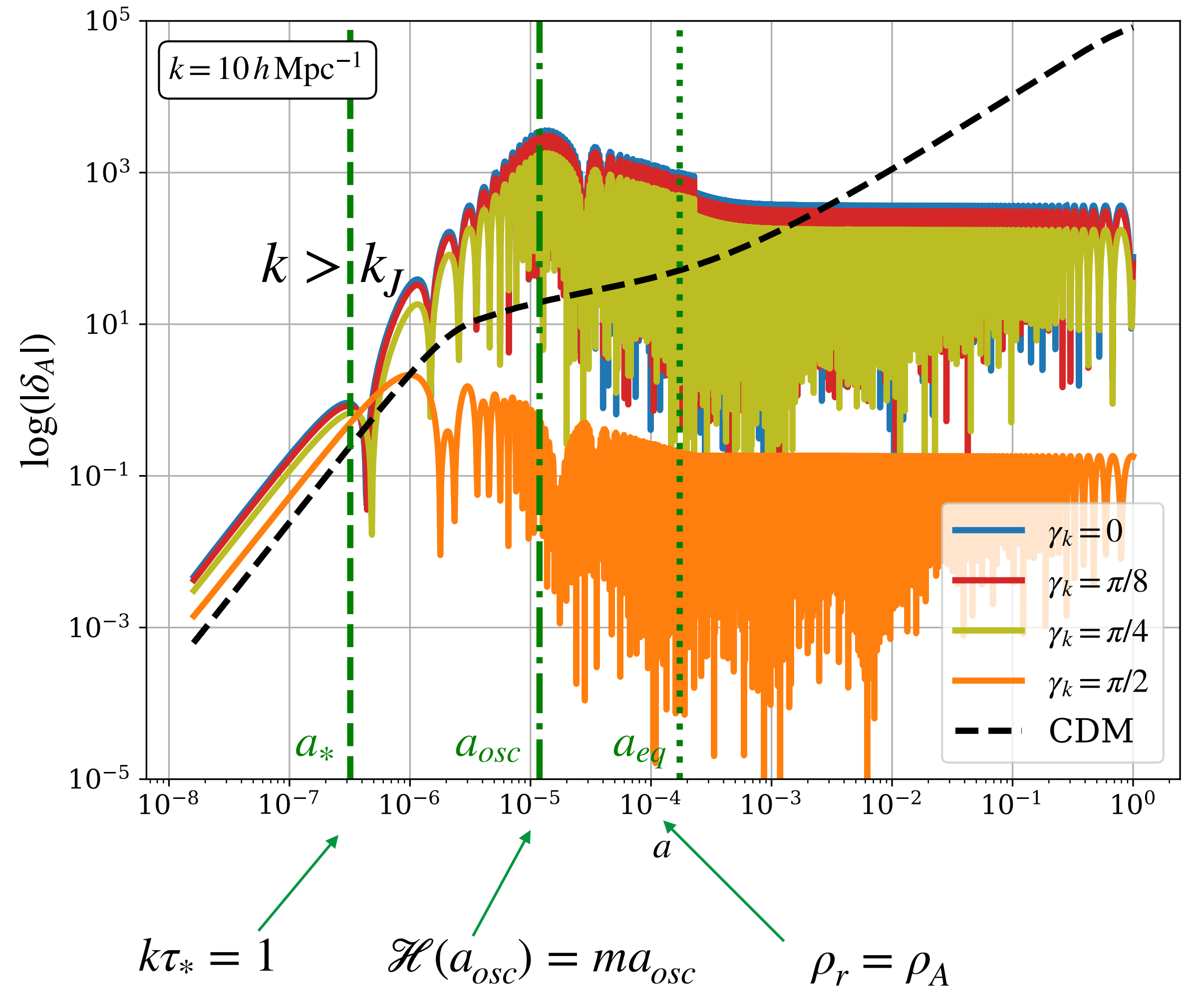
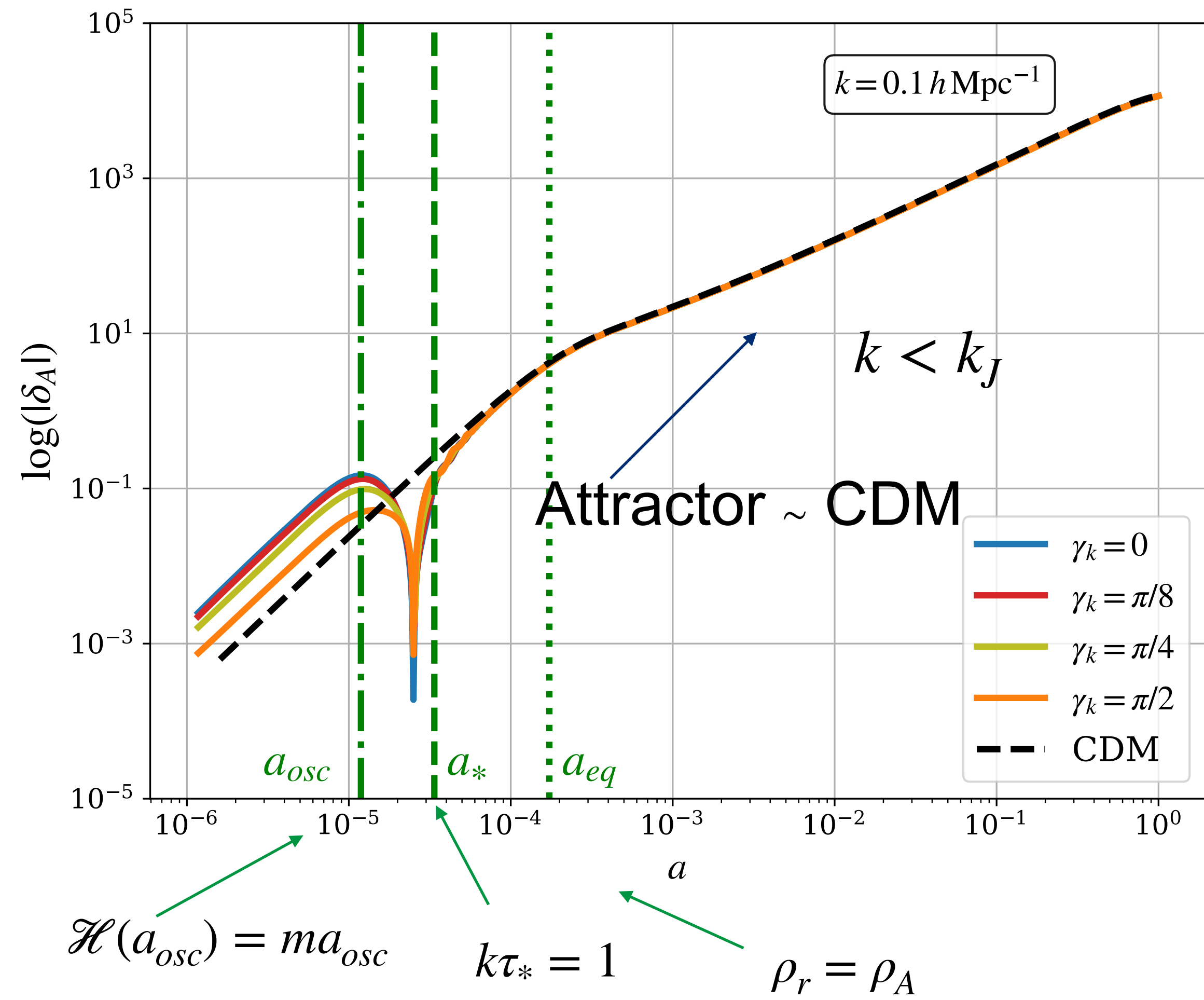
Parametrization

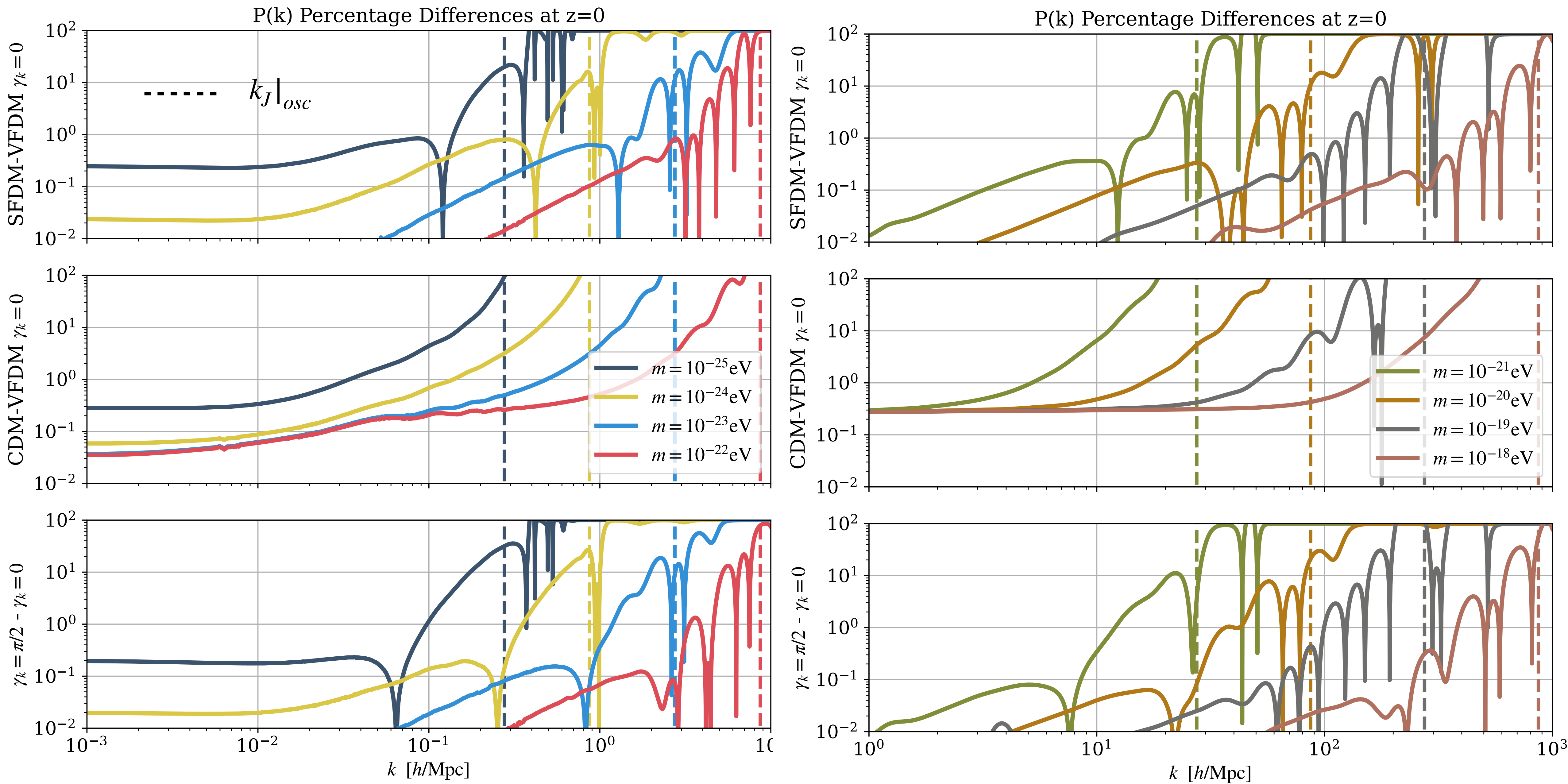
$$P(k, \gamma_k) = P(k, \frac{\pi}{2}) (1 - g(k) \cos(\gamma_k)^4)$$

$$g(k) = 1 - P(k, 0) / P(k, \frac{\pi}{2})$$

$$\% \text{Diff} = 100 \times \left(\frac{P(k, \gamma_k) - P(k, 0)}{P(k, 0)} \right)$$

Angular dependence





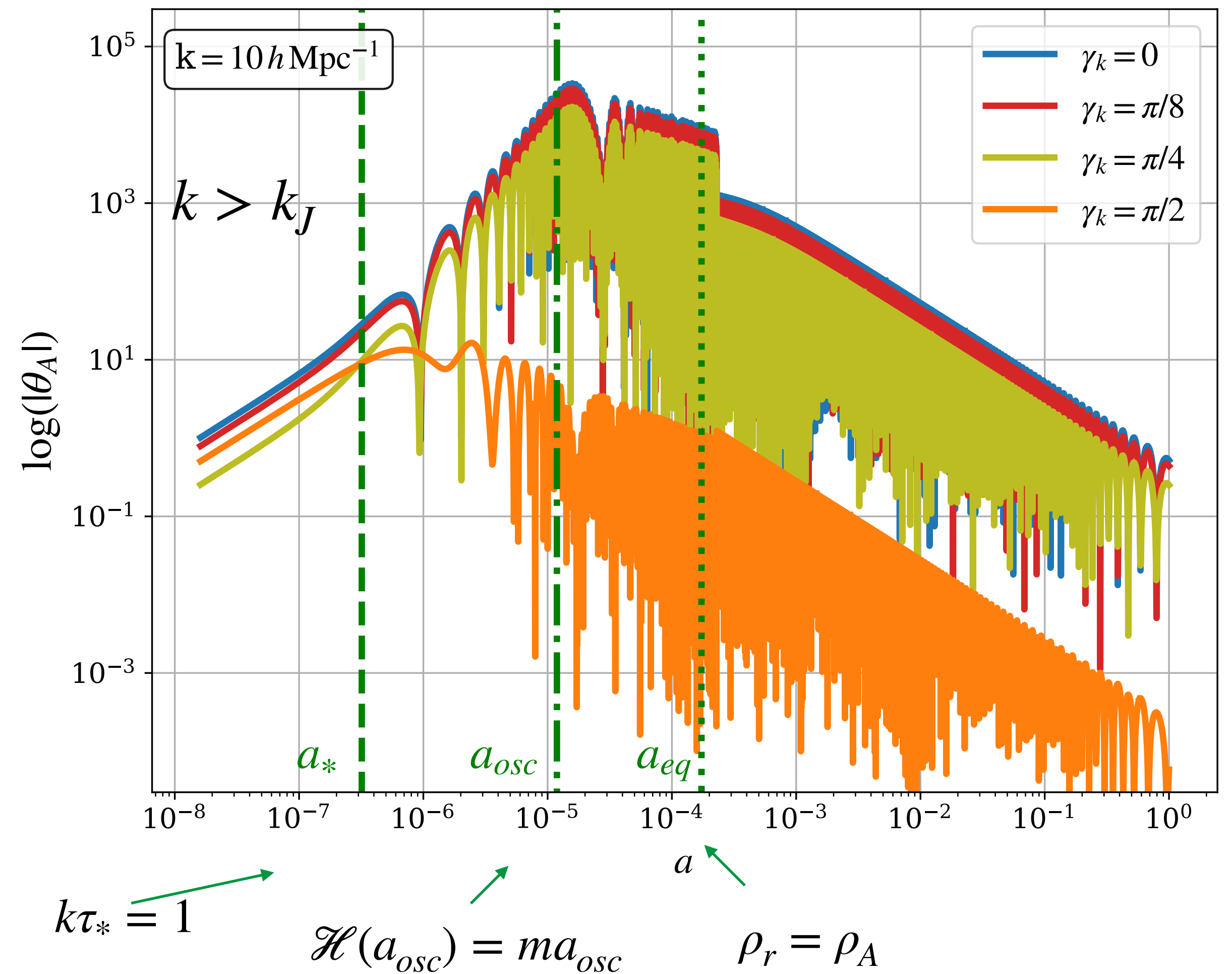
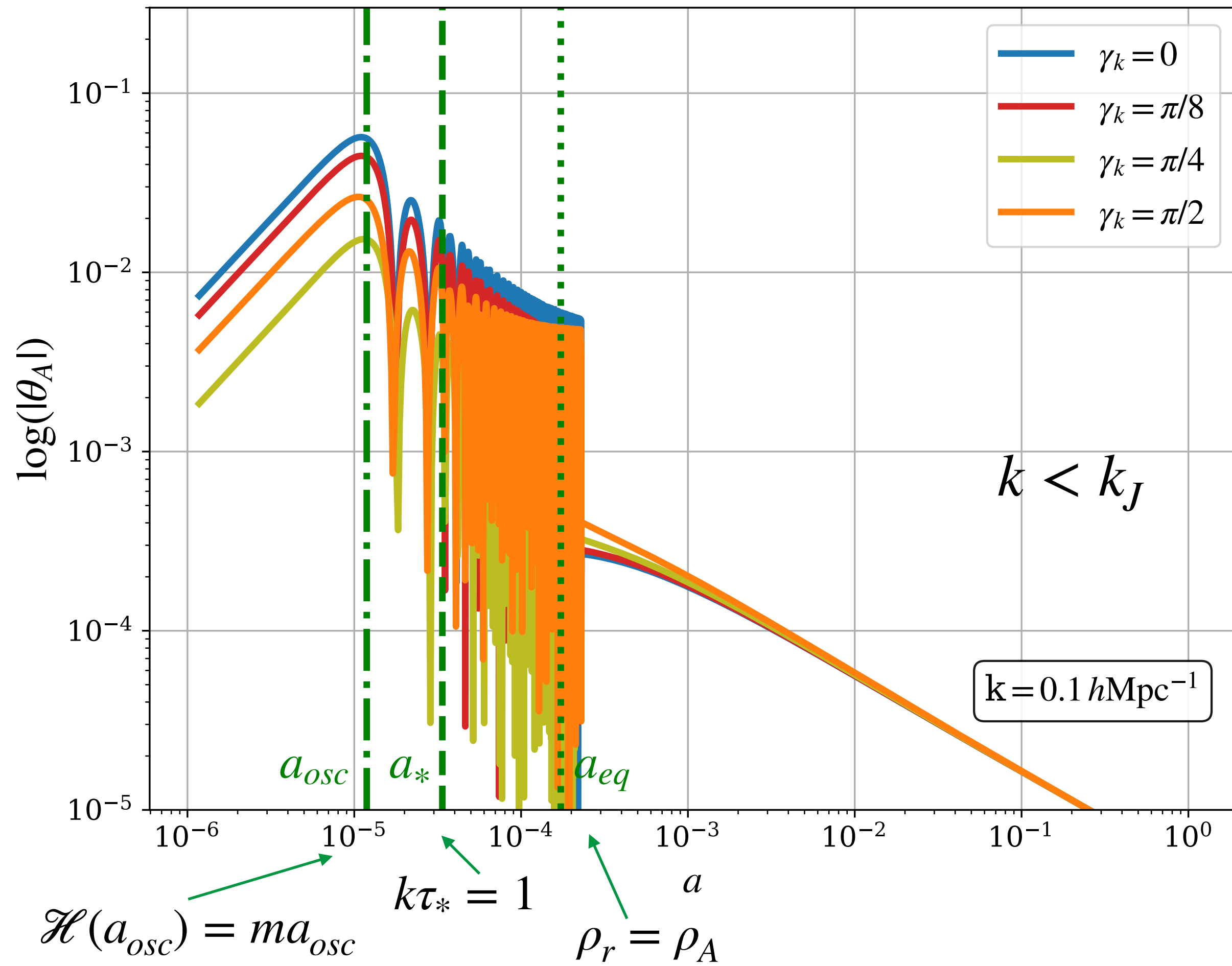
$\% \text{Diff} = 100 \times (\text{PA} - \text{PB}) / \text{PB}$, where the spectrum PB corresponds to the VFDM model with $\gamma_k=0$.

Velocity divergence evolution

$$(\rho + P)\theta = ik^i \delta T^A_0_i$$

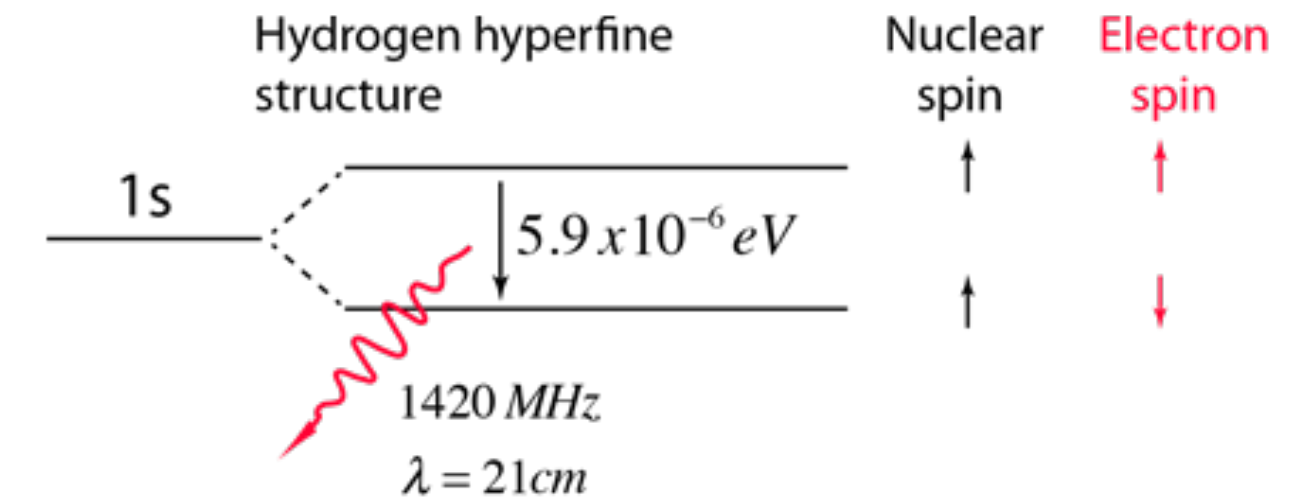
E.g. $m = 10^{-25} \text{eV}$ $k_J \simeq 0.27 \text{ h/Mpc}$

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$$\theta'' + 3\theta' + \left(\frac{k^4}{k_J^4} + 2 \right) \theta = - \frac{k^4}{k_J^4} \frac{k^2}{4\mathcal{H}} \eta$$


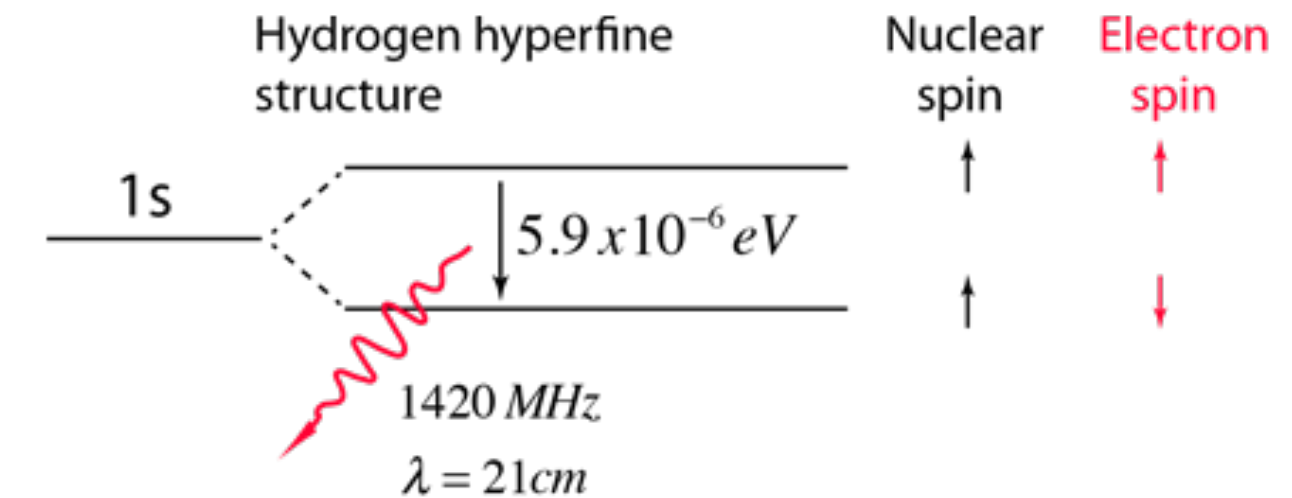
Power Spectrums on small scales and observations

21-cm experiments: Use the redshifted 21 cm line emission from HI observed with radio telescopes to explore the large-scale structure



Power Spectrums on small scales and observations

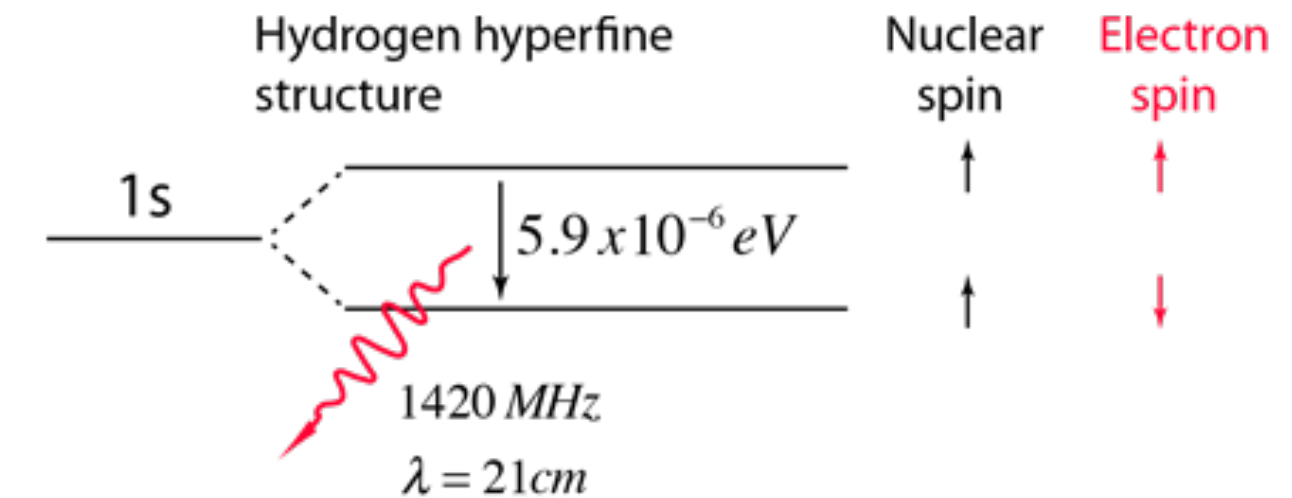
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- According to forecasts in [Muñoz et al PRD 2020] on how well 21-cm experiments could probe the matter power spectrum (PS) during cosmic dawn ($z = 12 - 25$):
 - A global-signal experiment could measure the amplitude of the PS integrated over $k = (40 - 80) \text{ Mpc}^{-1}$ with a precision of tens of percent.
 - A fluctuation experiment could constrain the PS to a similar accuracy in bins covering $k = (40 - 60) \text{ Mpc}^{-1}$ and $k = (60 - 80) \text{ Mpc}^{-1}$ even without astrophysical priors.

Power Spectrums on small scales and observations

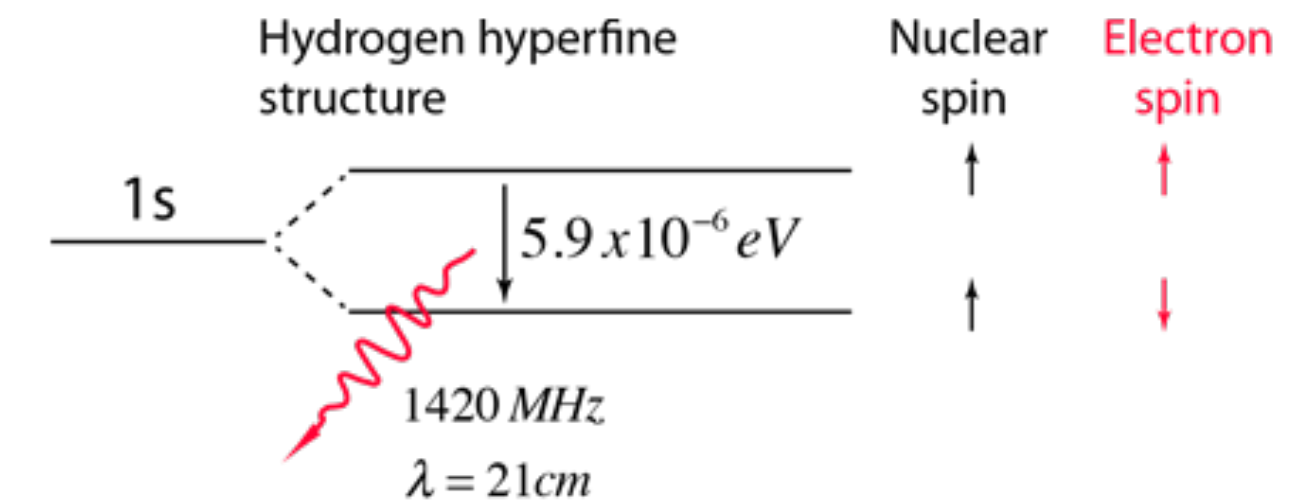
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 - A global-signal experiment could measure the amplitude of the PS integrated over $k = (40 - 80) \text{ Mpc}^{-1}$ with a precision of tens of percent.
 - A fluctuation experiment could constrain the PS to a similar accuracy in bins covering $k = (40 - 60) \text{ Mpc}^{-1}$ and $k = (60 - 80) \text{ Mpc}^{-1}$ even without astrophysical priors.
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Power Spectrums on small scales and observations

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- Forecasts generally assume that the relative velocity between CDM and baryons PS around recombination is the same for any DM candidate.

Baryon-DM *relative velocity Power Spectrum*

Primordial scalar power spectrum

Baryon-DM relative velocity: $\overrightarrow{v_{bd}} = \overrightarrow{v_b} - \overrightarrow{v_d}$

$$\langle v_{bd}^2 \rangle = \int \frac{dk}{k} \Delta_{vbd}^2(k)$$

$$\Delta_v^2(k) = \Delta_\zeta^2(k) \left(\frac{\theta_b - \theta_d}{k} \right)^2$$

Relative velocity divergence of baryons “b” and DM “d”

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- For SFDM, the effect on the 21 cm power spectrum was studied in [Marsh PRD 2015, Hotinli et al PRD 2022], in particular the **VAO** features, reaching at the *optimistic* conclusion that eventually future experiments may be sensitive to $m \sim 10^{-18}$ eV!!

SFDM and velocity acoustic oscillations (VAO)

[Hotinli, Marsh & Kamionkowski PRD 2022]

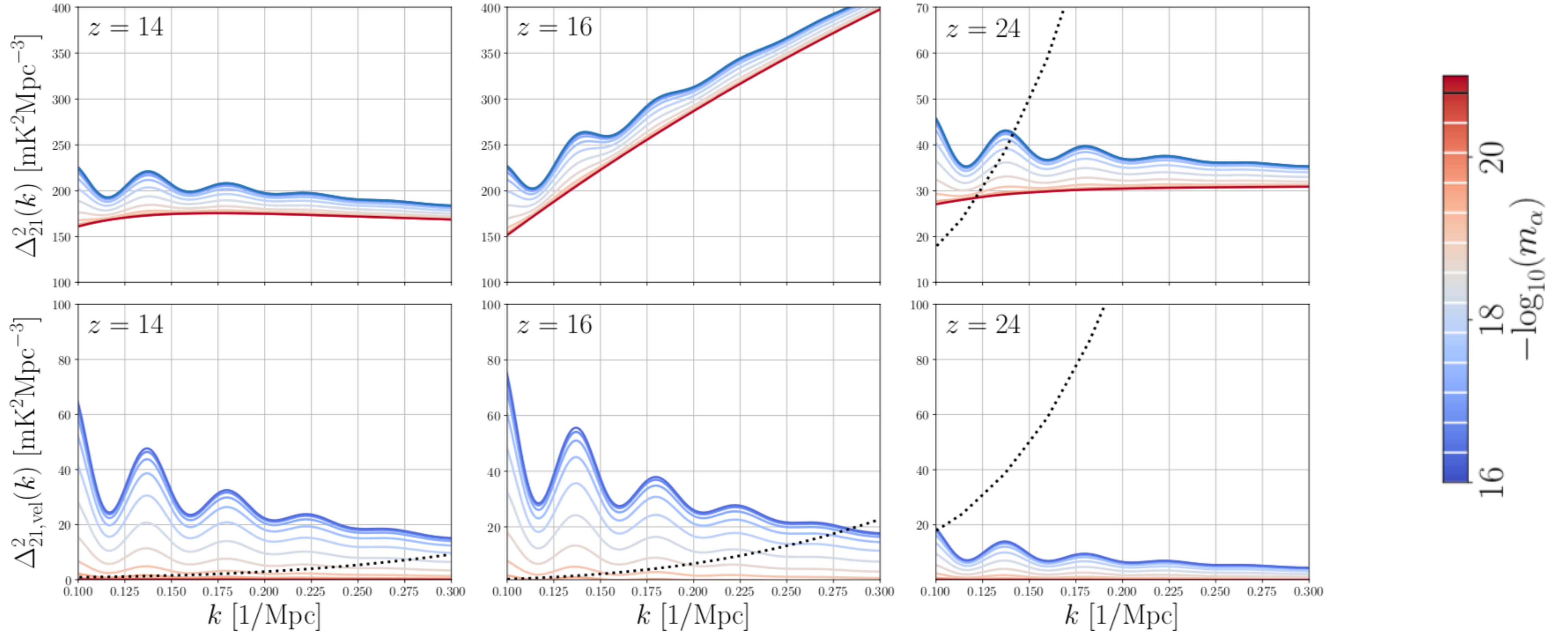
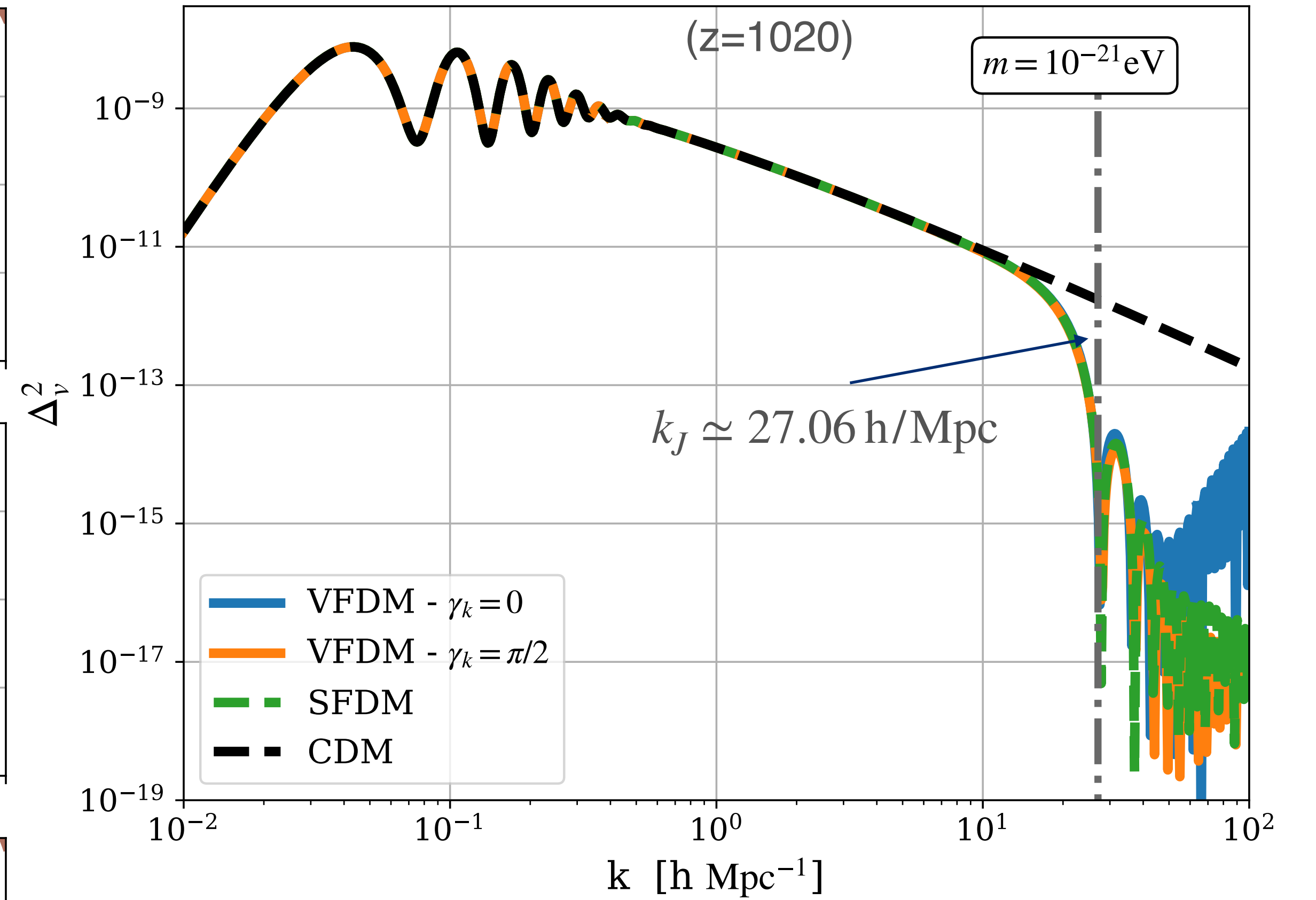
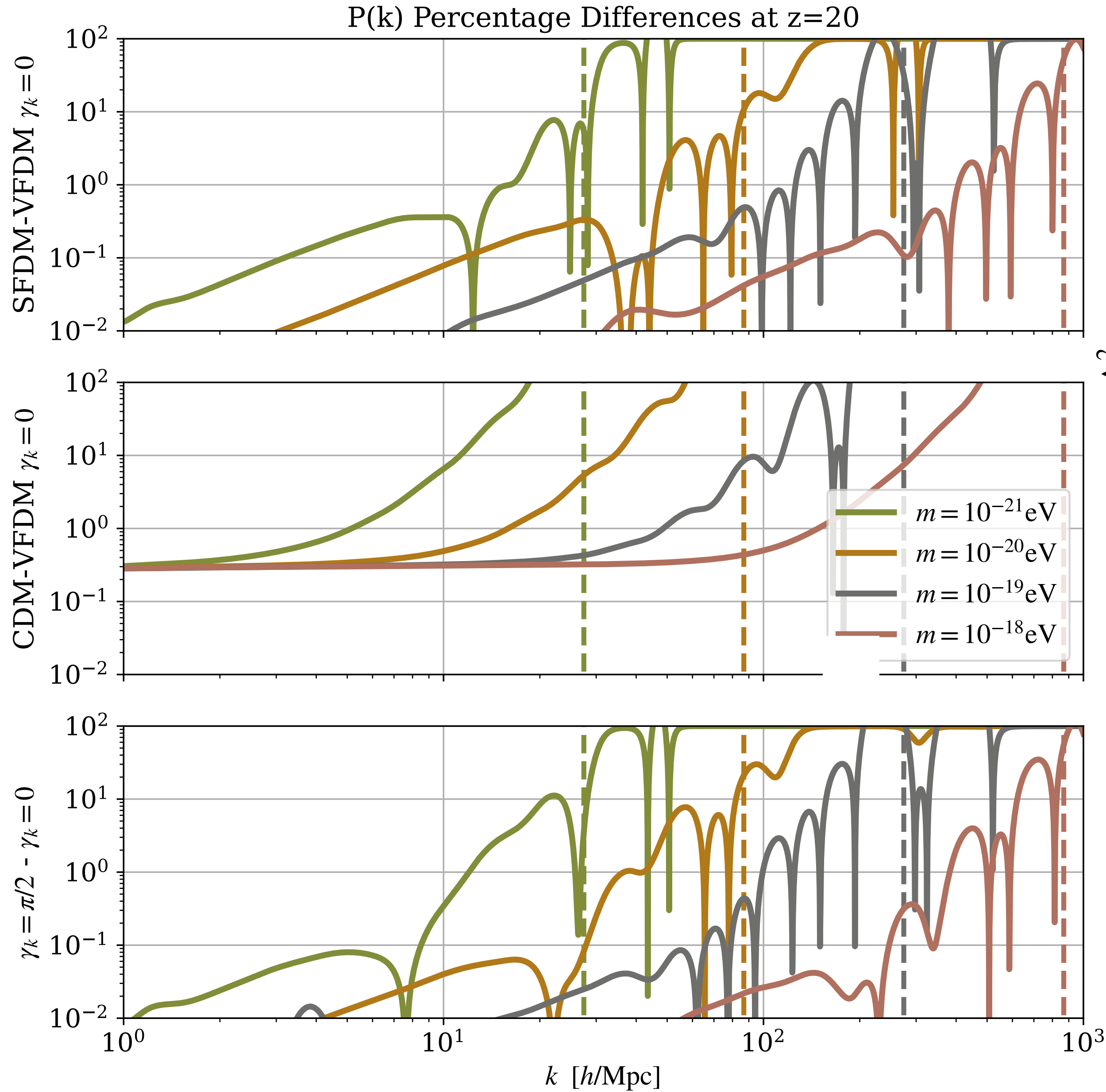
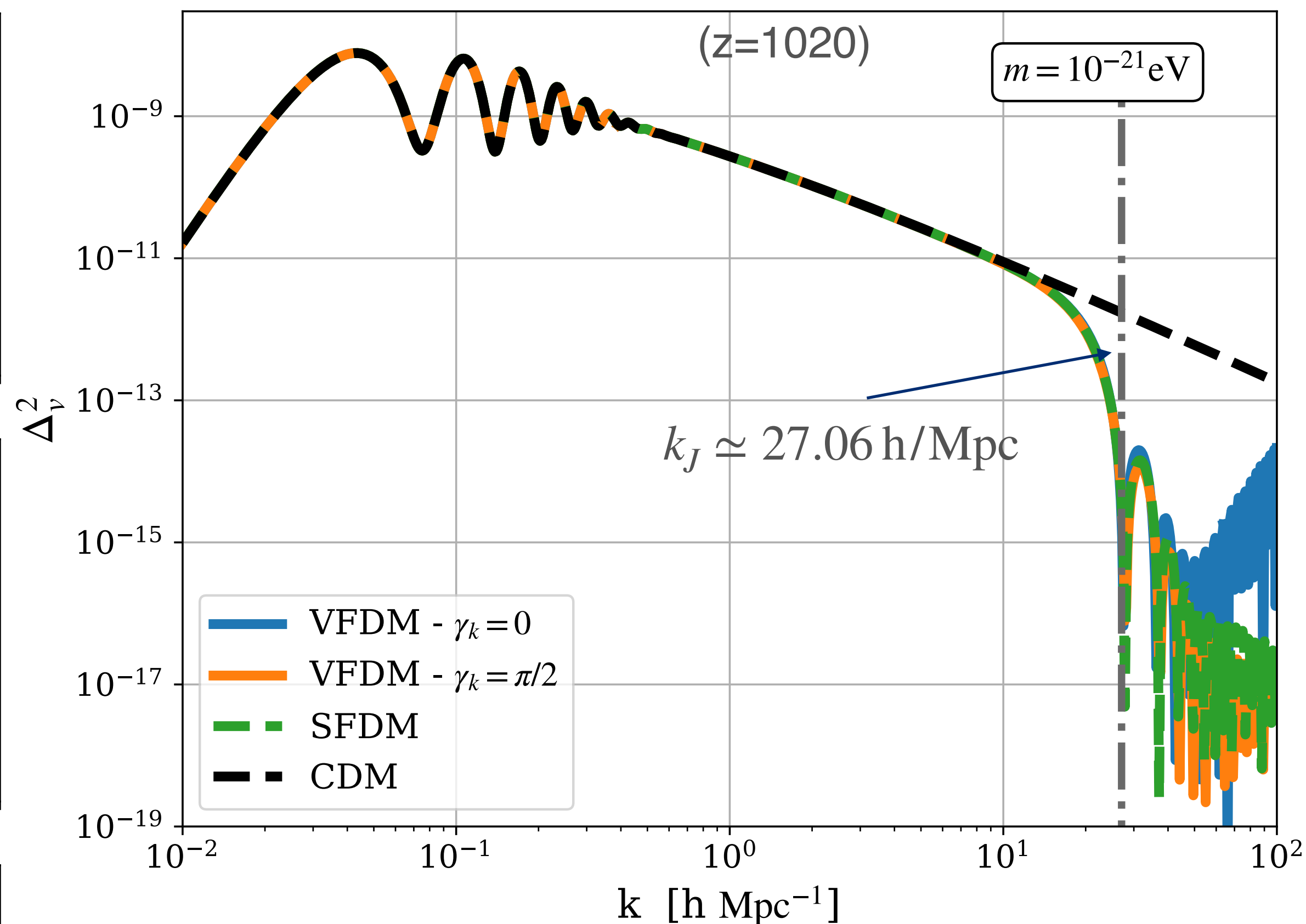
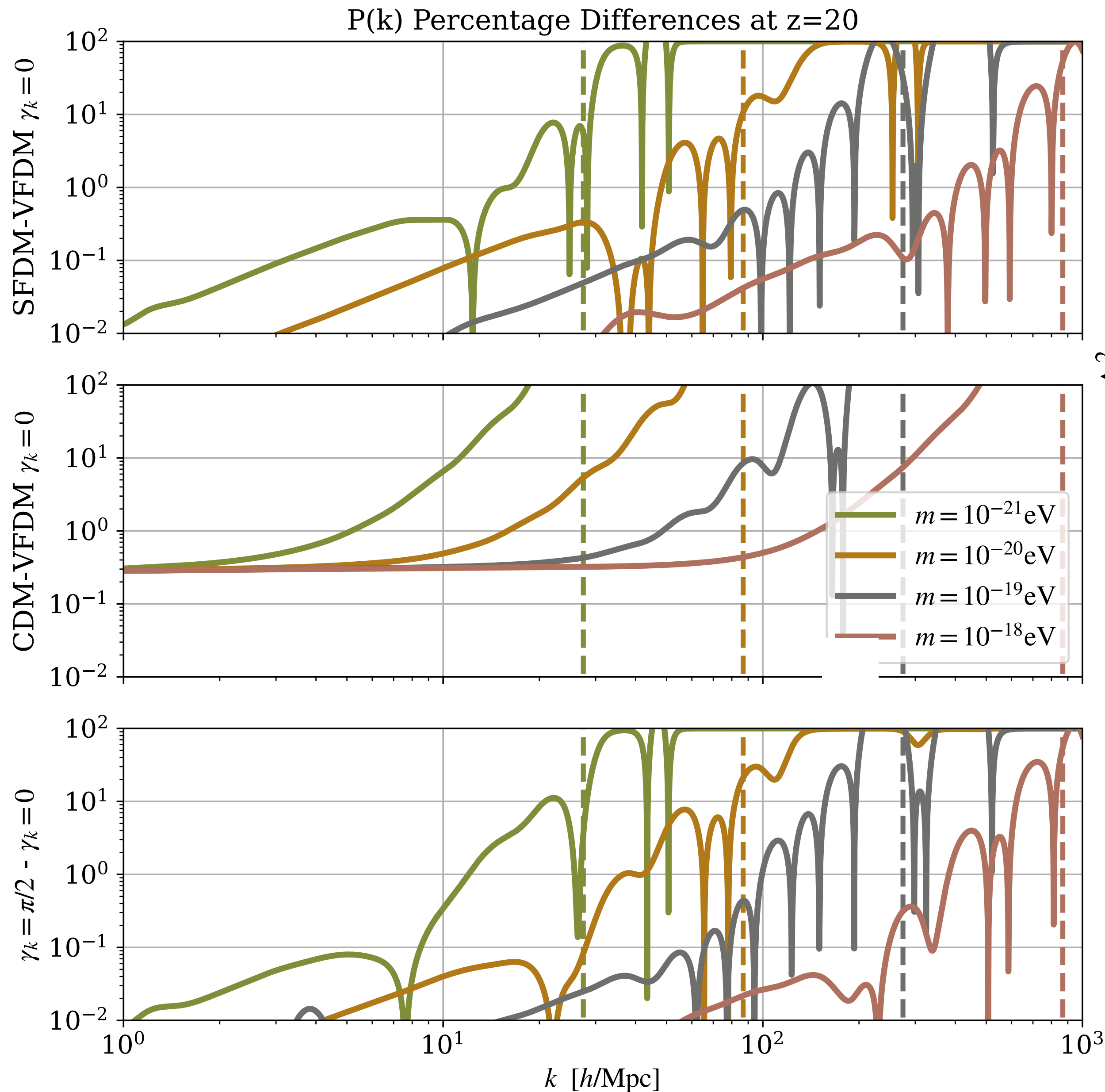


FIG. 3. The effect of ULAs on the VAO signature in the 21-cm power-spectra for redshift bins centred at $z = \{14, 16, 24\}$. The VAO amplitude can be shown to vary with m_α . The dotted black lines correspond to the anticipated noise (cosmic variance and thermal noise combined) for the HERA experiment, which we calculate with 21cmSense. We discuss the binning in wavenumber k in Sec. IV. Upper plots correspond the 21-cm signal. The blue end of the color spectrum corresponds to the prediction from the Λ CDM cosmology, averaged over 20 simulations with 21cmvFAST.

Matter & relative velocity power spectra -VFDM vs SFDM



Matter & relative velocity power spectra -VFDM vs SFDM



VFDM and SFDM have the same Jeans scale k_J but anisotropies and the enhancement of $\gamma_k \simeq 0$ modes make the analysis for VFDM more complicated than for the SFDM case...

Summary on Ultralight Dark Matter

Early-time evolution: SFDM behaves as isotropic Dark Energy. For VFDM σ_{ij} has to be considered in the early universe, BBN gives $m \gtrsim 10^{-26} \text{eV}$.

Suppression effect at Jeans scale:

- In both SFDM and VFDM models, we obtain a suppression in the power spectrum at small scales characterized by the same scale, namely the Jeans scale $k_J = \sqrt{ma\mathcal{H}}$.
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Beyond the linear regime: constraints are sensitive to uncertainties in the modeling of small scale structure $\rightarrow$ crucial to have complementary independent probes

Phenomenological descriptions on small scales: necessary and under development

Thanks for your attention!!



Quantum Summer 2025

Iriri, ES, Brazil. April 07-11, 2025.

Diana López Nacir

