

# The Hubble tension (from) A Supernova perspective

**David Camarena**

PPGCosmo, UFES

in collaboration with Valerio Marra

16.04.2021 · PPGCosmo Seminars · UFES

# $H_0$ discrepancy



- disagreement between early and late-time
- $\Lambda$ CDM model can not explain this tension
- how quantify the tension?

$$\mathcal{T} \sim \frac{|\hat{x}_1 - \hat{x}_2|}{\sqrt{\sigma_1^2 + \sigma_2^2}}$$

- statistical fluct. or real disagreement?

$2\sigma \rightarrow$ curiosity

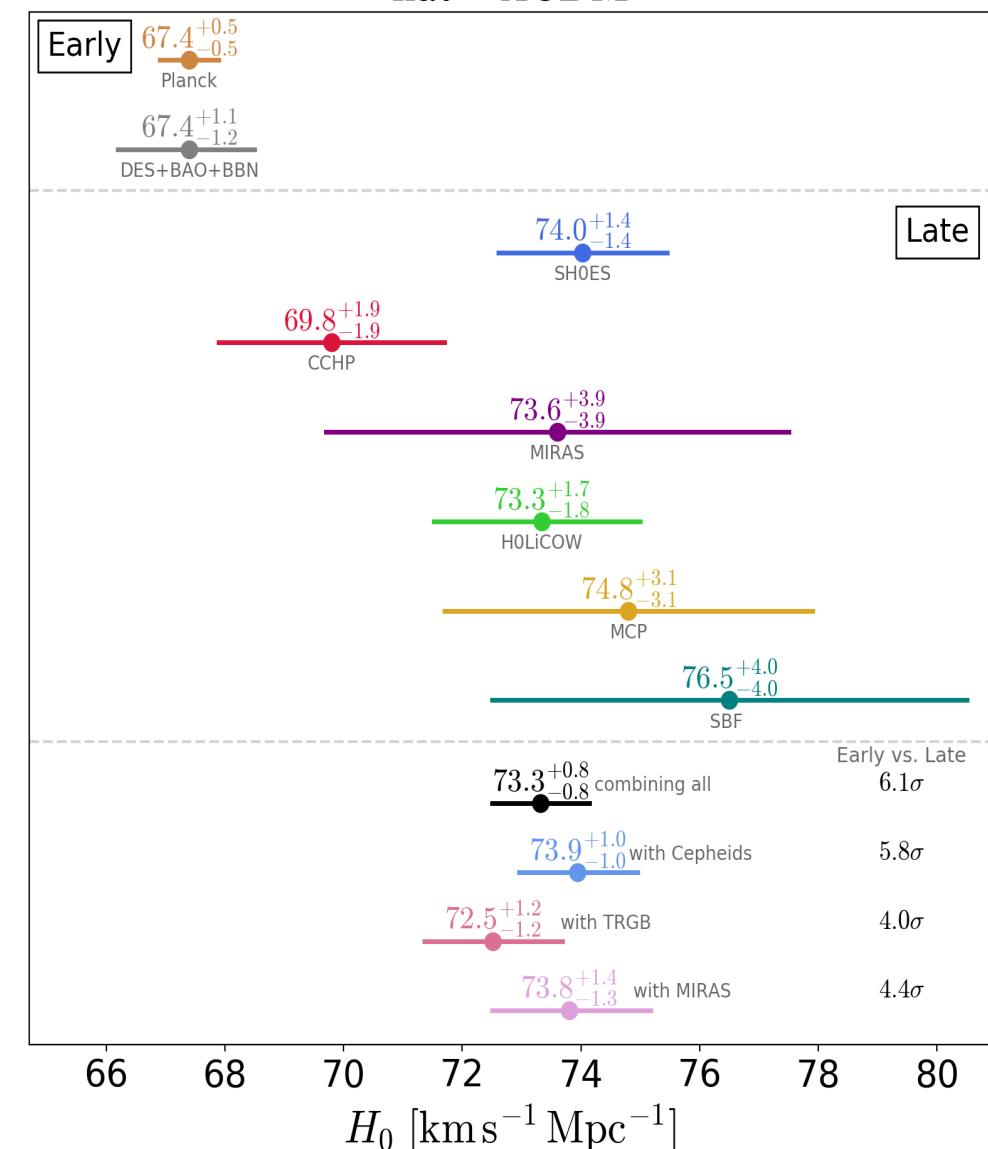
$3\sigma \rightarrow$ tension

$4\sigma \rightarrow$ discrepancy

$5\sigma \rightarrow$ crisis

L. Verde *et al.* arXiv:1907.10625

flat –  $\Lambda$ CDM



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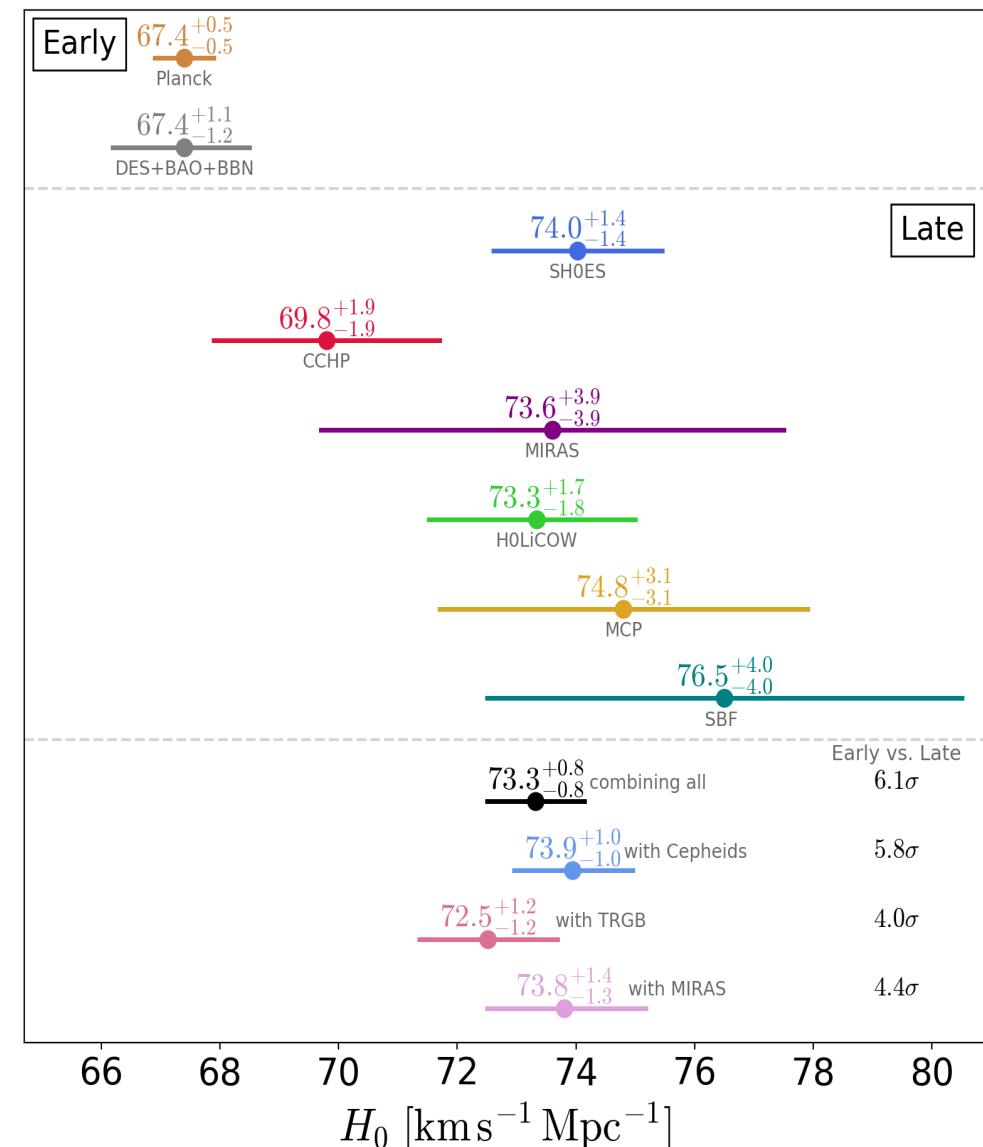
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$4\sigma \rightarrow$ **discrepancy**

$5\sigma \rightarrow$ **crisis!**

L. Verde *et al.* arXiv:1907.10625

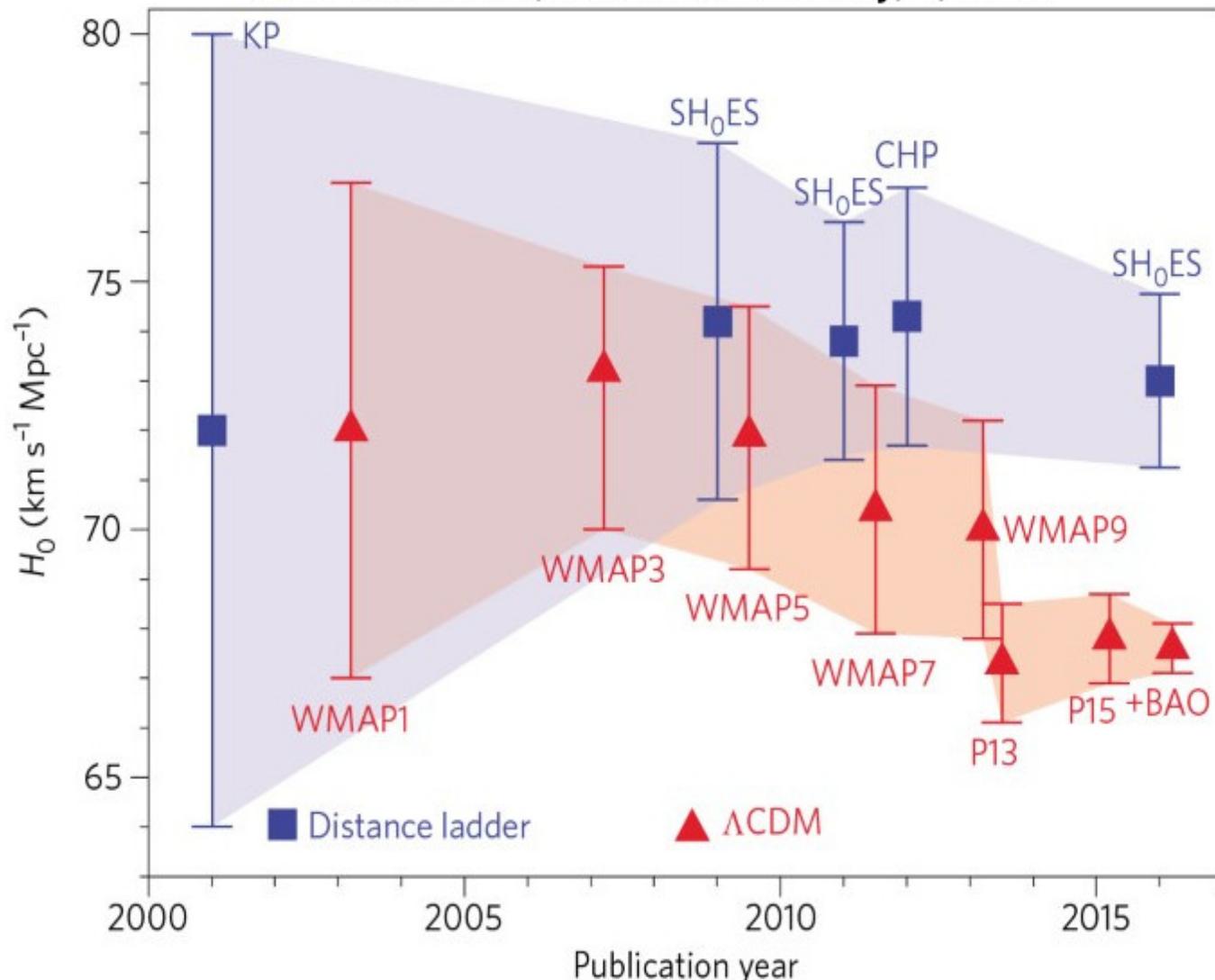
flat –  $\Lambda$ CDM



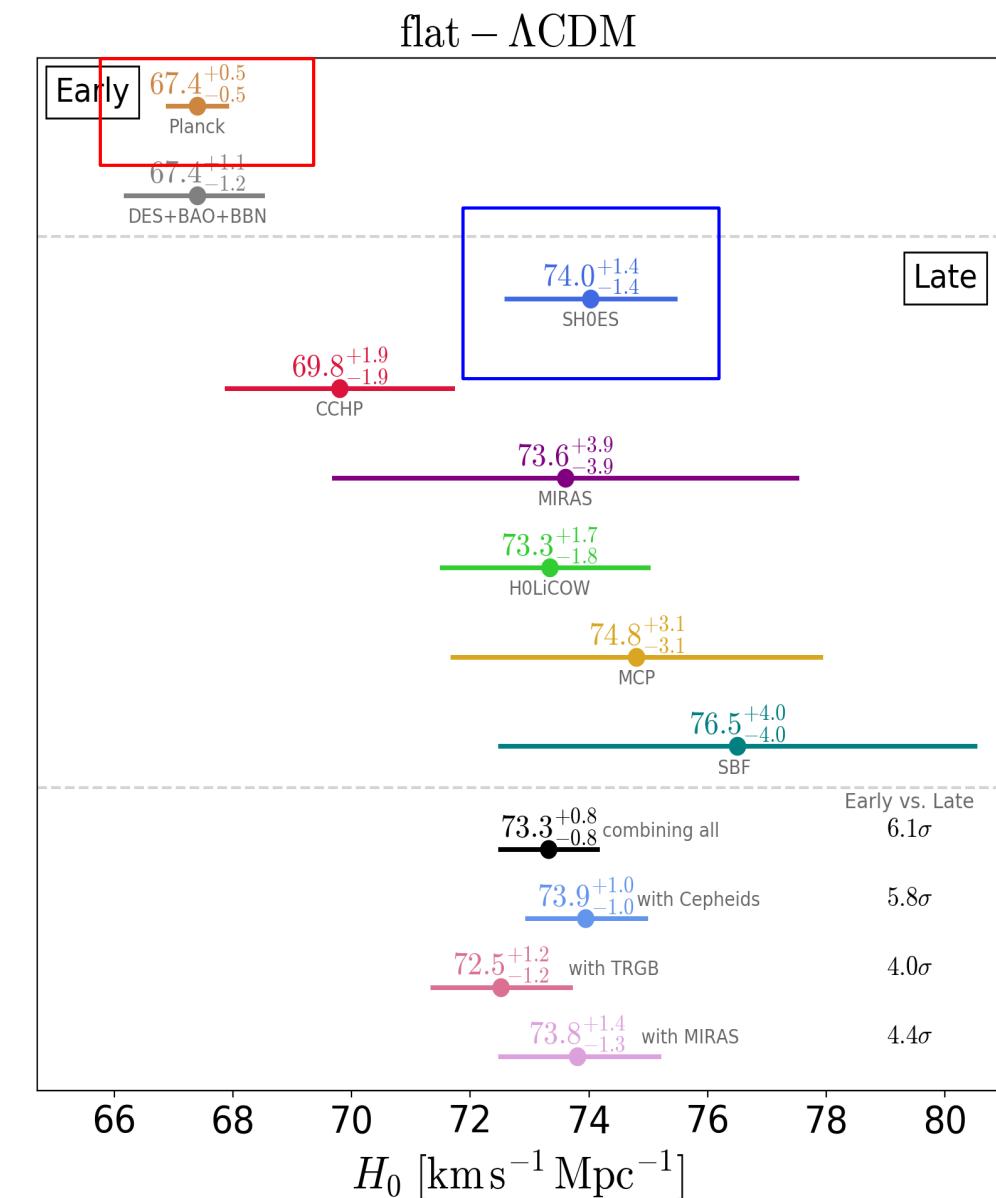
# $H_0$ discrepancy



W. L. Freedman, Nature Astronomy, 1, 0169



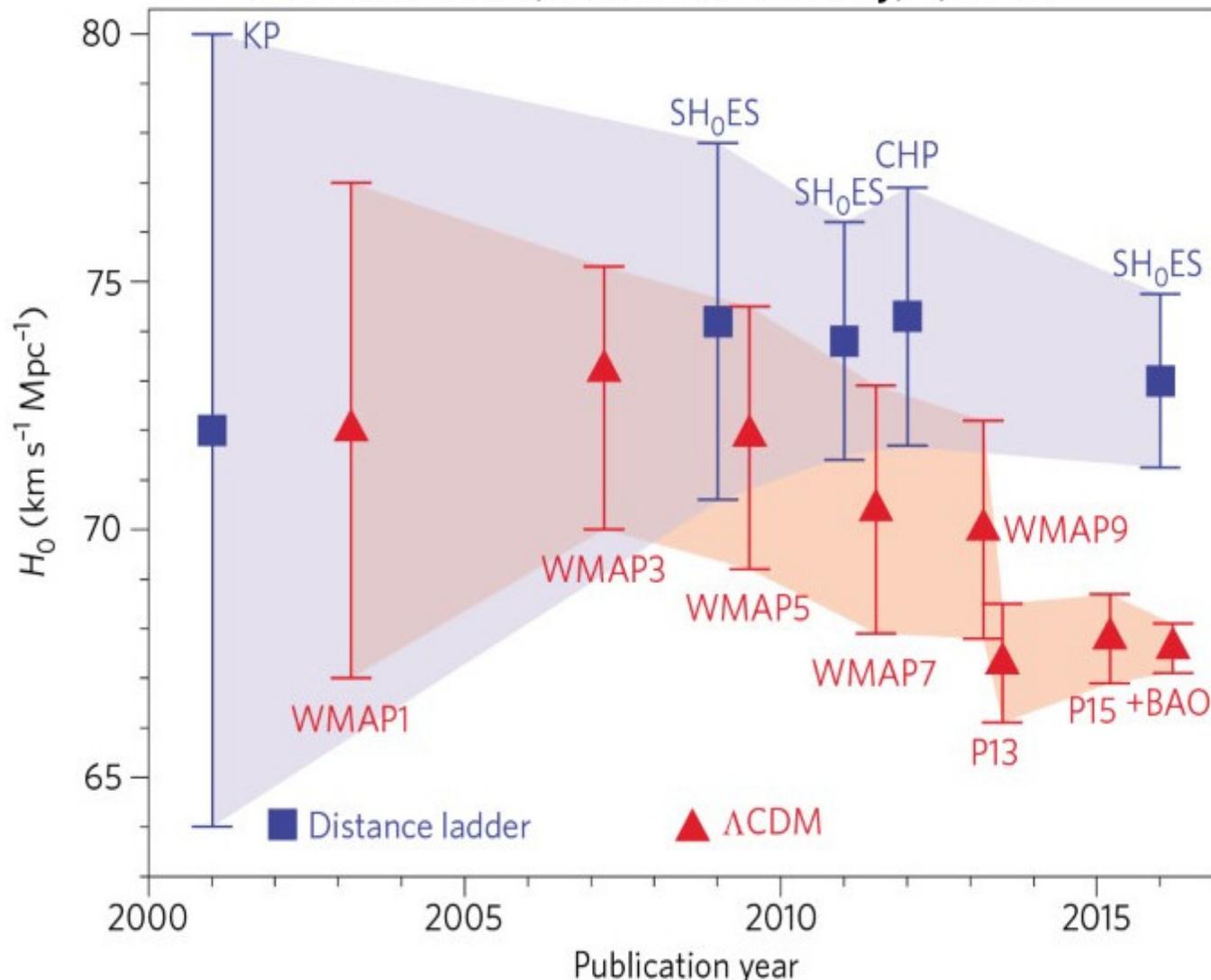
L. Verde et al. arXiv:1907.10625



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W. L. Freedman, Nature Astronomy, 1, 0169



Riess, A. G. et. al, arXiv:2012.08534

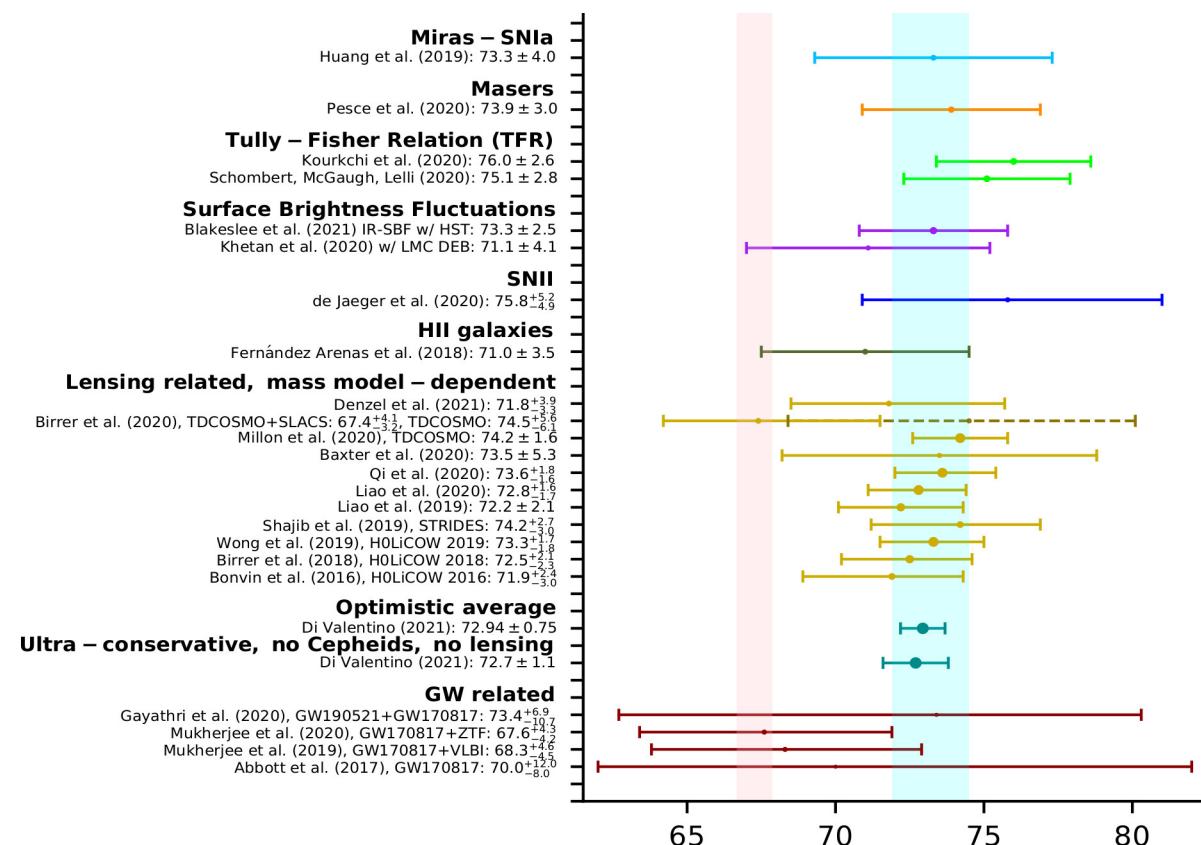
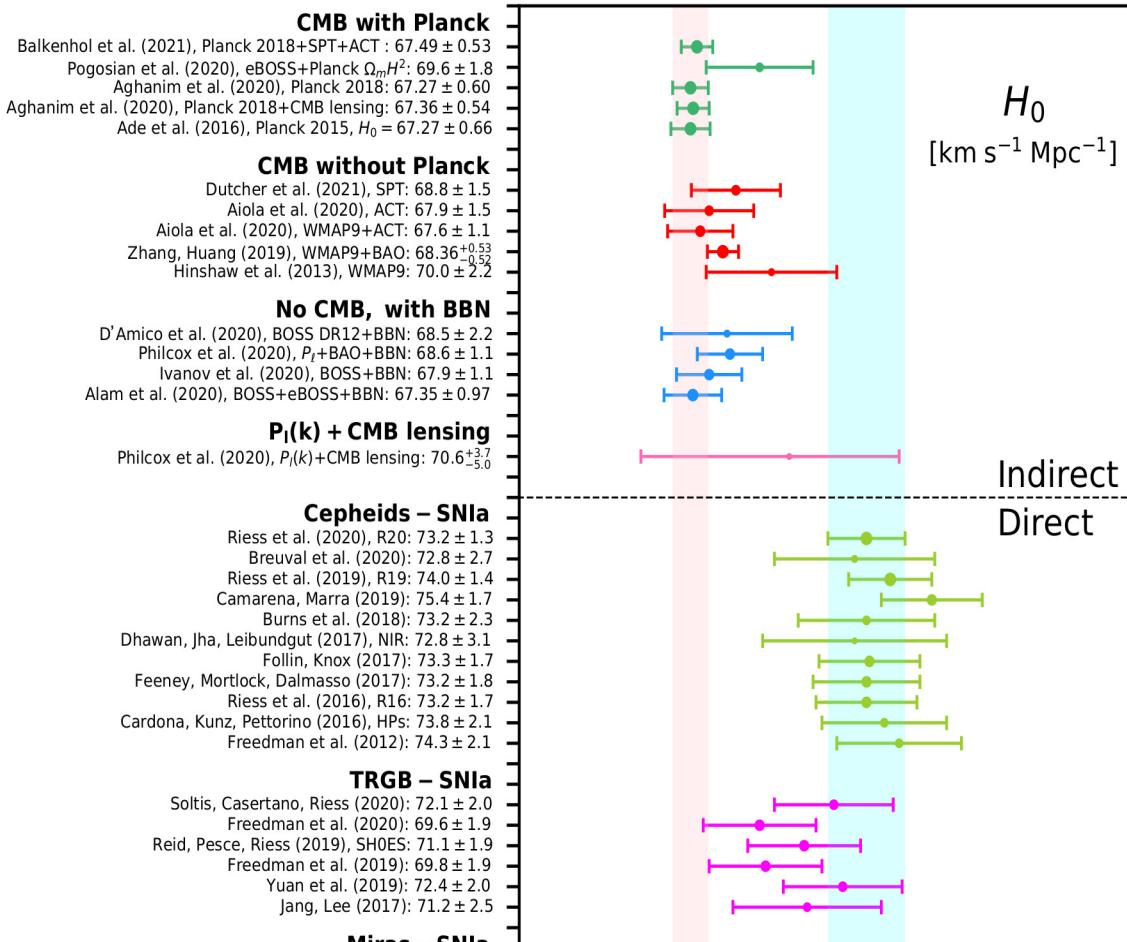
$$H_0 = 73.2 \pm 1.3$$

$\sim 4\sigma$

$$H_0 = 67.49 \pm 0.53$$

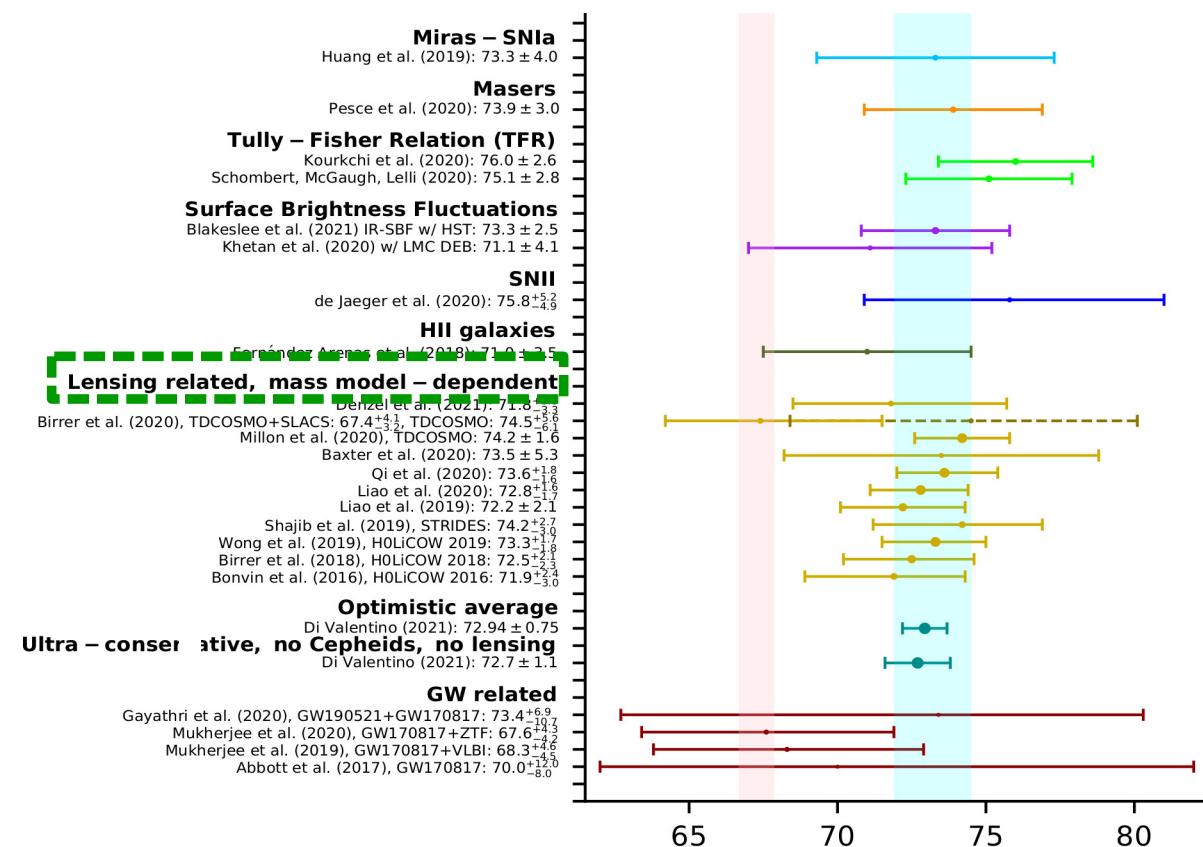
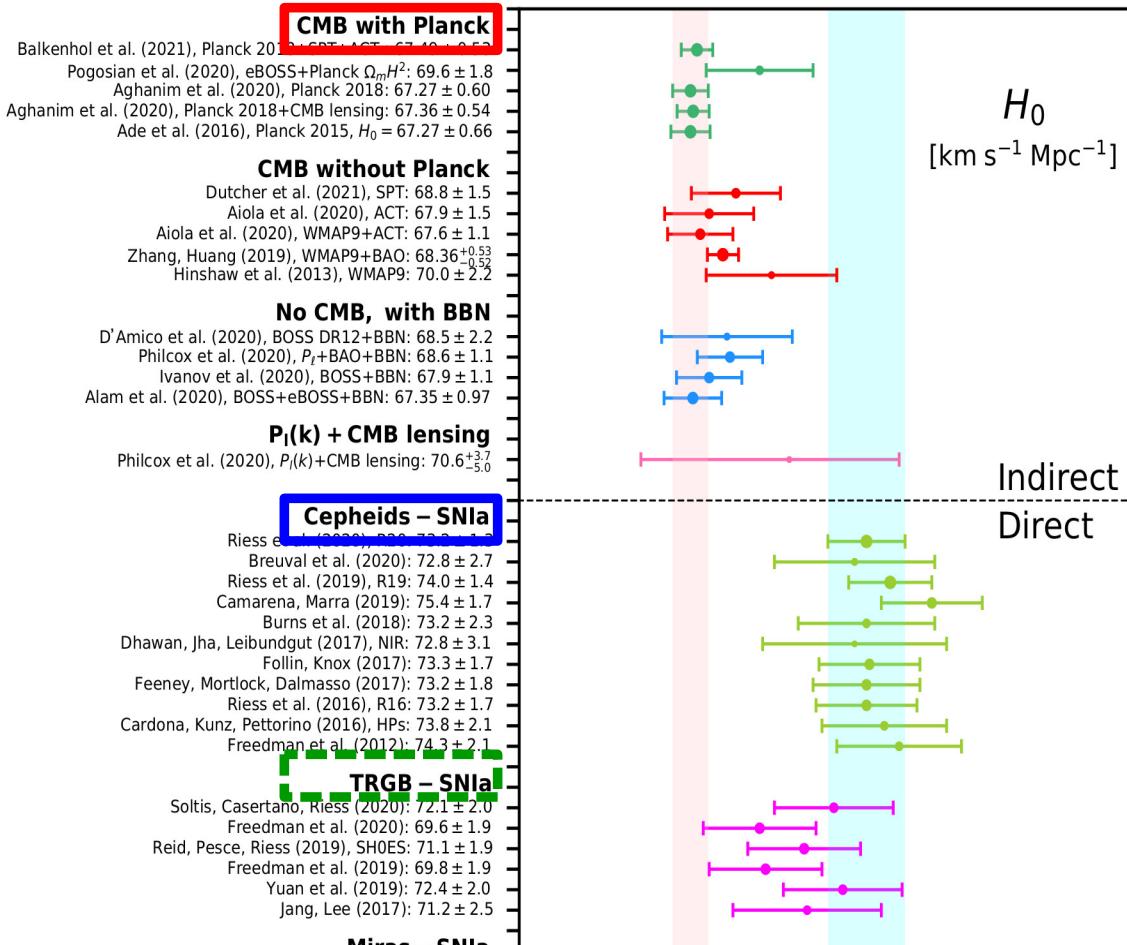
Planck Collaboration, arXiv:1807.06209

# $H_0$ discrepancy



E. Di Valentino et al., arXiv:2103.01183

# $H_0$ discrepancy

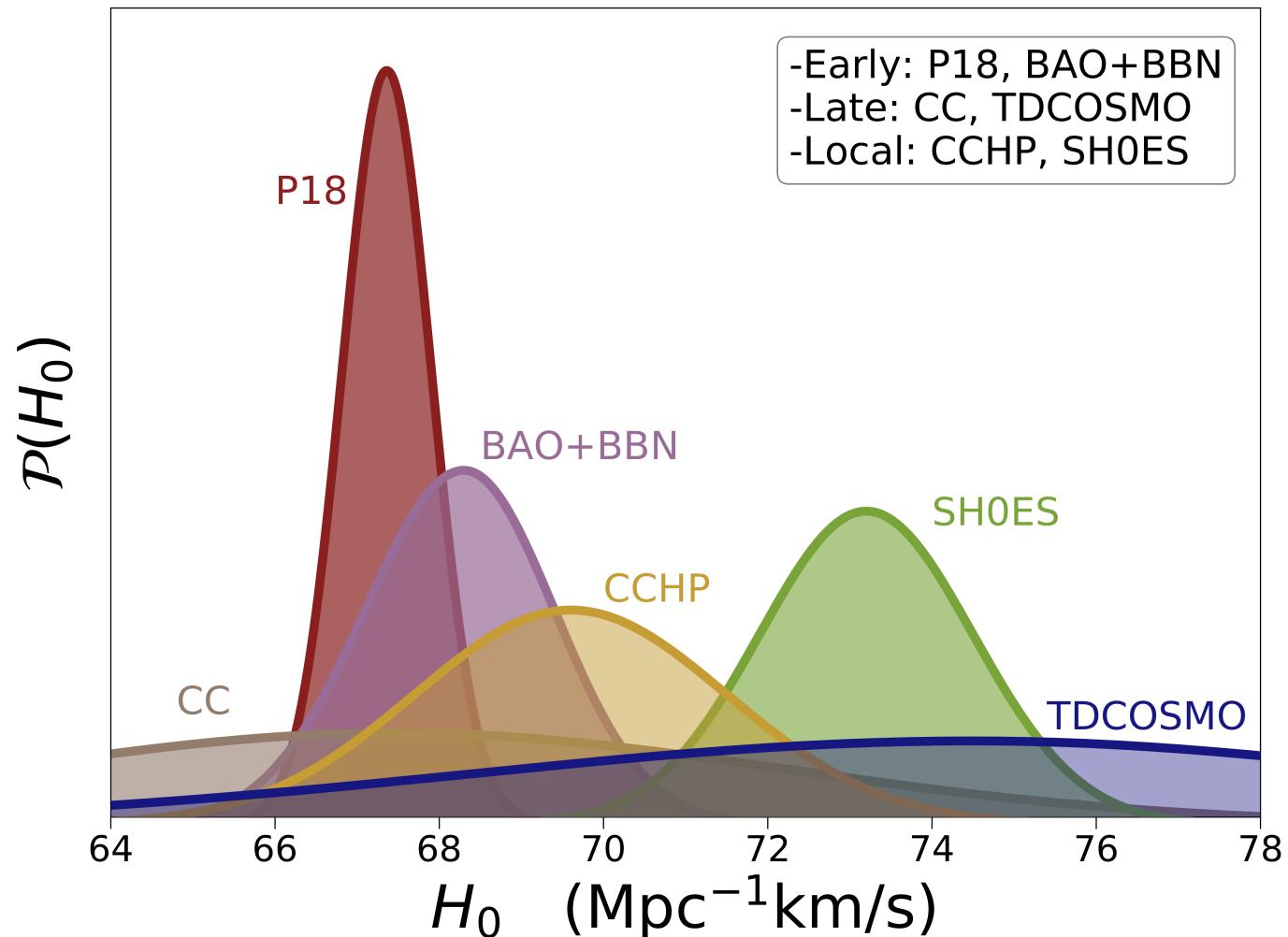


E. Di Valentino et al., arXiv:2103.01183

# $H_0$ discrepancy



J. L. Bernal et. al, arXiv:2102.05066



# Systematic or new physics?



MAKE A

CHOICE?



## Systematic errors

- Cosmic variance on  $H_0$
- Cepheids calibration
- Excess of lens  $A_L$
- Discrepancy low- $\ell$  and high- $\ell$
- ...

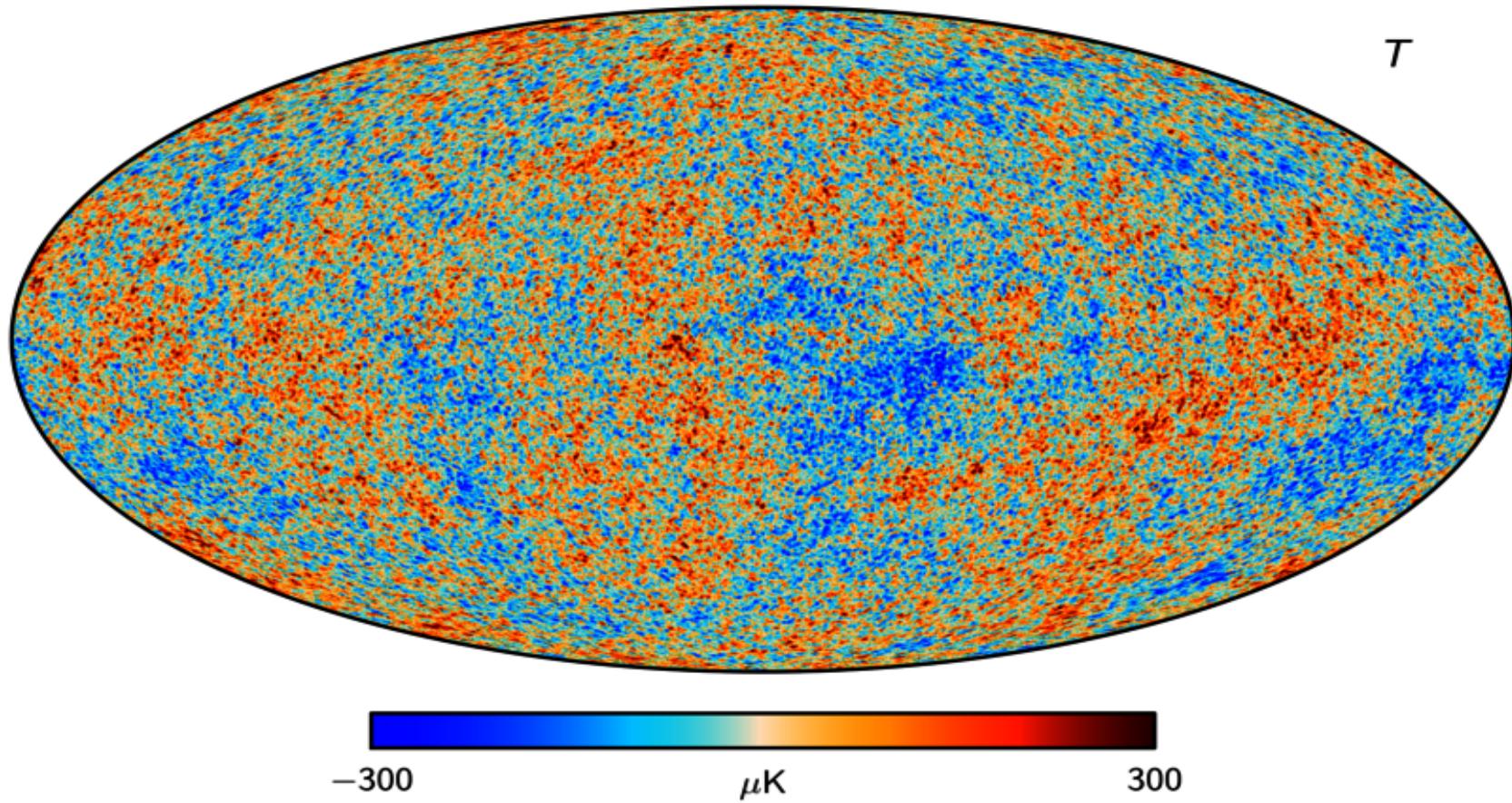
## New physics

- Low- $z$  transitions
- Early dark energy
- Neutrinos
- Void models
- Dark sector interactions
- ...

# Cosmic Microwave Background



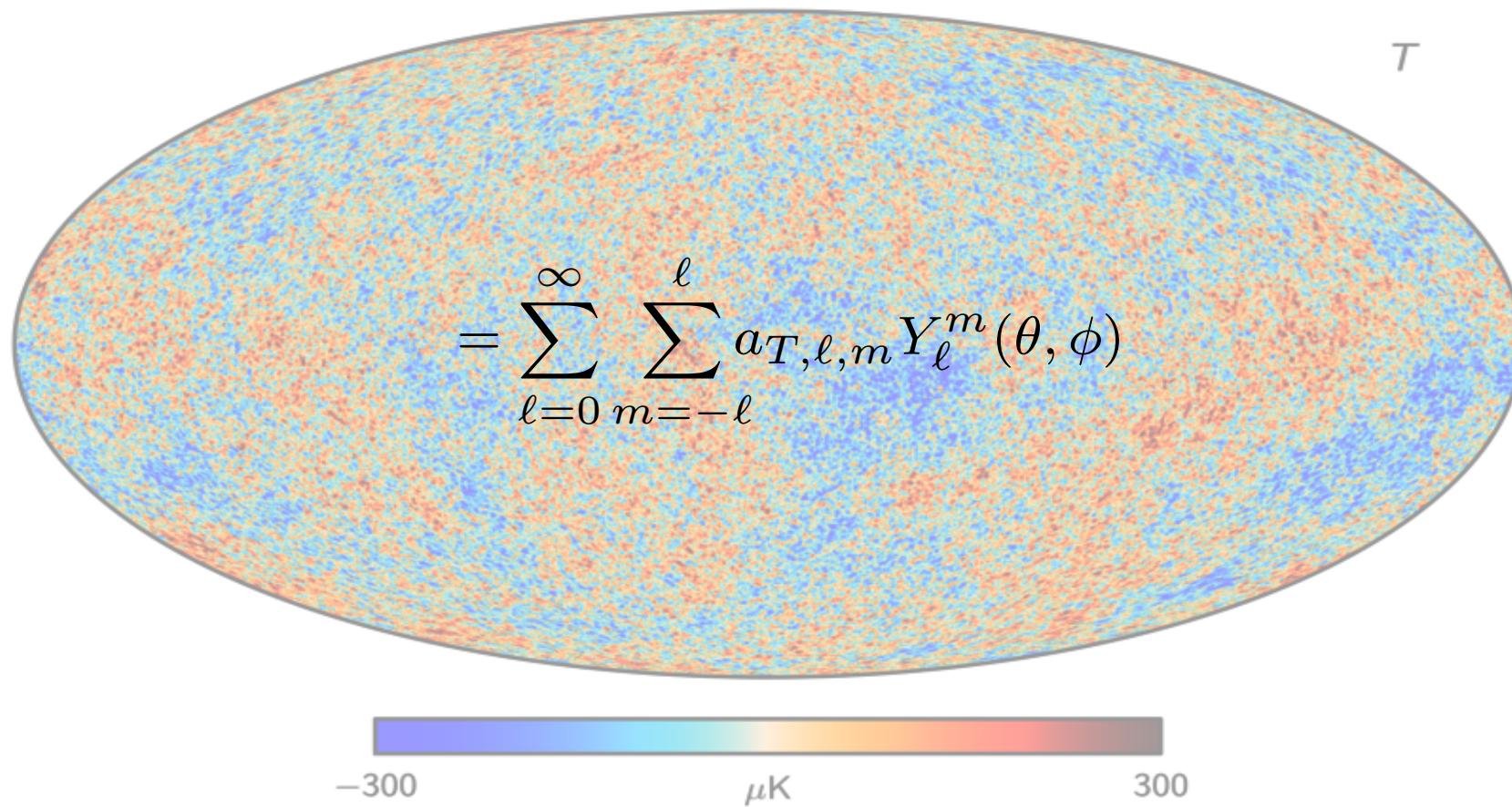
$TT$  map



# Cosmic Microwave Background



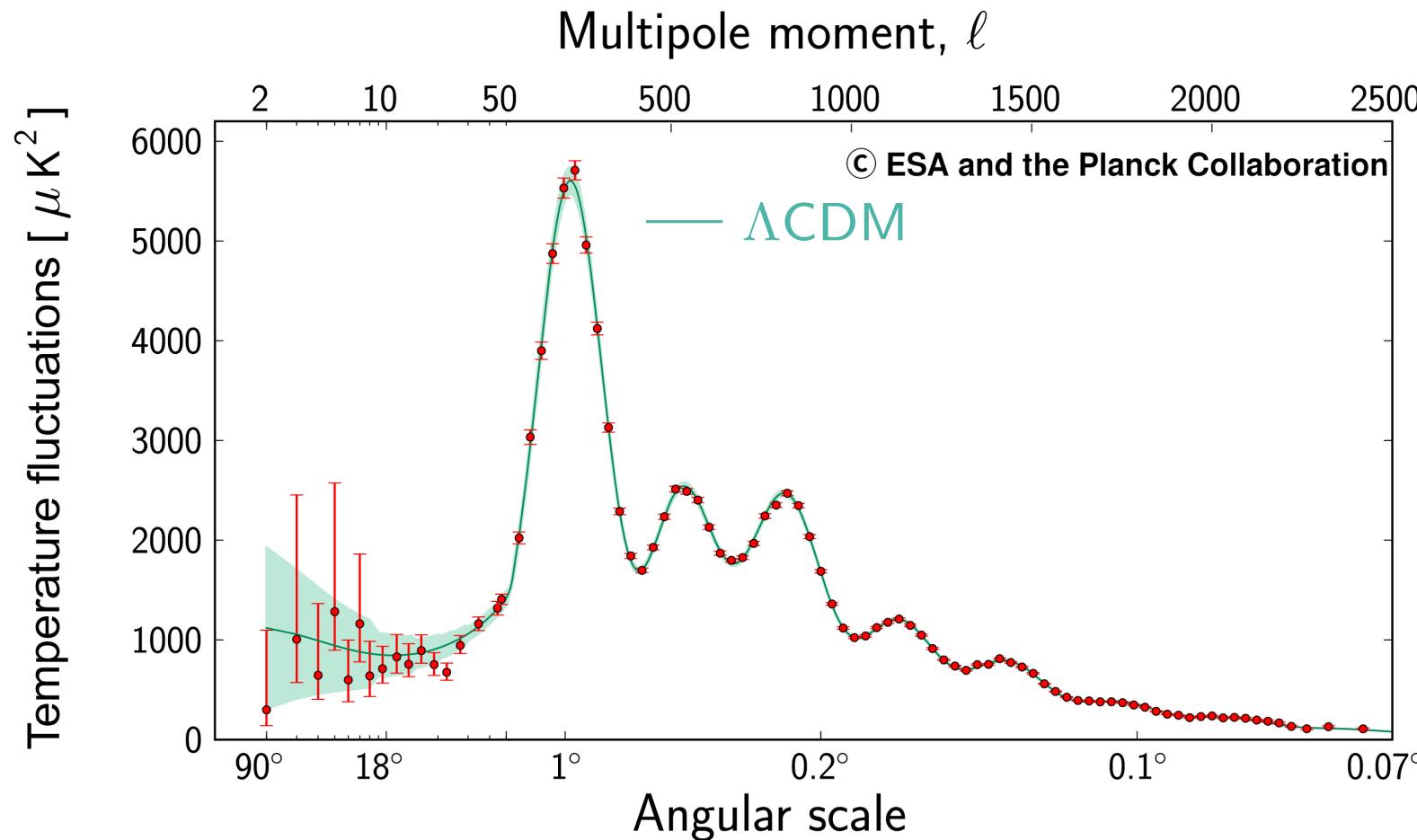
$$C_{TT,\ell} = \langle |a_{T,\ell m}|^2 \rangle$$



# Cosmic Microwave Background



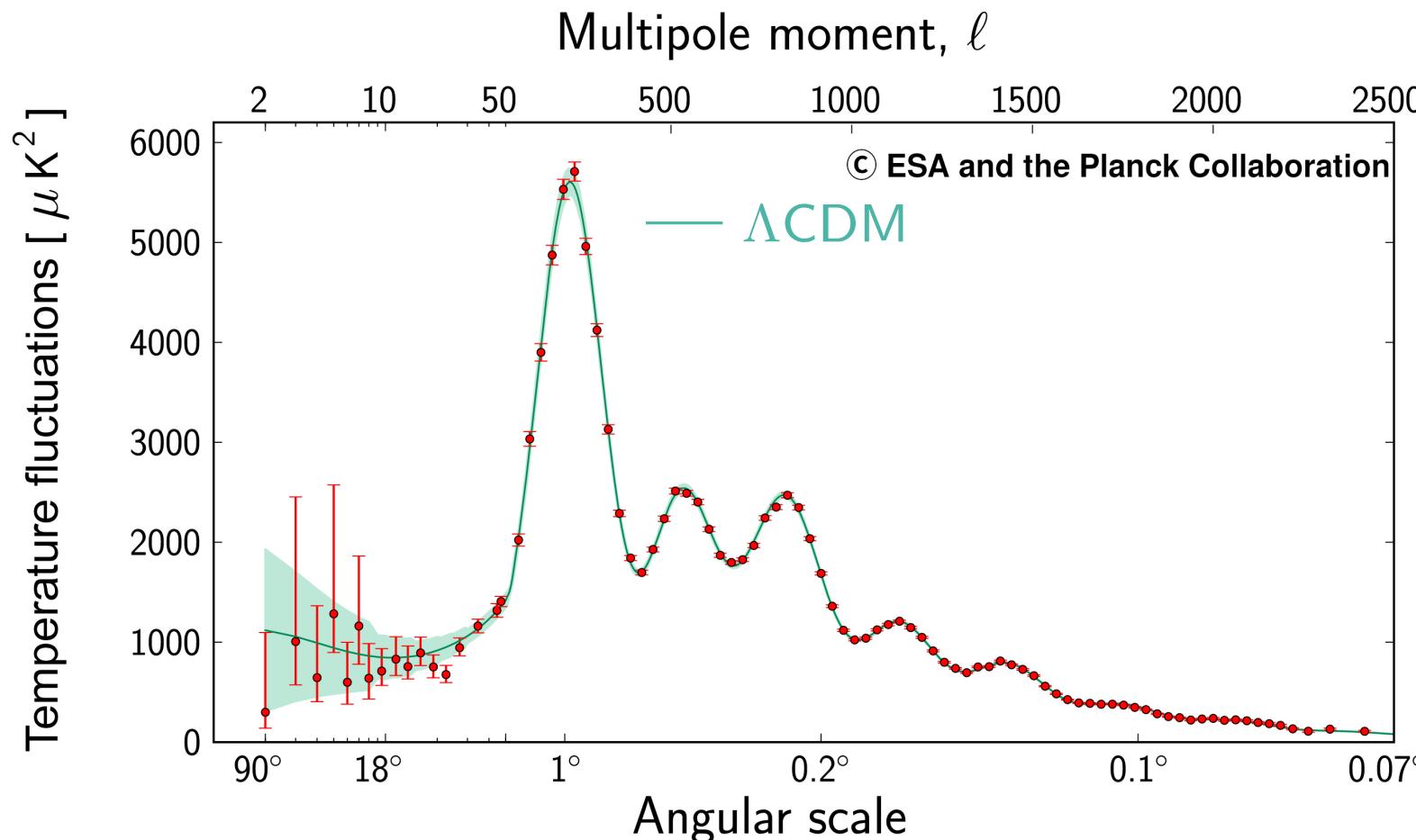
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# Cosmic Microwave Background



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Results from Planck18 (arXiv:1807.06209)

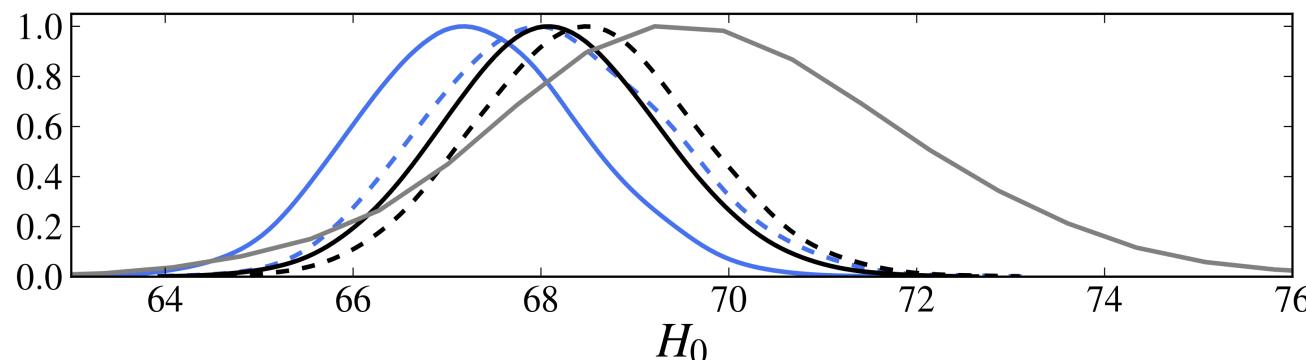
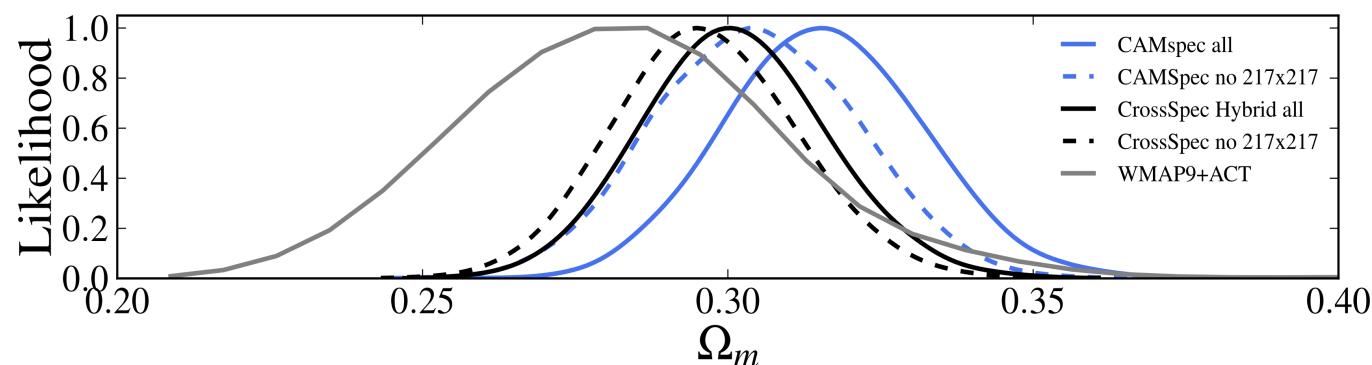
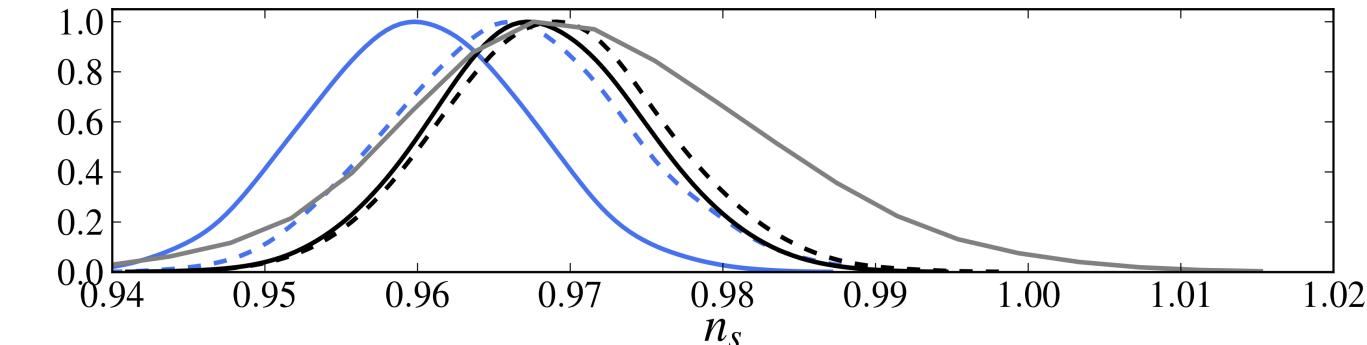
Parameter	TT,TE,EE+lowE+lensing 68% limits
$\Omega_b h^2$ . . . . .	$0.02237 \pm 0.00015$
$\Omega_c h^2$ . . . . .	$0.1200 \pm 0.0012$
$100\theta_{\text{MC}}$ . . . . .	$1.04092 \pm 0.00031$
$\tau$ . . . . .	$0.0544 \pm 0.0073$
$\ln(10^{10} A_s)$ . . . . .	$3.044 \pm 0.014$
$n_s$ . . . . .	$0.9649 \pm 0.0042$
$H_0$ [ $\text{km s}^{-1} \text{ Mpc}^{-1}$ ] . .	$67.36 \pm 0.54$

From peak structure:  $r_s$  ( $d_A^*$ ),  $\Omega_b h^2$ ,  $\Omega_m h^2 \rightarrow H_0$

# Cosmic Microwave Background



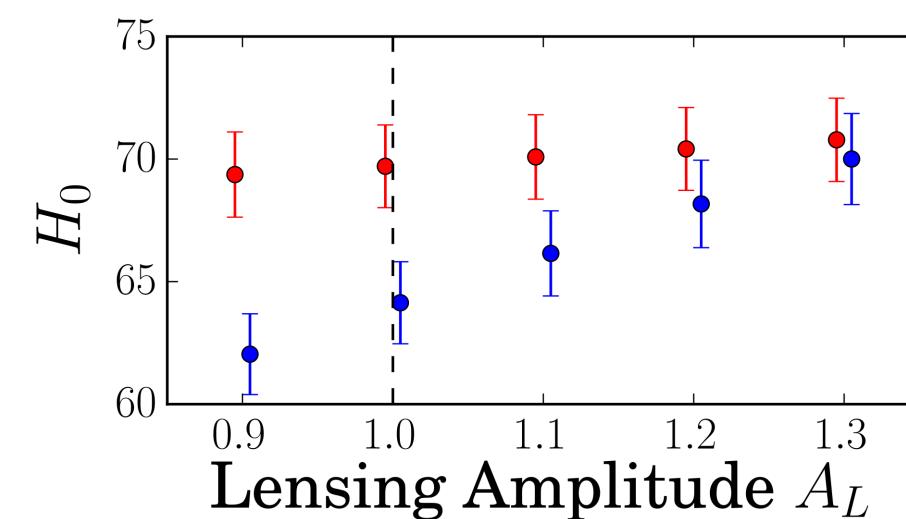
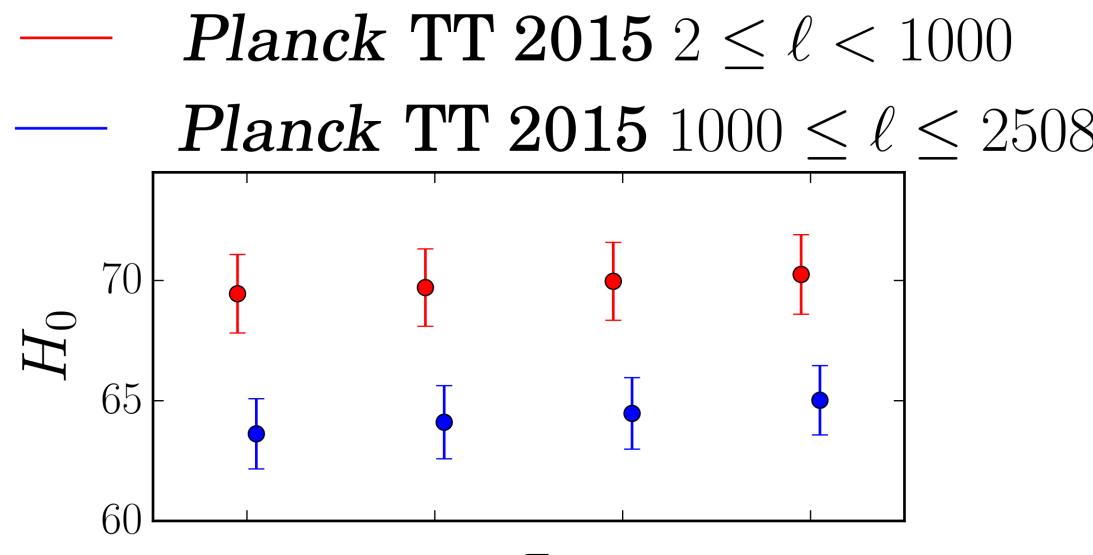
- Internal inconsistencies in the Planck  $TT$  power spectrum between frequencies (D. Spergel et al., arXiv:1312.3313)



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- Tension between multipoles  $\ell < 1000$  and  $\ell \geq 1000$  (G. E. Addison et. al arXiv:1511.00055)



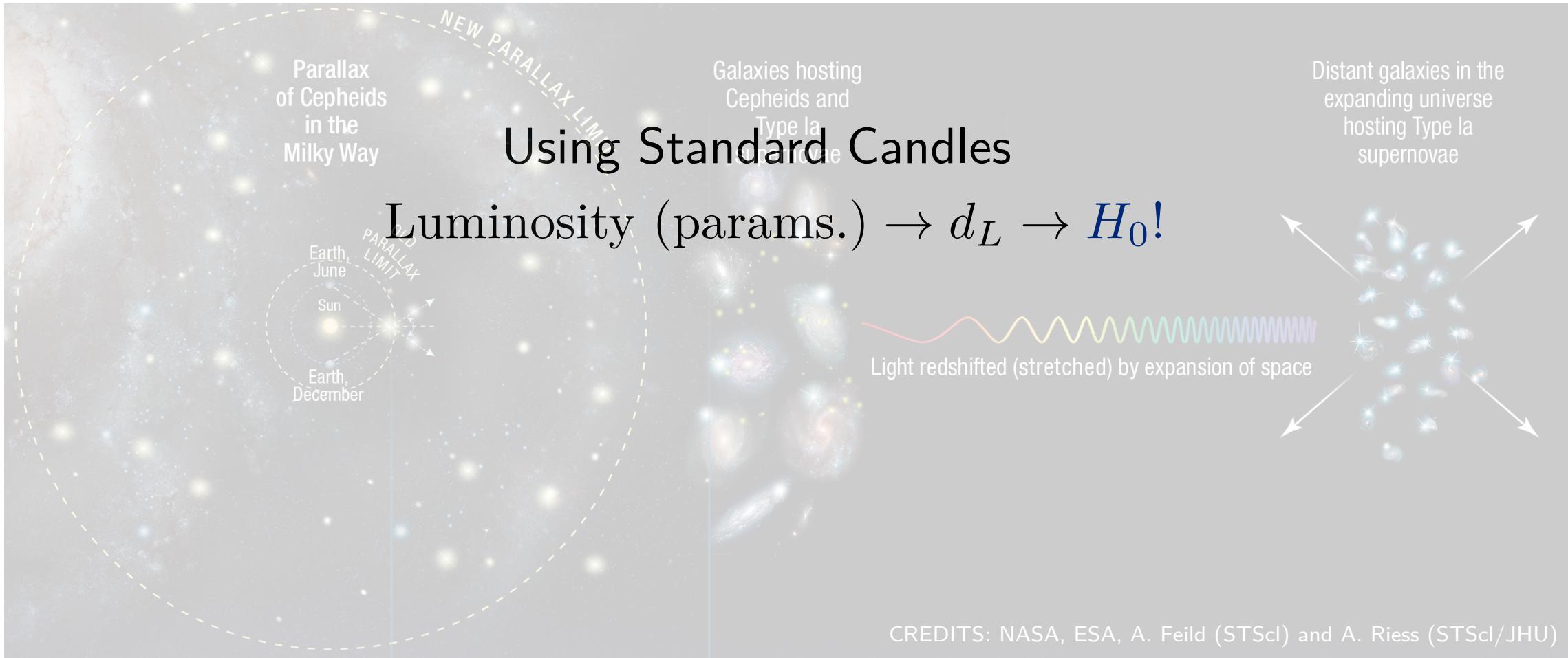
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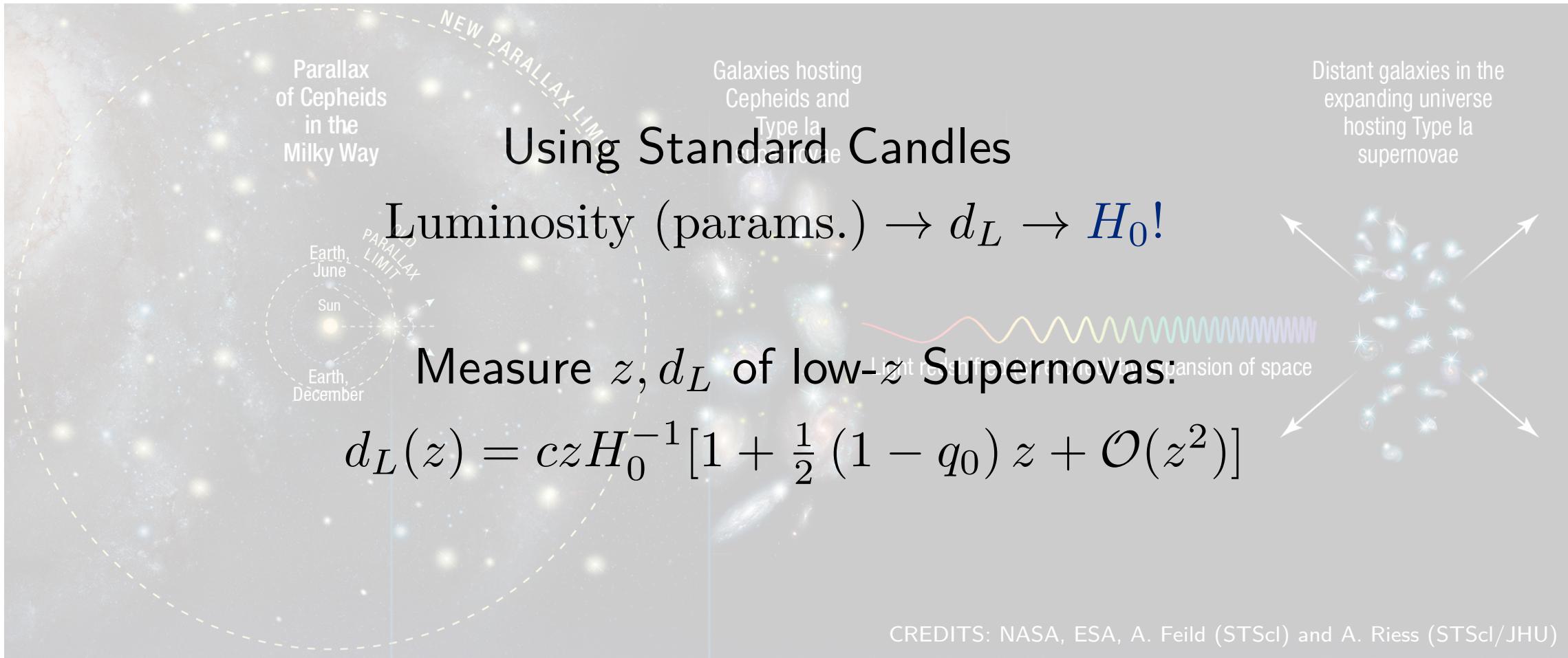
- Internal inconsistencies in the Planck  $TT$  power spectrum between frequencies (D. Spergel et al., arXiv:1312.3313)
- Tension between multipoles  $\ell < 1000$  and  $\ell \geq 1000$  (G. E. Addison et. al arXiv:1511.00055)
- Planck 2018 conclusions (Planck Collaboration arXiv:1807.06209):

“Nevertheless, **there are a number of curious “tensions”** both internal to the Planck data [...] and with some external data sets [...] **none of these**, with the exception of the discrepancy with direct measurements of  $H_0$ , **is significant at more than the  $2 - 3\sigma$  level.** Such relatively modest discrepancies generate interest, in part, because of the high precision of the Planck data set. **We could, therefore, disregard these tensions** and conclude that the 6 parameter  $\Lambda$ CDM model provides an astonishingly accurate description of the Universe”

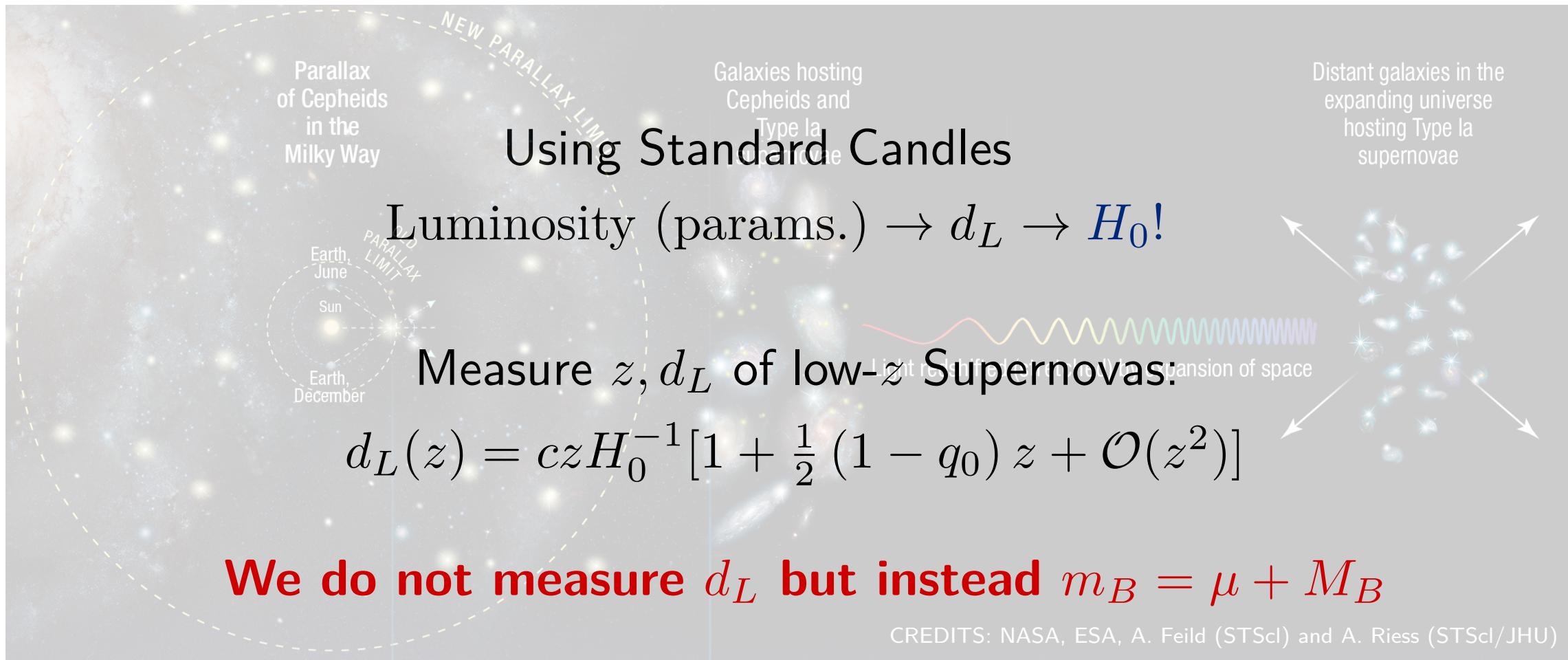
# The cosmic distance ladder



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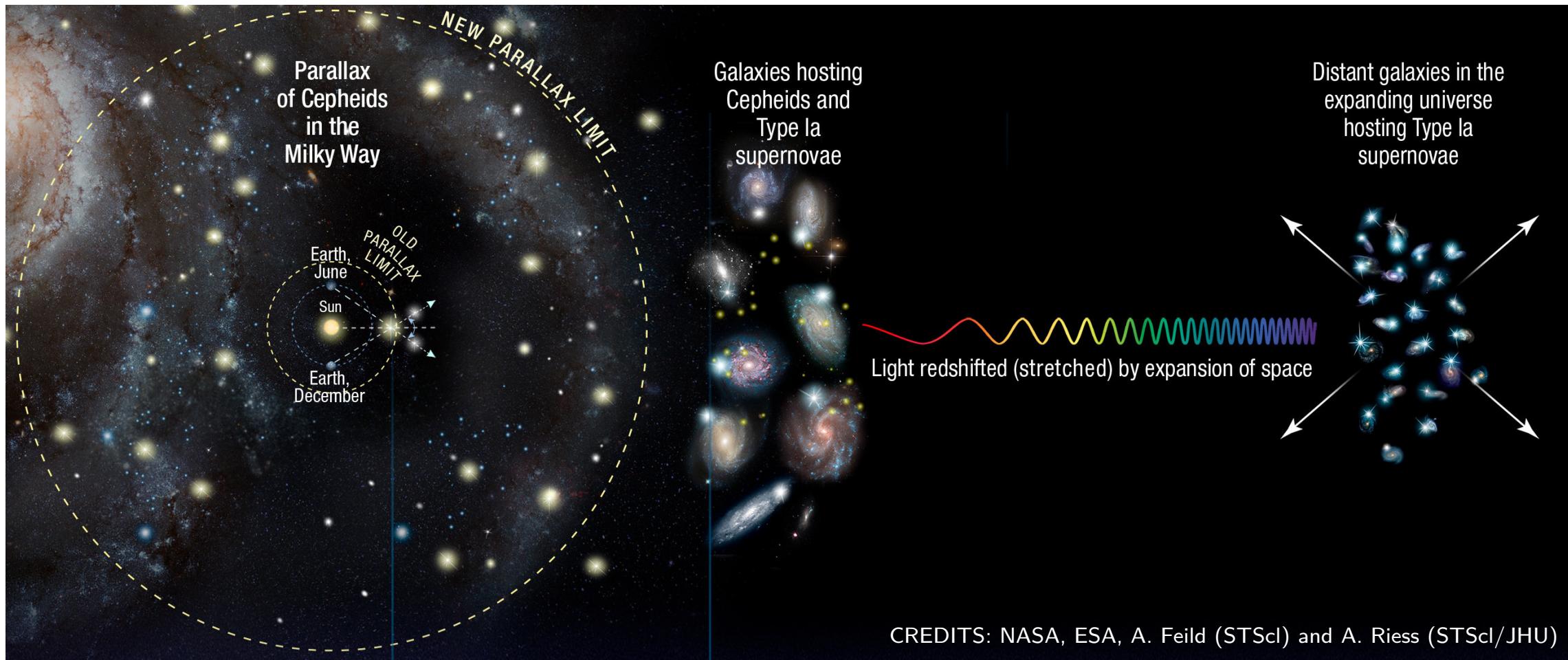
# The cosmic distance ladder



$$\mu(z) = 5 \log_{10} \frac{d_L(z)}{10pc}$$

**Supernovas need to be calibrated through  $M_B$ !**

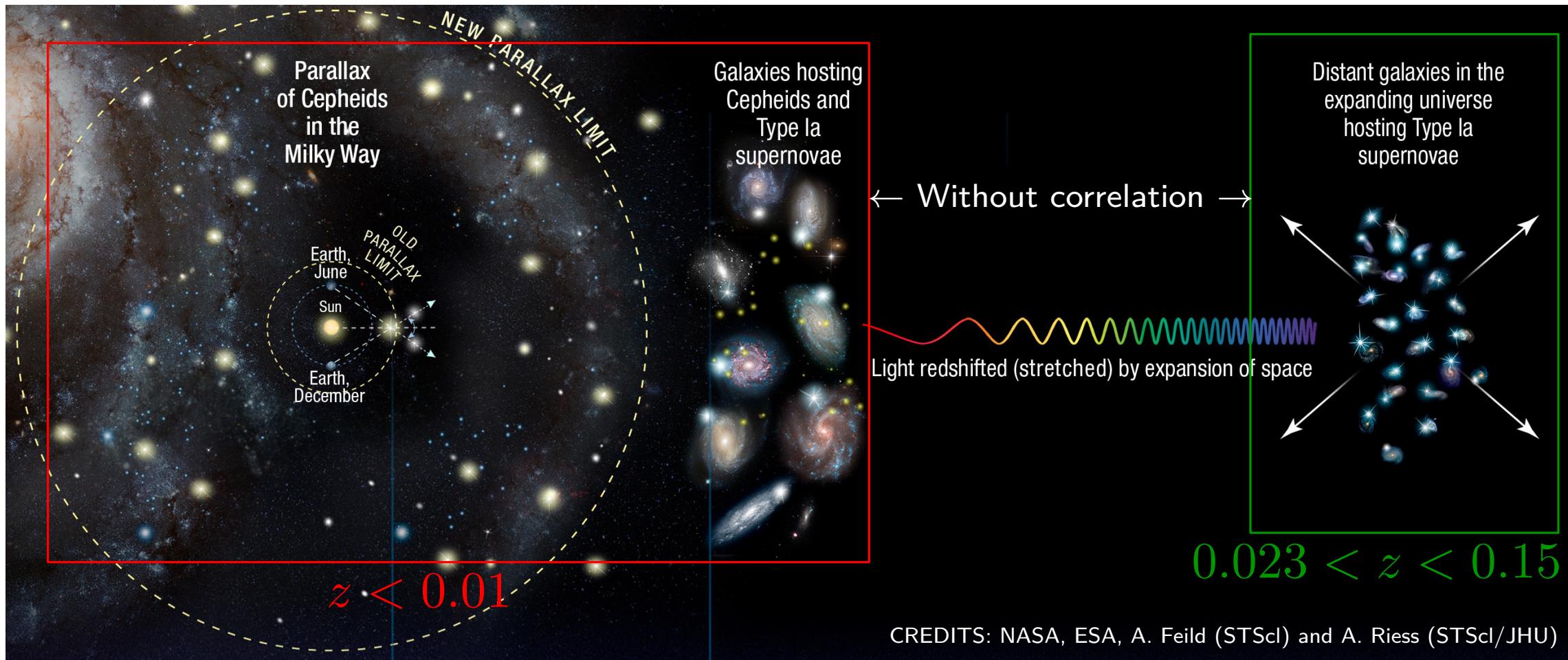
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$$\mu = m_B - M_B + \text{nuisances}$$

$$d_L = d_L(m_B, M_B, \text{nui.})$$

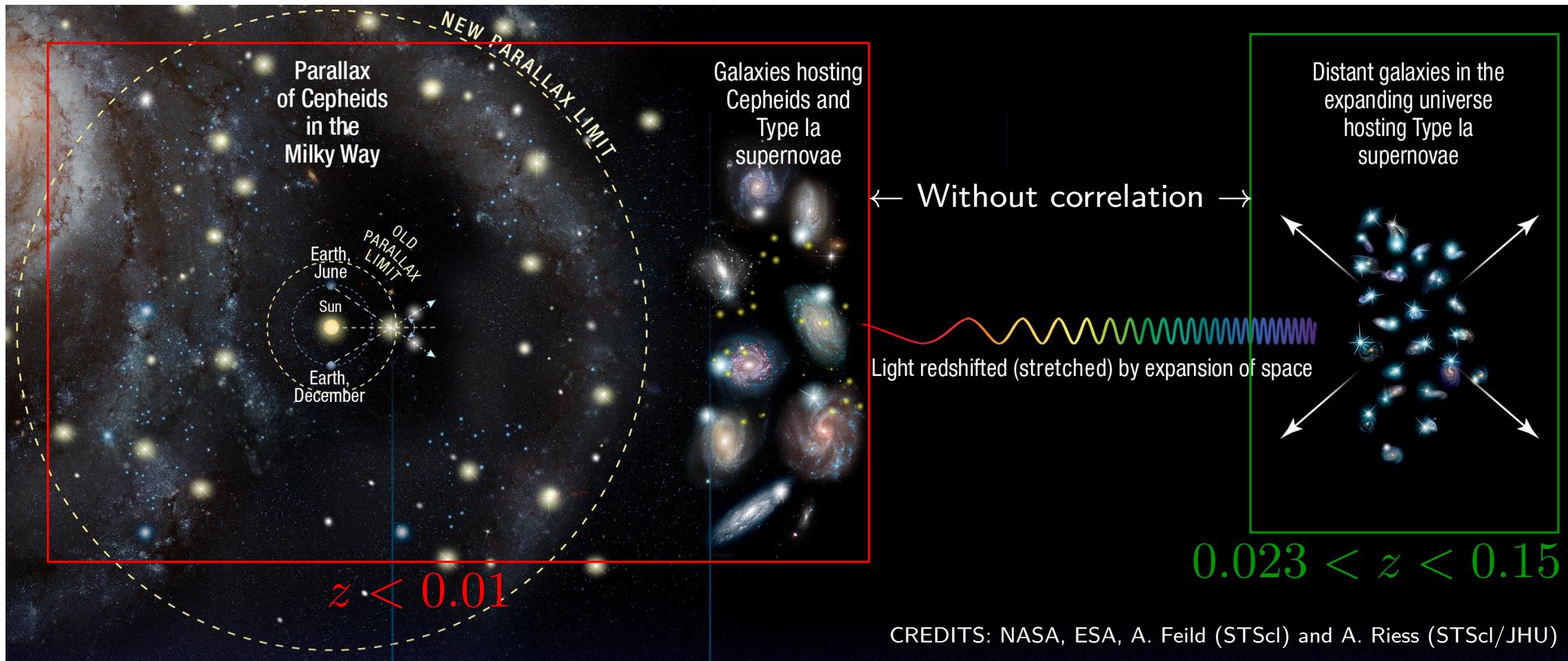
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$$\begin{aligned}\mu &= m_B - M_B + \text{nuisances} \\ d_L &= d_L(m_B, M_B, \text{nui.})\end{aligned}$$

$$d_L(z) = czH_0^{-1} [1 + \frac{1}{2} (1 - q_0) z + \mathcal{O}(z^2)]$$

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**$M_B$  is the backbone of SH0ES analysis!**

# The cosmic distance ladder



- Why Supernovas in  $0.023 < z < 0.15$ ?

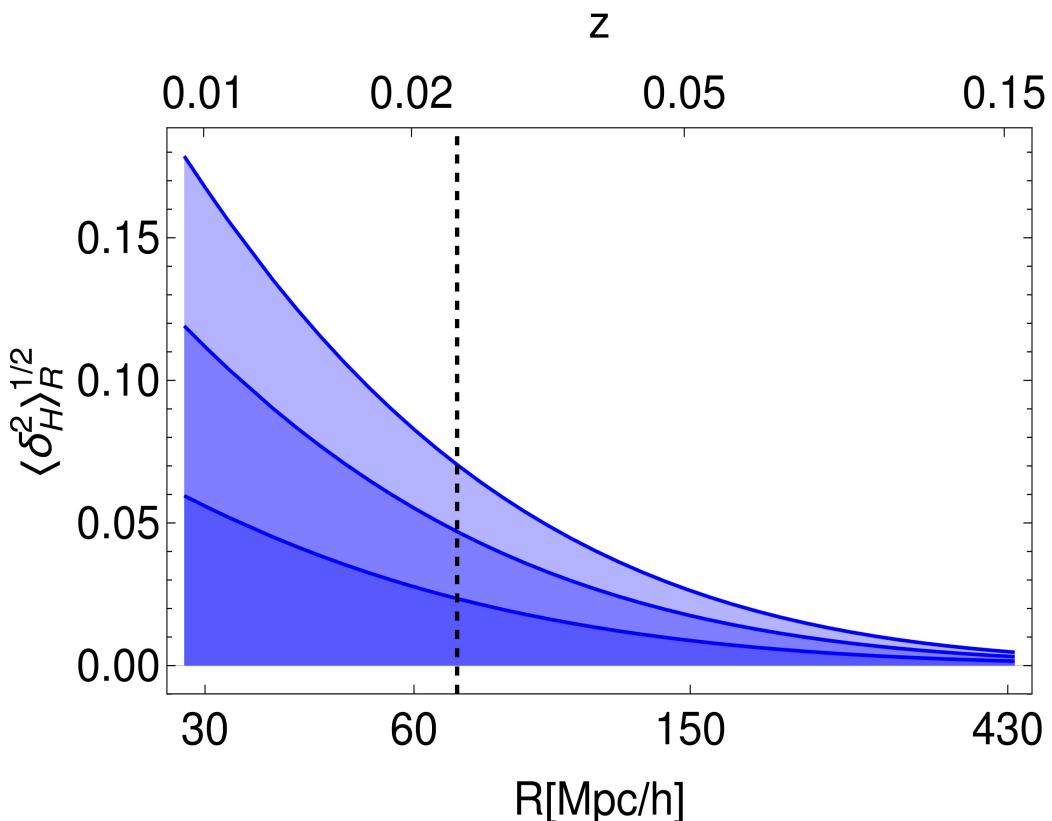
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Peculiar velocities could be non-negligible:  $H_0 r_i = H_0 r_i + v_i^r$

Linear perturbation theory:  $\langle \delta_H^2 \rangle = \frac{f(z)^2}{2\pi R^2} \int_0^\infty dk P(k) [(kR) \mathcal{L}(kR)]^2$



D.C and V. Marra, arXiv:1805.09900

$\Lambda$ CDM ( $w$  &  $\gamma$  extensions) predicts:

For  $0.023 < z < 0.15$ :

$$\sigma_{cv} \approx 0.88 \text{ km s}^{-1} \text{ Mpc}^{-1} (1.2\%)$$

For  $0.01 < z < 0.15$ :

$$\sigma_{cv} \approx 1.5 \text{ km s}^{-1} \text{ Mpc}^{-1} (2\%)$$

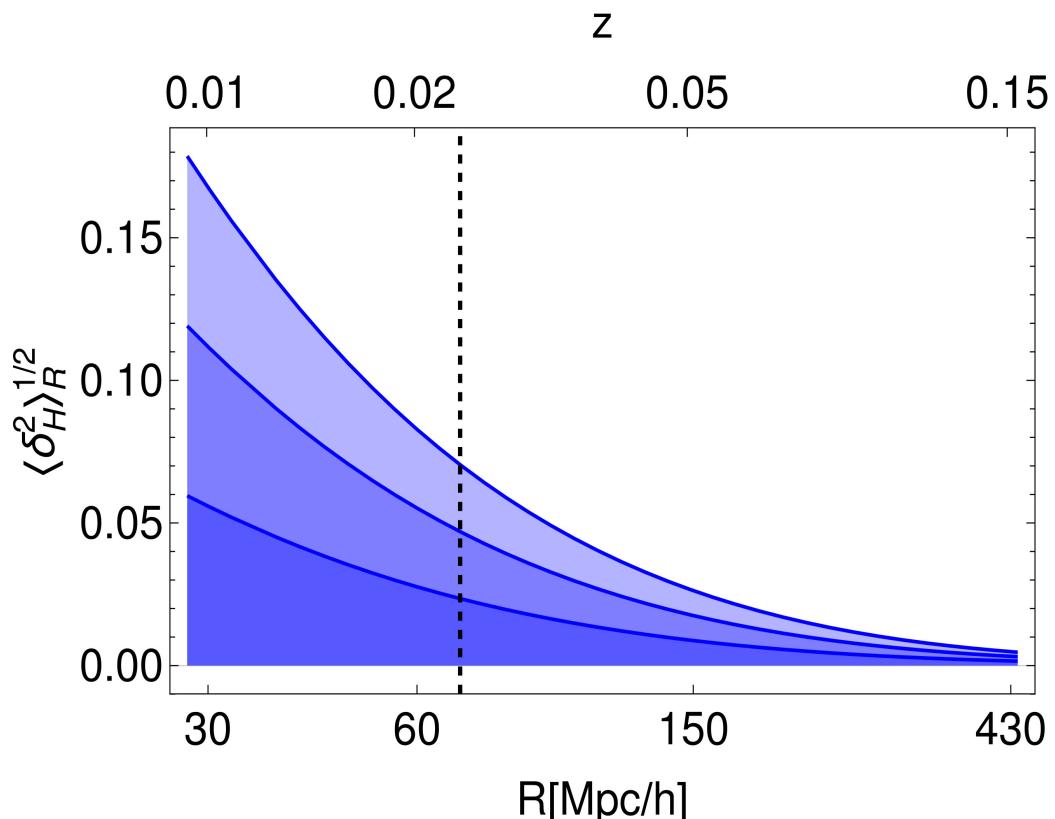
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**Not enough** to explain  $H_0$  tension!

# The cosmic distance ladder



- Why Supernovas in  $0.023 < z < 0.15$ ?
  - "Cosmic variance" on  $H_0$  (E. L. Turner et al., Astron. J.103, p.1427 (1992) )
  - Deviation from FLRW metric: 2.4% (0.010) or 1.3% (0.023) (V. Marra et al., arXiv:1303.3121)
  - $\Lambda$ CDM N-body simulations: 0.8% (R. Wojtak et al., arXiv:1312.0276), 1.1% (I. Oddershov et al., arXiv:1407.7364)
  - Sample variance:  $0.31 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (0.4%) (Wu and Huterer arXiv:1706.09723)
  - Local void constrained by supernovas: 0.6% (W. D'Arcy Kenworthy et al. arXiv:1901.08681)

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**Consensus: local structures does not explain  $4.2\sigma$  discrepancy!**

# The cosmic distance ladder



- Why Supernovas in  $0.023 < z < 0.15$ ?

$\mathcal{L}$ : likelihood  
 $p$ : prior

$$d_L^{\text{SN}}(m_B, M_B, \text{nui.})$$

↑  
confront!

$$d_L(z) = czH_0^{-1} [1 + \frac{1}{2}(1 - q_0)z + \frac{1}{6}(1 - q_0 - 3q_0^2 + j_0)z^2 + \mathcal{O}(z^3)]$$

Bayes' theorem:

$$f(H_0|\text{SN}) = \mathcal{E}^{-1} \int dM_B dq_0 dj_0 p(q_0)p(j_0) p(M_B) \mathcal{L}(\text{params}|\text{SN})$$

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**Higher  $z$  means higher orders:**  $+s_0, \ell_0$

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**SH0ES assumes:**  $q_0 = -0.55$  &  $j_0 = 1$ .

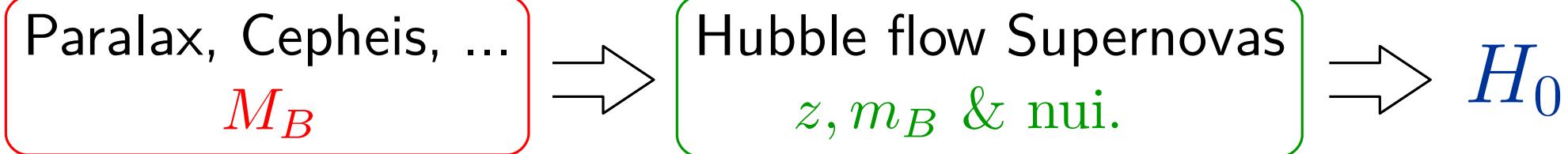
**Model-independent determination?**

# Absolute magnitude of Supernovas



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**Demarginalization:** Assuming a Gaussian dist.  $\mathcal{N}(\tilde{M}_B, \sigma_M^2)$

$$\begin{aligned}\tilde{H}_0 &= \frac{\ln 10}{5} \left[ \tilde{M}_B + \frac{\ln 10}{5} \left( \sigma_M^2 + \frac{1}{S_0} - \frac{S_1}{S_0} \right) \right] \\ \sigma_H &= \frac{\ln 10}{5} \sqrt{\sigma_M^2 + \frac{1}{S_0}}\end{aligned}$$

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$$f(H_0|\text{SN}) = \mathcal{E}^{-1} \int dM_B f(M_B) \mathcal{L}(\text{params}|\text{SN})$$



**Deconvolution:**  $\log_{10} H_0 = 0.2M_B + a_B + 5$

$$\tilde{H}_0 = \frac{\ln 10}{5} \left[ \tilde{M}_B + 5a_B + 25 \right]$$

$$\sigma_H = \frac{\ln 10}{5} \sqrt{\sigma_M^2 + 25\sigma_a^2}$$

# Absolute magnitude of Supernovas



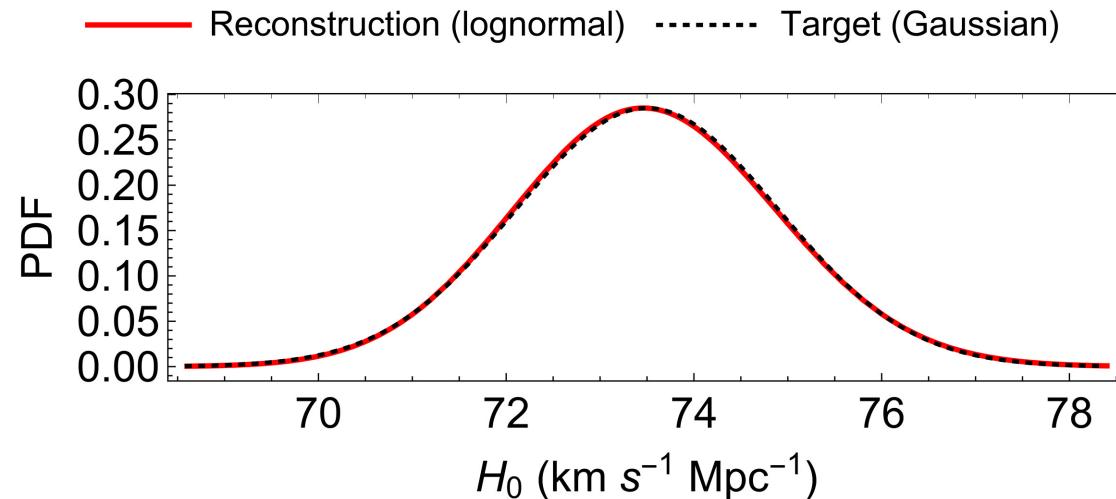
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Supercal, Scolnic D. M. et al. arXiv:1710.00845

	$M_B$	$\sigma_M$
Dem marginalization	-19.2421	0.0375
Error propagation	-19.2411	0.0375
Deconvolution	-19.2414	0.0375

Pantheon, Scolnic D. M. et al. arXiv:1710.00845

	$M_B$	$\sigma_M$
Dem marginalization	-19.2435	0.0373
Error propagation	-19.2424	0.0373
Deconvolution	-19.2428	0.0373



# Absolute magnitude of Supernovas



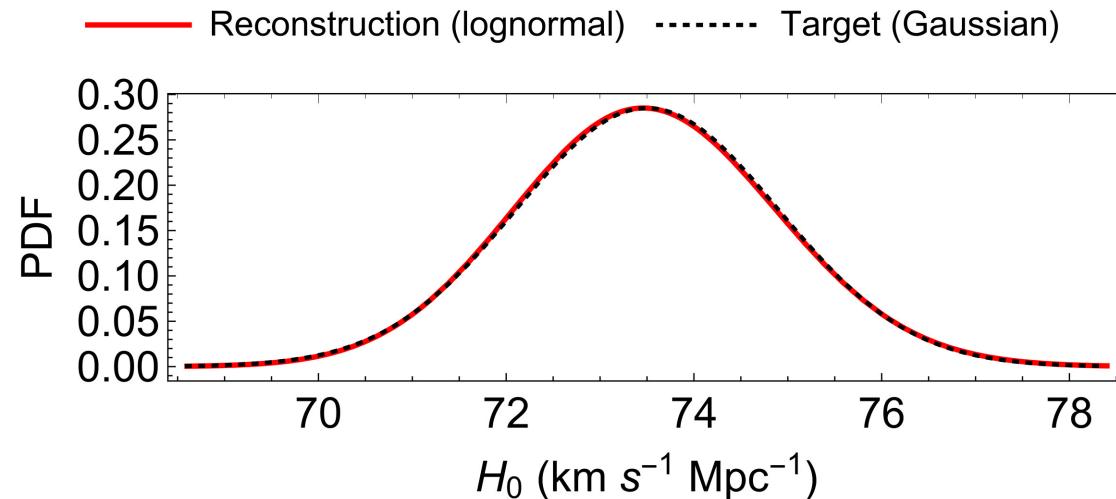
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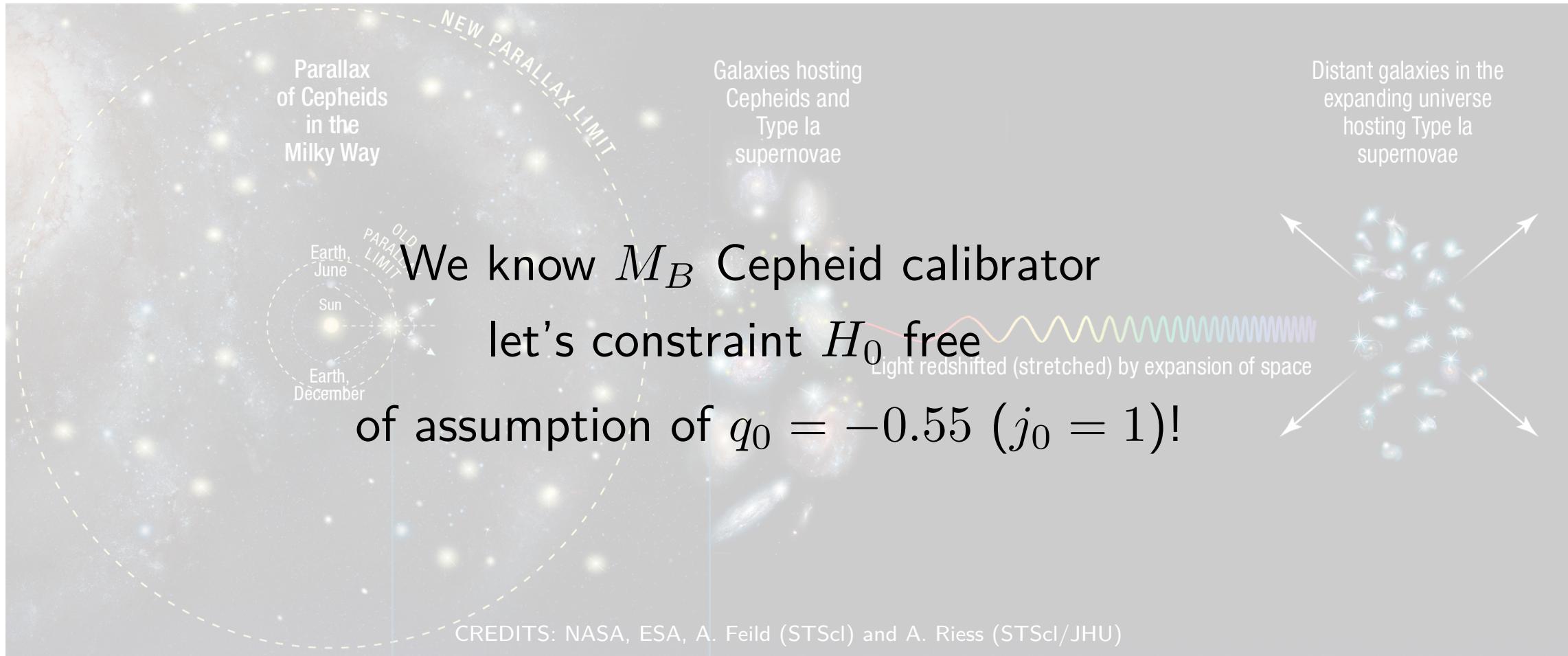
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	$M_B$	$\sigma_M$
Dem marginalization	-19.2435	0.0373
Error propagation	-19.2424	0.0373
Deconvolution	-19.2428	0.0373



$H_0$  prior translated in  $M_B$  prior!

# Joint $H_0$ - $q_0$ constraint



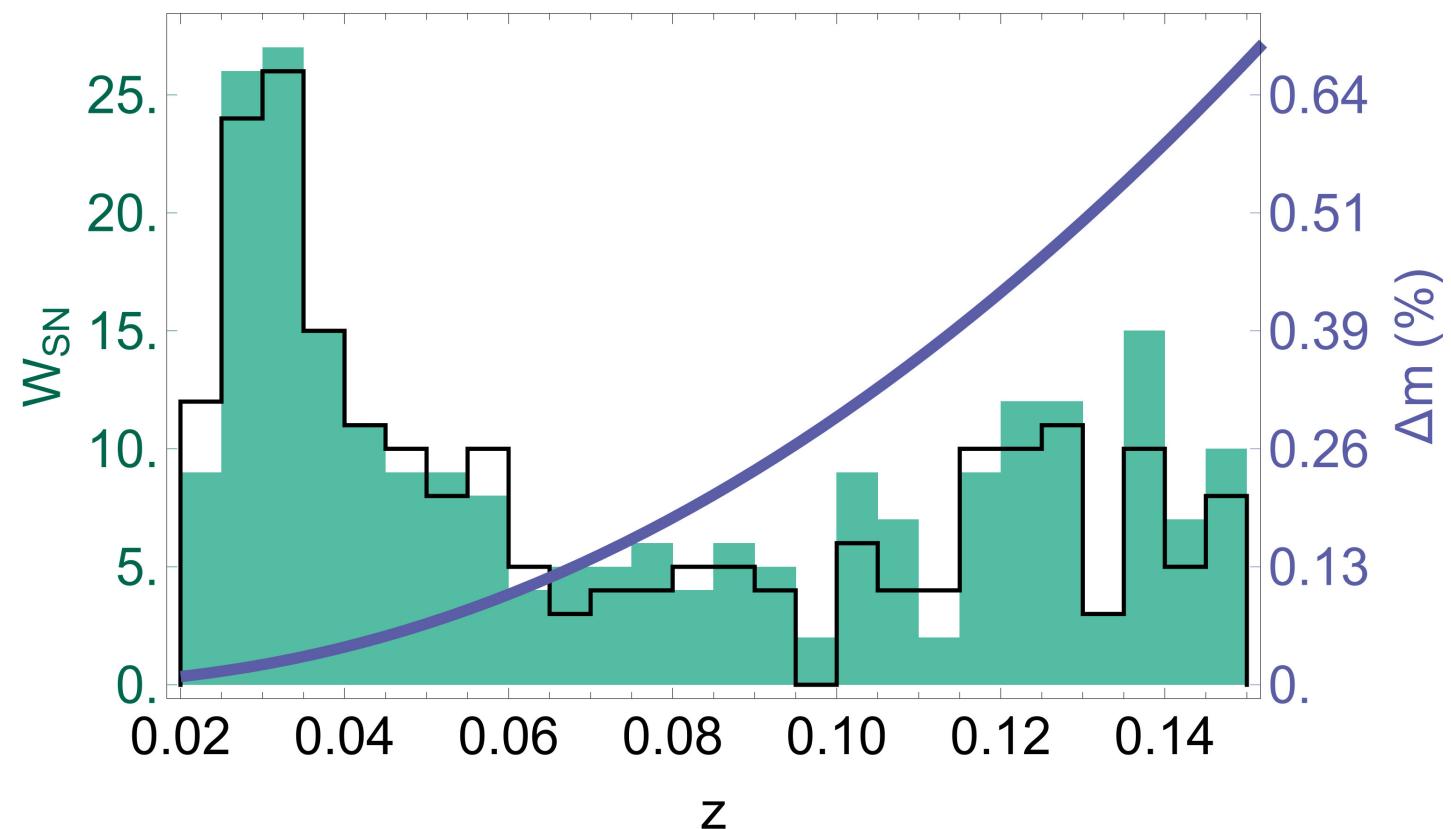
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We assume:

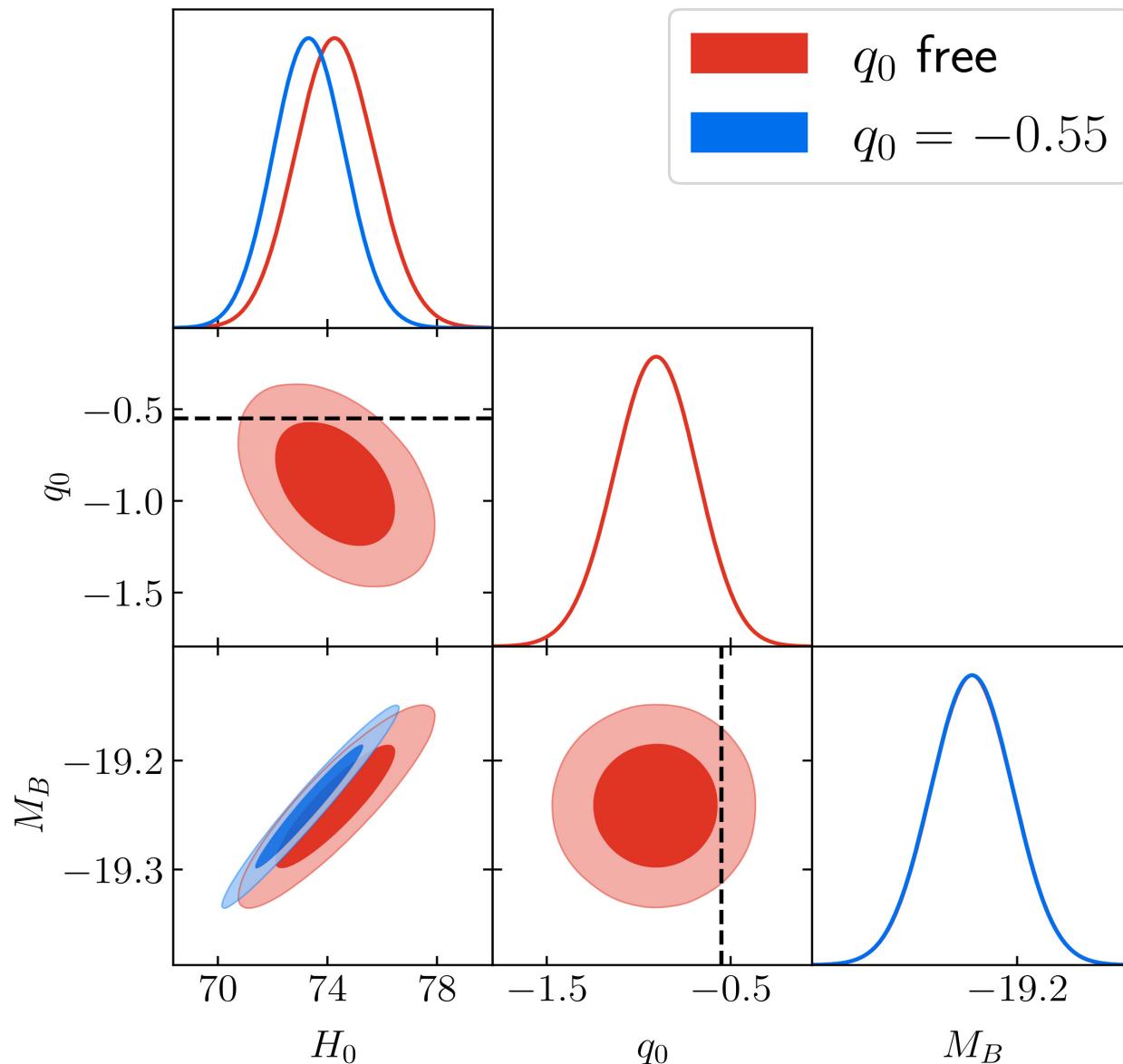
$$d_L(z) = czH_0^{-1}[1 + \frac{1}{2}(1 - q_0)z]$$

$$f(H_0, q_0 | \text{SN}) = \mathcal{E}^{-1} \int dM_B f(H_0) f(q_0) f(M_B) \mathcal{L}(\text{params} | \text{SN})$$



D.C and V. Marra, arXiv:1906.11814

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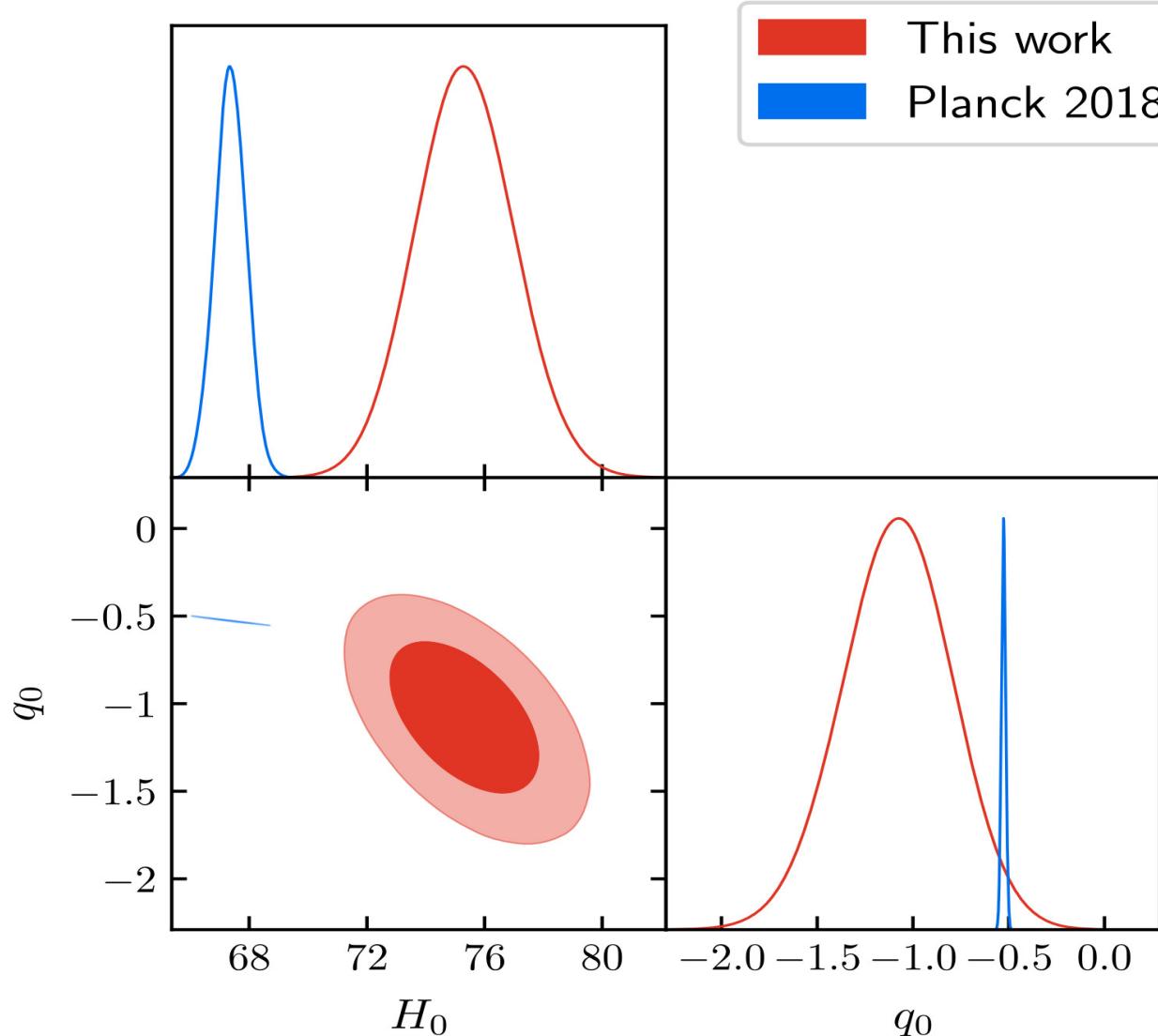


D.C and V. Marra, arXiv:2101.08641

parameter	$\mu_i \pm \sigma_i$	$C_{ij}$
$H_0$ [km/s/Mpc]	$74.30 \pm 1.45$	1 -0.41
$q_0$	$-0.91 \pm 0.22$	-0.41 1

1.2 km s<sup>-1</sup> Mpc<sup>-1</sup> higher than SH0ES

# Joint $H_0$ - $q_0$ constraint



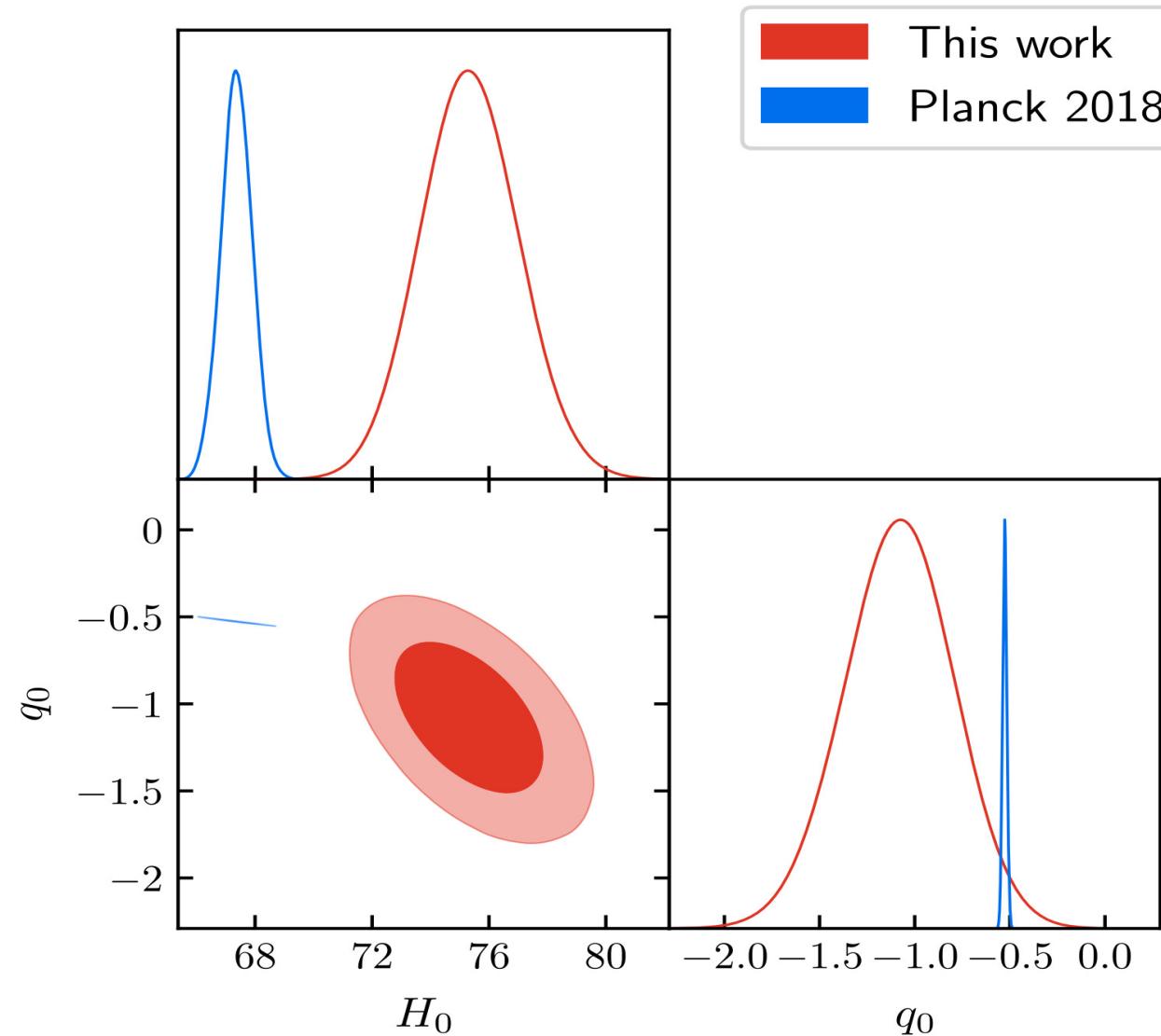
D.C and V. Marra, arXiv:2101.08641

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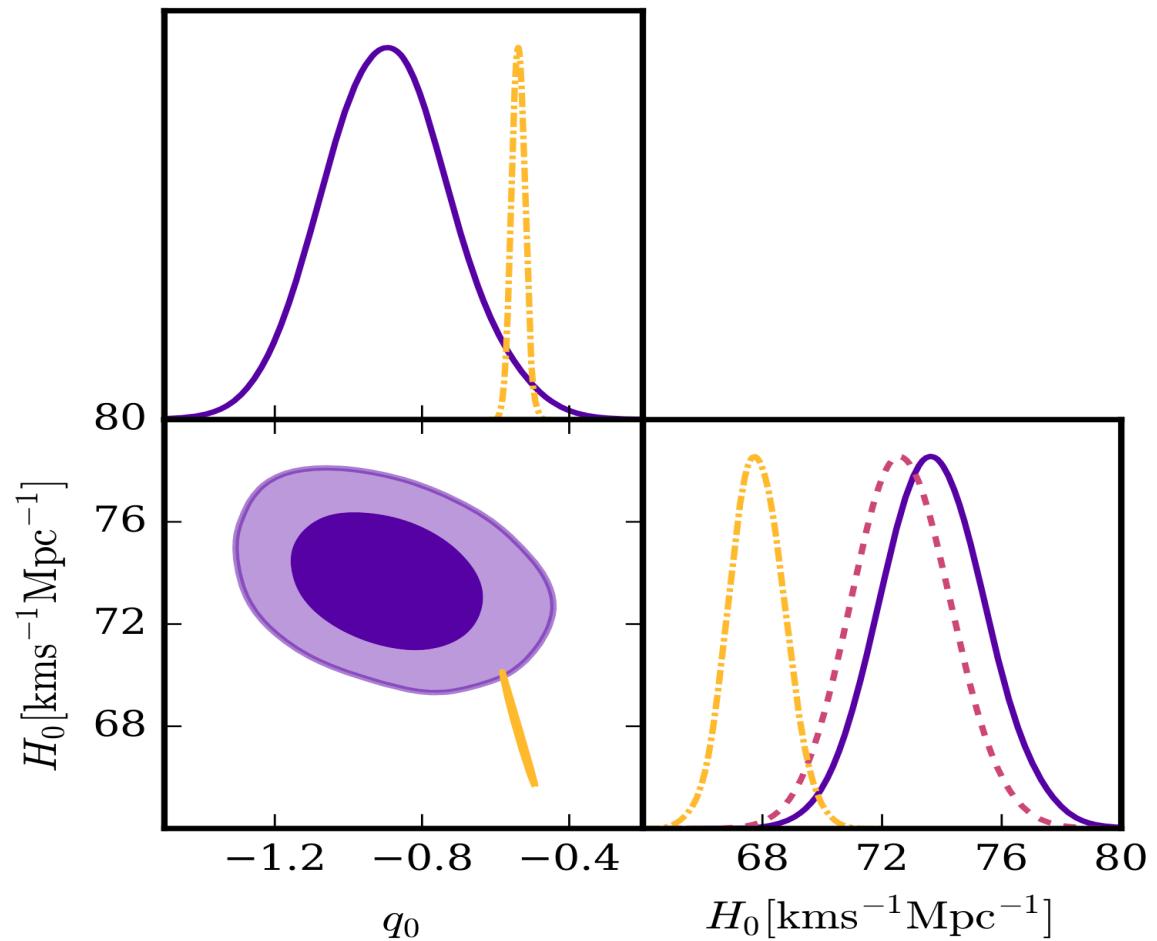
$1.2 \text{ km s}^{-1} \text{ Mpc}^{-1}$  higher than SH0ES

$H_0$  :  $4.5\sigma$  discrepancy with CMB  
 $q_0$  :  $\sim 2\sigma$  "curiosity" with CMB

# Joint $H_0$ - $q_0$ constraint



Feeney et al. (arXiv:1707.00007)



# The cosmic distance ladder



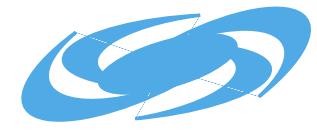
- Sub-luminous low metallicity Cepheids underestimates errors (G. Efstathiou, arXiv:1311.3461)
- Bayesian hierarchical model of the local distance ladder: joint analysis leads to  $H_0 = 72.72 \pm 1.67$  marginalizing over  $\sim 3000$  parameters (Feeney et al., arXiv:1707.00007)
- Blind re-analysis: in agreement with SH0ES analysis, no human bias detected (B. R. Zhang et al., arXiv:1706.07573)
- Tension among anchors (G. Efstathiou, arXiv:2007.10716)
- Local Hole  $\sim 150 h^{-1}$  Mpc reduces  $\sim 1.8\%$  the local Hubble constant. (B. R. Zhang et al., arXiv:1810.02595)
- Analysis of simulated data ( $0.01 < z < 2.3$ ) shows that the assumption on the DE model produces  $\Delta H_0 = 0.47$ . (S. Dhawan et al., arXiv:2001.09260)

# Inverse distance ladder

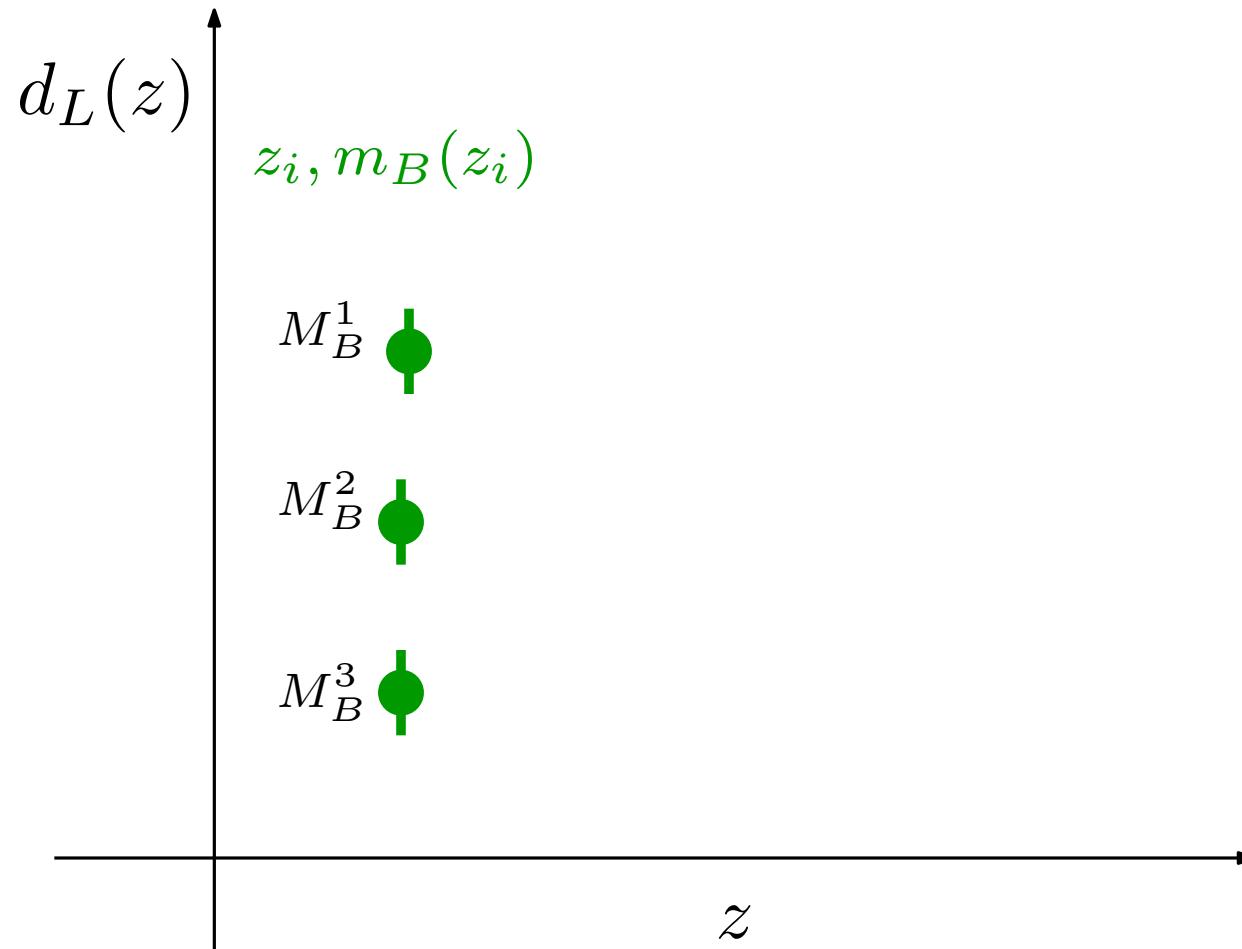


**CMB** and **BAO**(and others probes to calibrate **Supernovas**)

# Inverse distance ladder



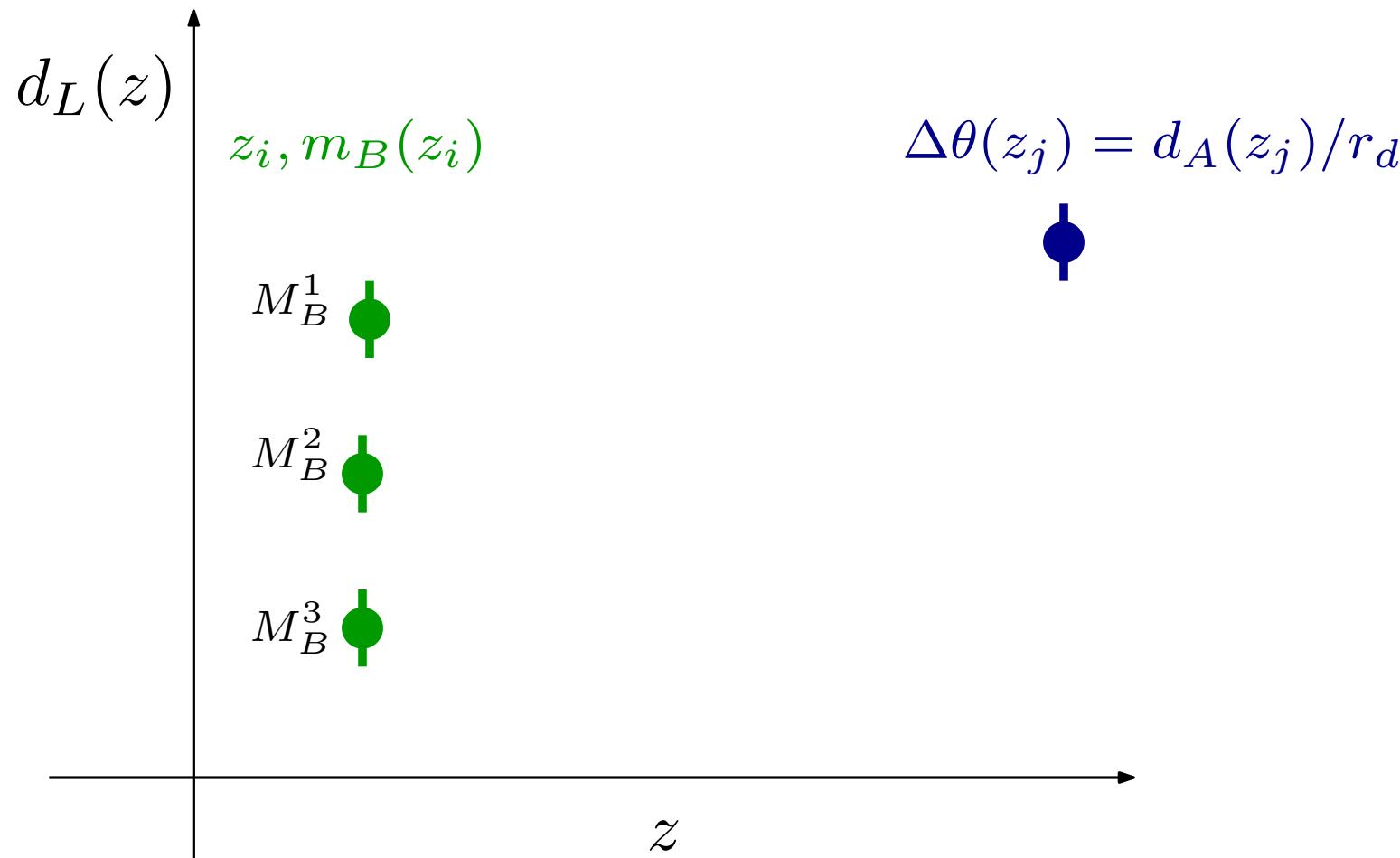
**CMB** and **BAO**(and others probes to calibrate **Supernovas**)



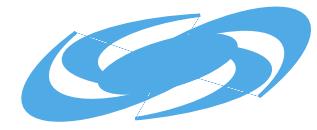
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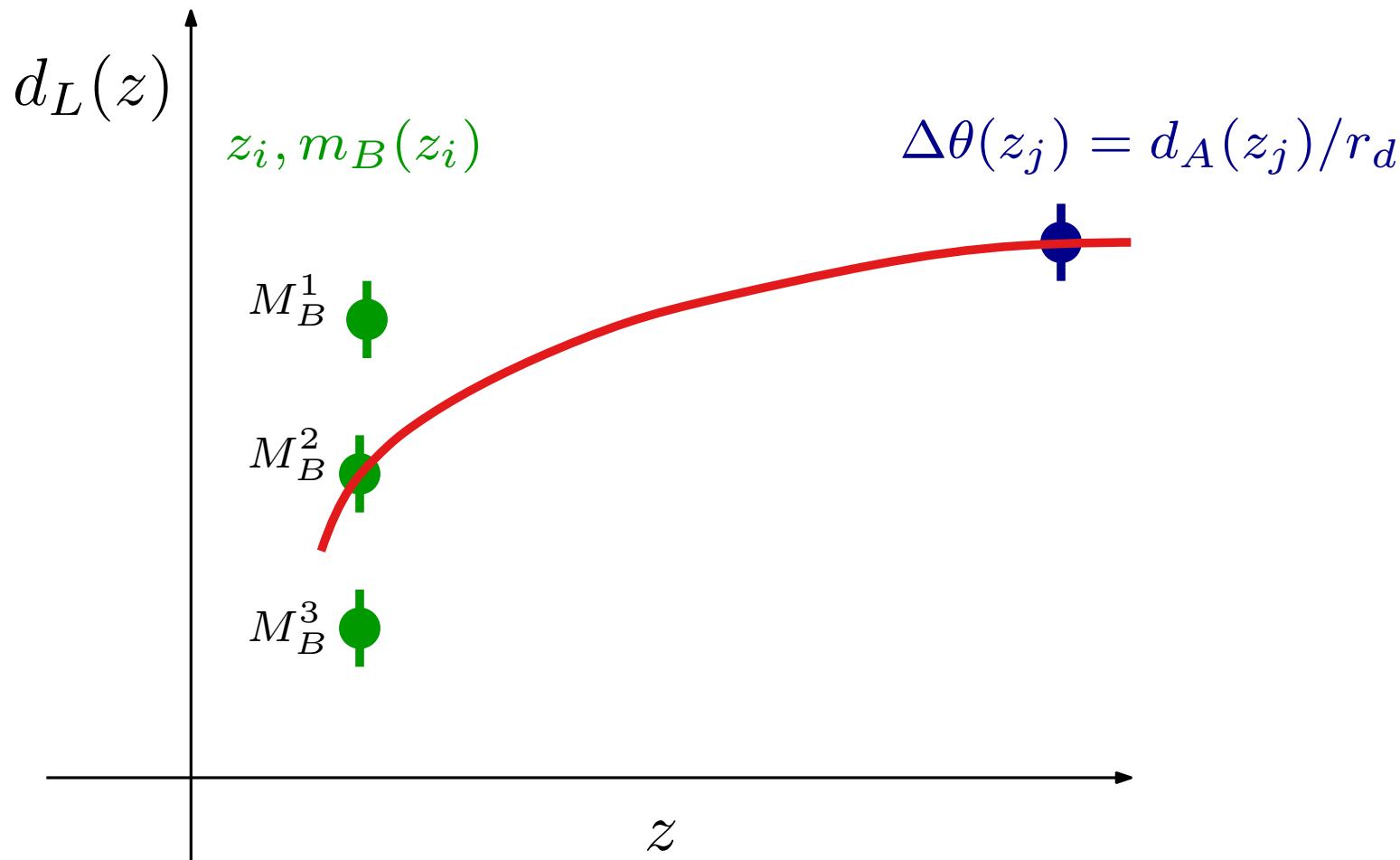
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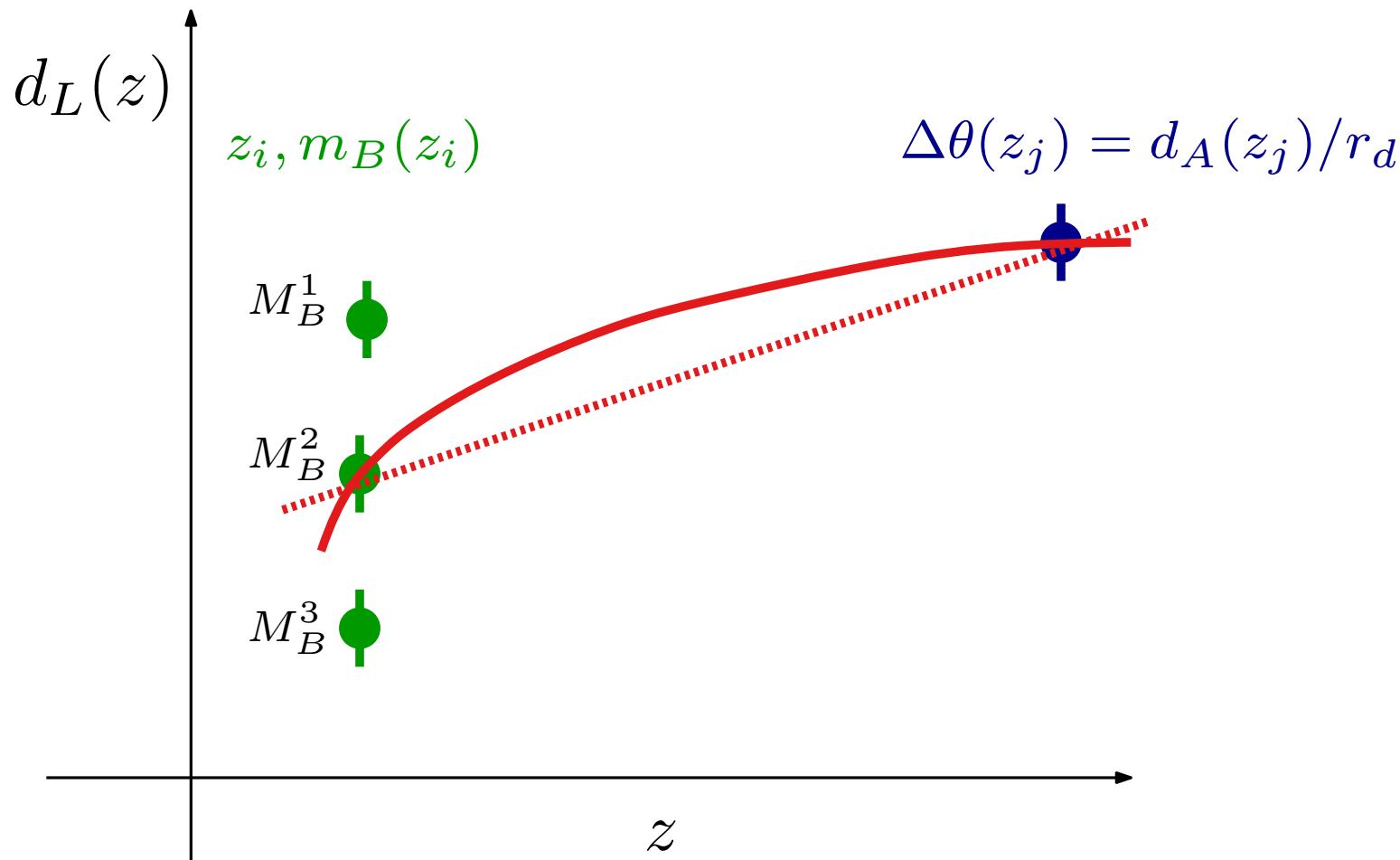
**CMB** and **BAO**(and others probes to calibrate **Supernovas**)



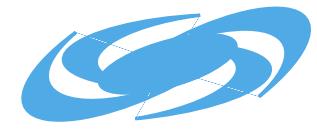
# Inverse distance ladder



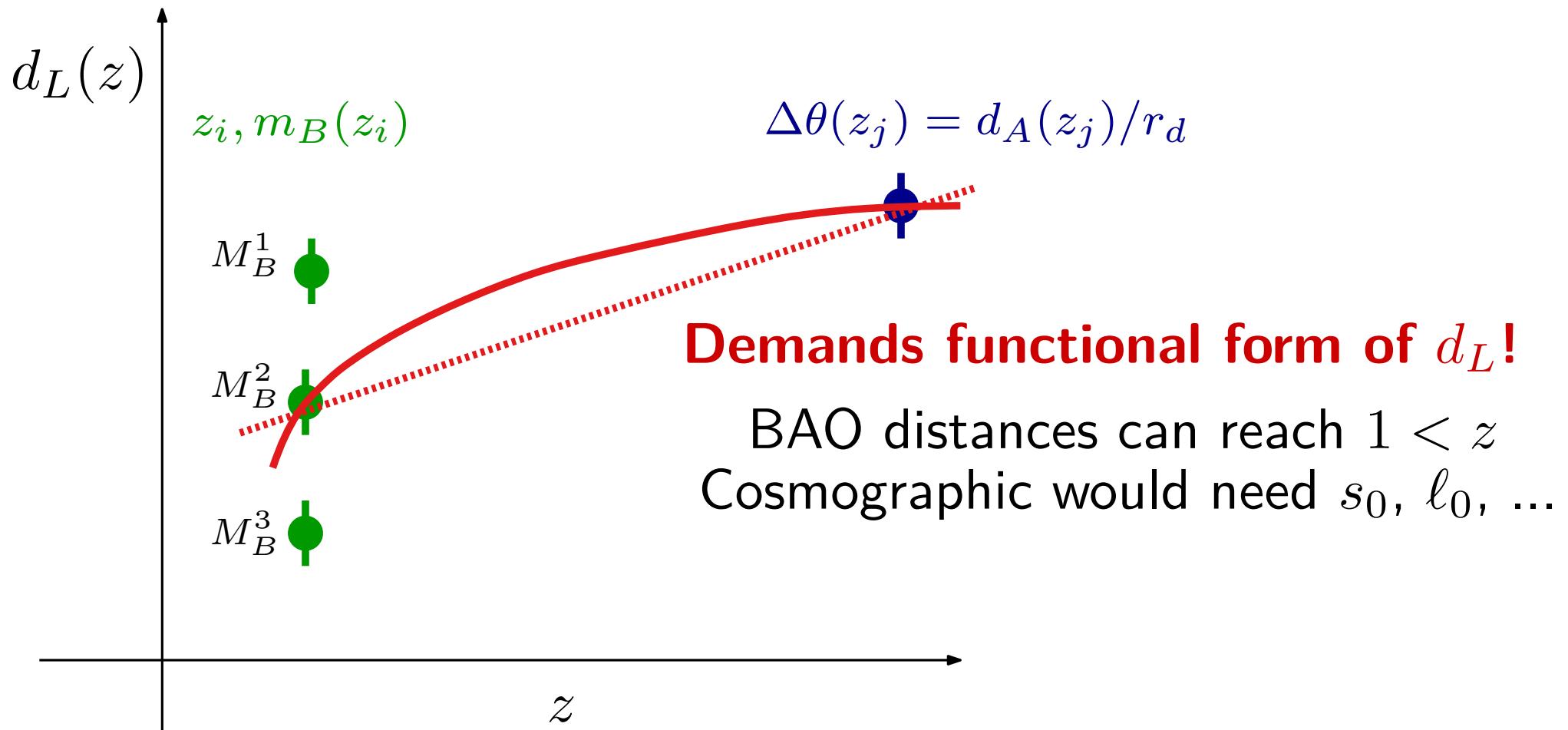
**CMB** and **BAO**(and others probes to calibrate **Supernovas**)



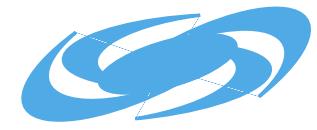
# Inverse distance ladder



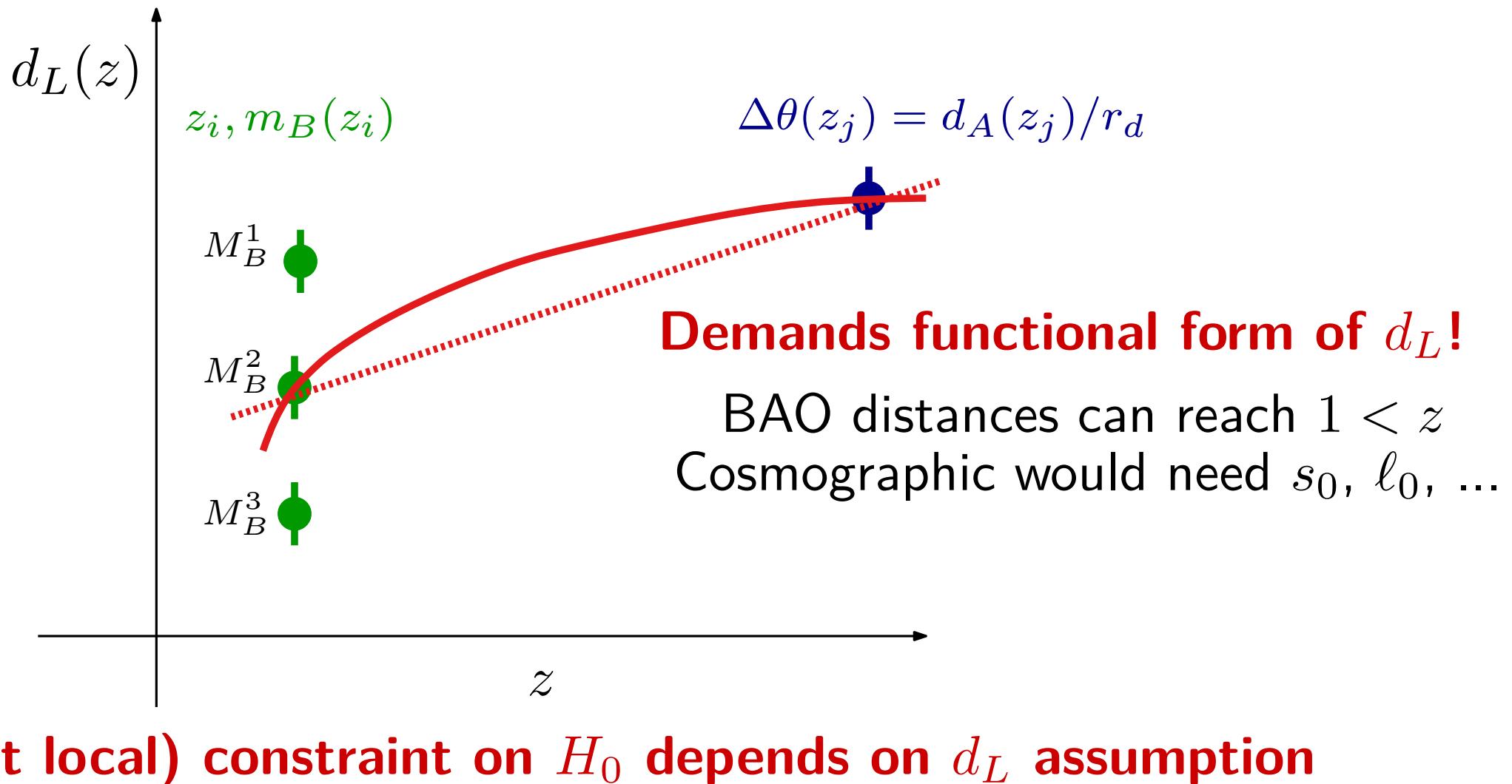
CMB and BAO (and others probes to calibrate Supernovas)



# Inverse distance ladder



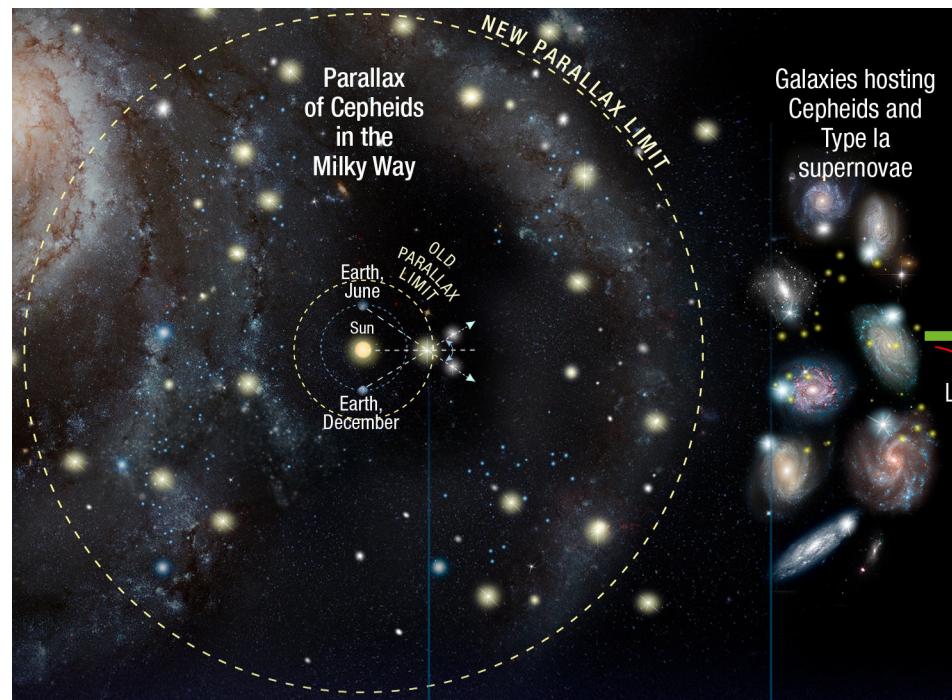
CMB and BAO (and others probes to calibrate Supernovas)



# Inverse distance ladder



**CMB** and **BAO**(and others probes to calibrate **Supernovas**)

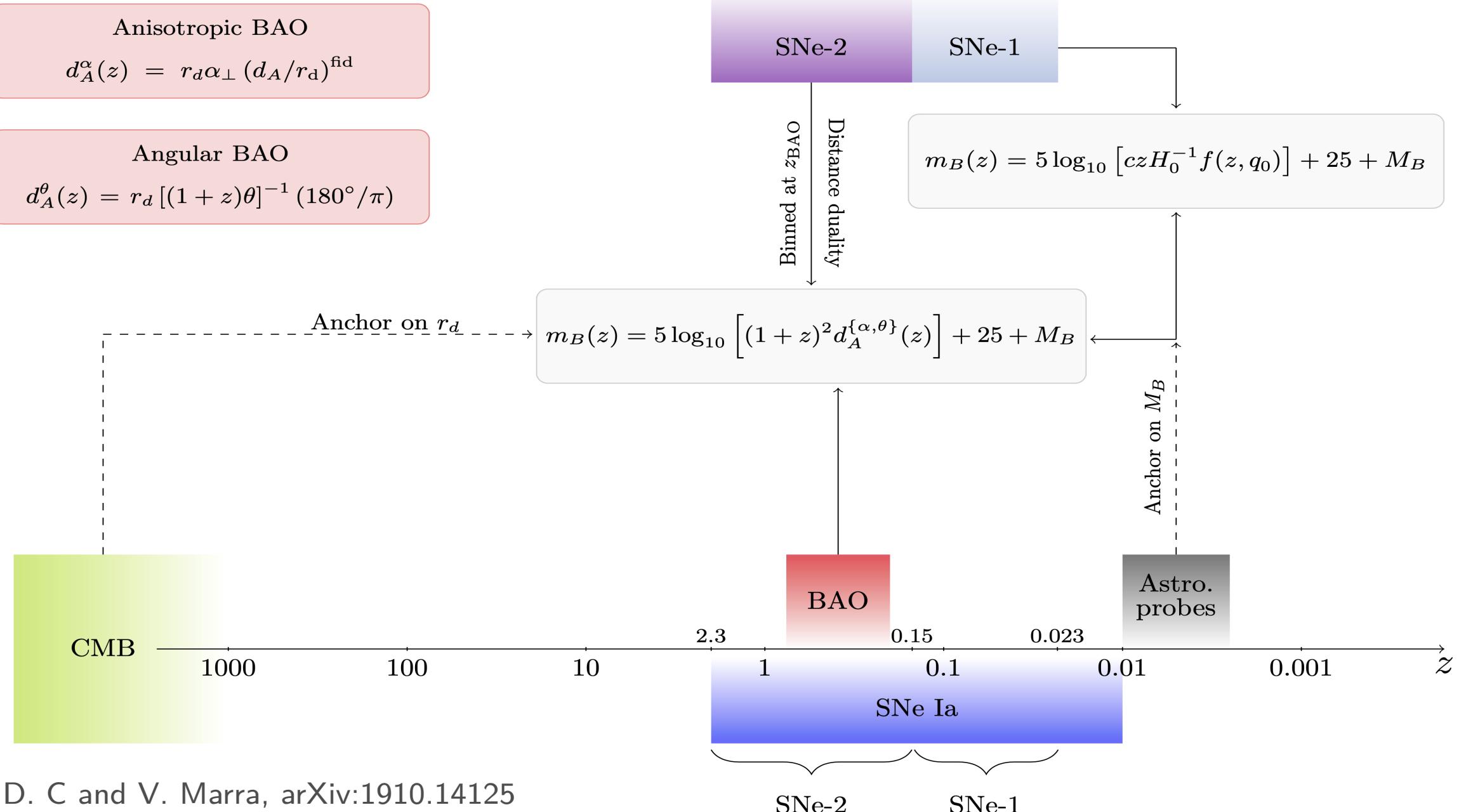


Don't care about  $d_L$  beyond  $z = 0.15$

Cepheids & Supernovas  
at same redshift

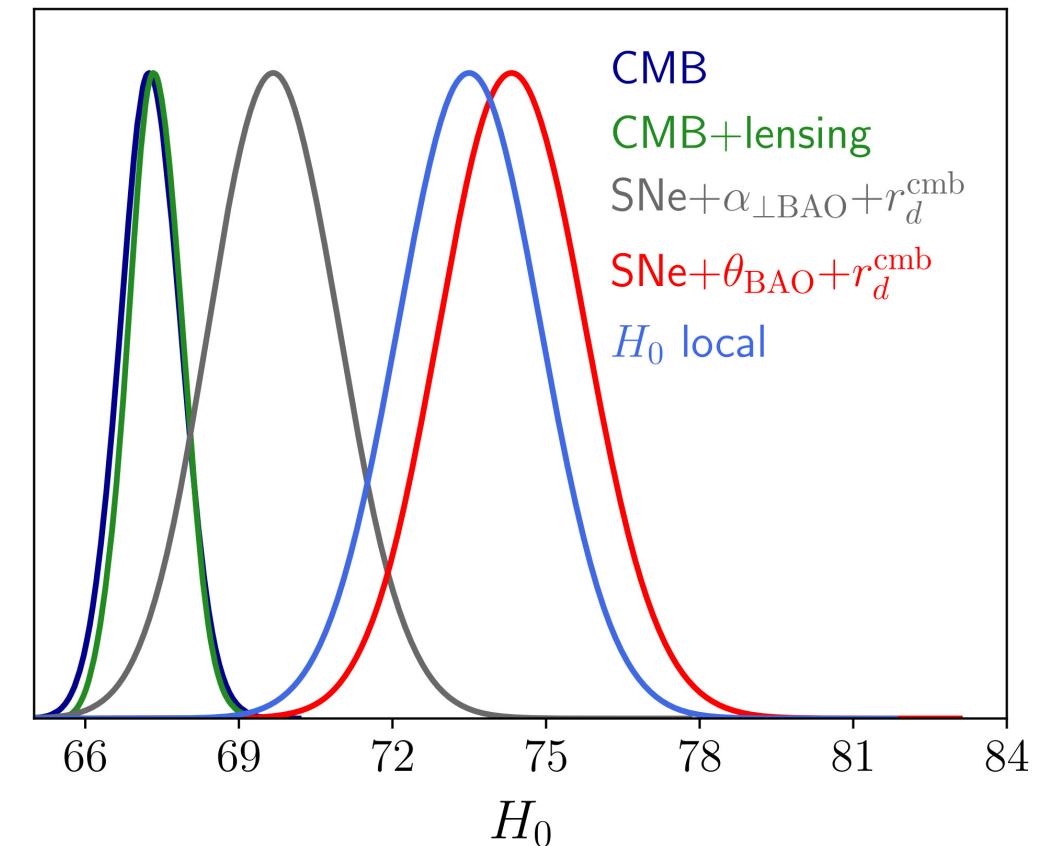
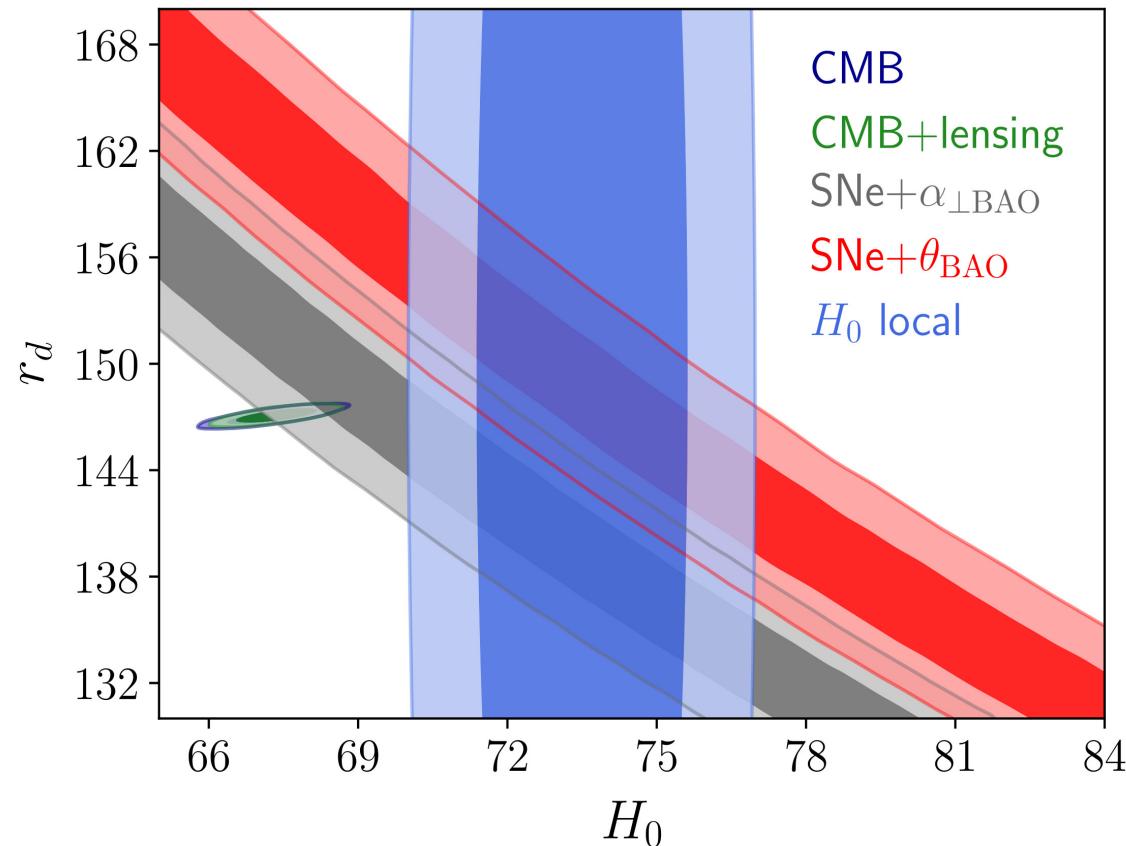
$$M_B = m_B - 5 \log_{10} \frac{d_L}{10pc}$$

# Inverse distance ladder



D. C and V. Marra, arXiv:1910.14125

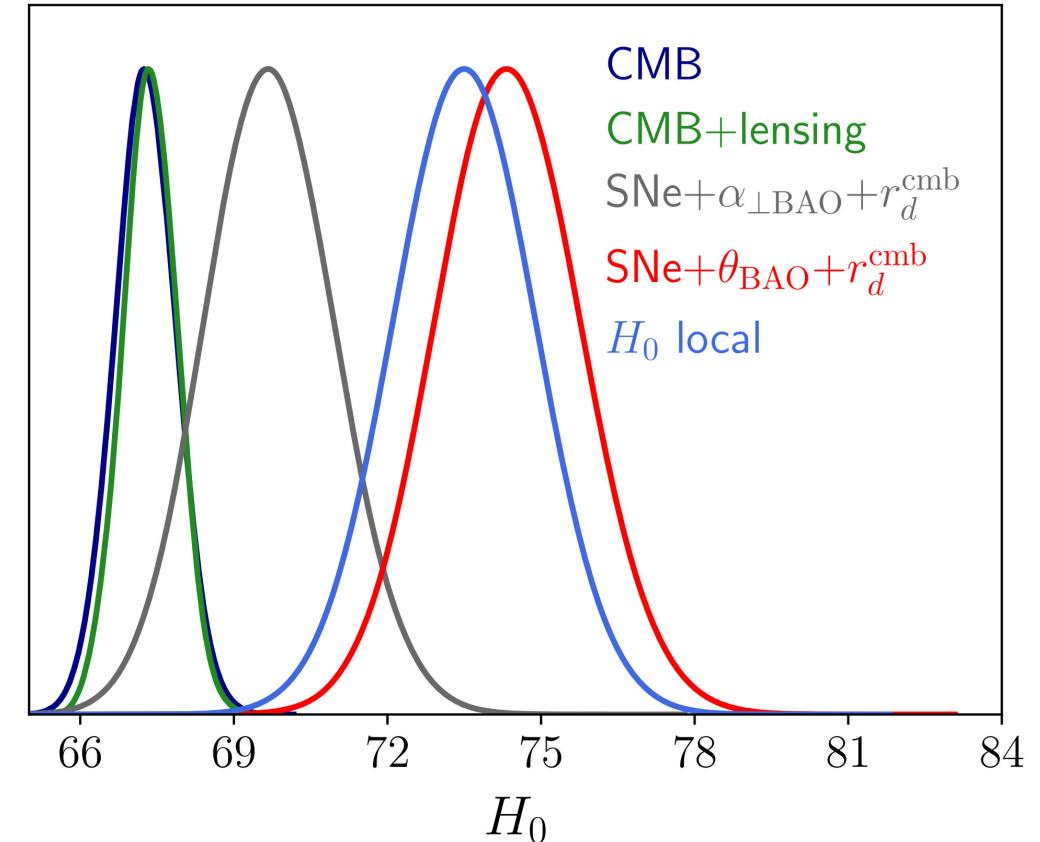
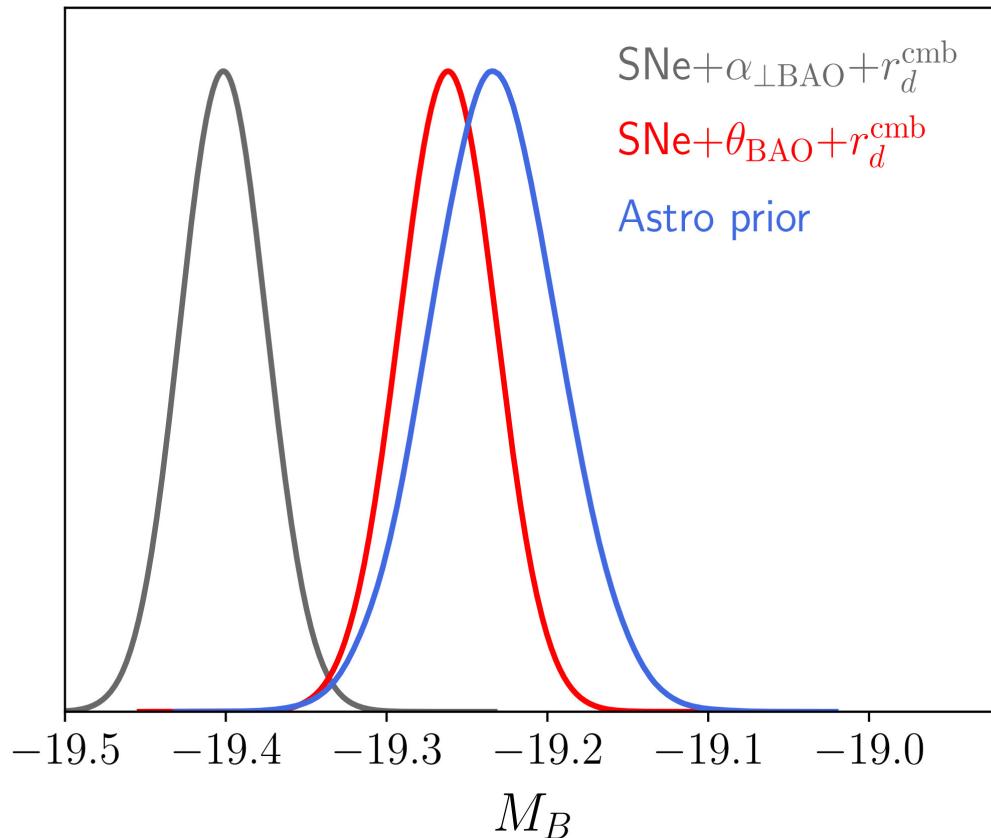
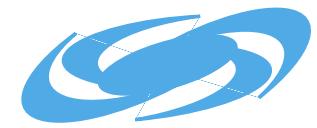
# Inverse distance ladder



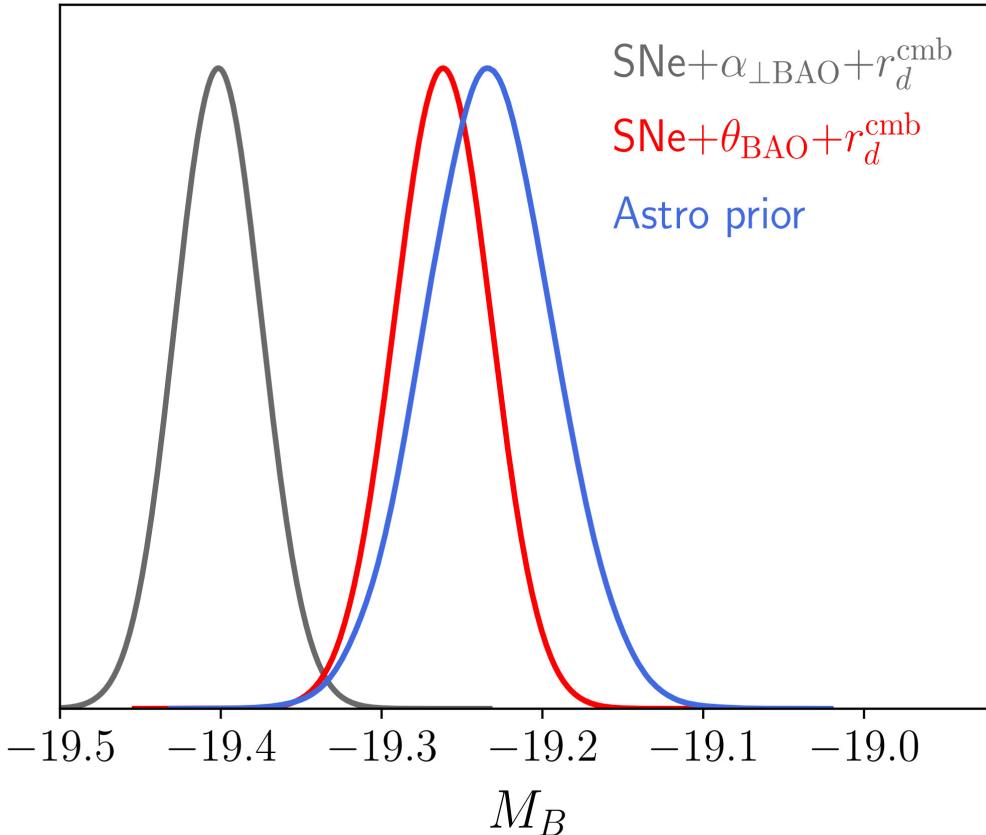
$\alpha_{\perp\text{BAO}}$  : Power spectrum reconstruction and full-shape analyses (BOSS collaboration)

$\theta_{\text{BAO}}$  : parametric fit to the angular 2-point correlation function  $\omega(\theta)$

# Inverse distance ladder



# Inverse distance ladder



**Tension on  $M_B$ !  
(assuming  $\alpha_{\perp BAO}$  and CMB)**

In agreement with analysis from P. Lemos et al., arXiv:1806.06781

## Tension between $\alpha_{\perp BAO}$ and $\theta_{BAO}$

Local deceleration parameter  $< -1$

Type of analysis	Constraint on $q_0$
SNe+ $\alpha_{\perp BAO}$	$q_0 = -1.08^{+0.29}_{-0.29}$
SNe+ $\theta_{BAO}$	$q_0 = -1.11^{+0.29}_{-0.29}$
SNe+ $\alpha_{\perp BAO} + r_d^{\text{cmb}}$	$q_0 = -1.09^{+0.29}_{-0.29}$
SNe+ $\theta_{BAO} + r_d^{\text{cmb}}$	$q_0 = -1.11^{+0.29}_{-0.29}$
SNe+ $\alpha_{\perp BAO} + M_B$	$q_0 = -1.08^{+0.29}_{-0.29}$
SNe+ $\theta_{BAO} + M_B$	$q_0 = -1.11^{+0.29}_{-0.29}$

Cosmic distance ladder:  $q_0^{\text{loc}} = -1.08 \pm 0.29$ .

$q_0 : \sim 2\sigma$  "curiosity" with CMB

# $M_B$ and physics beyond $\Lambda$ CDM



- Discrepancy on  $H_0$  between CMB and cosmic distance ladder.
- Discrepancy on  $M_B$  calibration from CMB+BAO and Cepheids.
- $M_B$  is the backbone of SH0ES analysis.

Credits: Renan Alves de Oliveira



# $M_B$ and physics beyond $\Lambda$ CDM

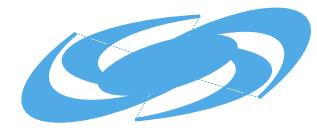


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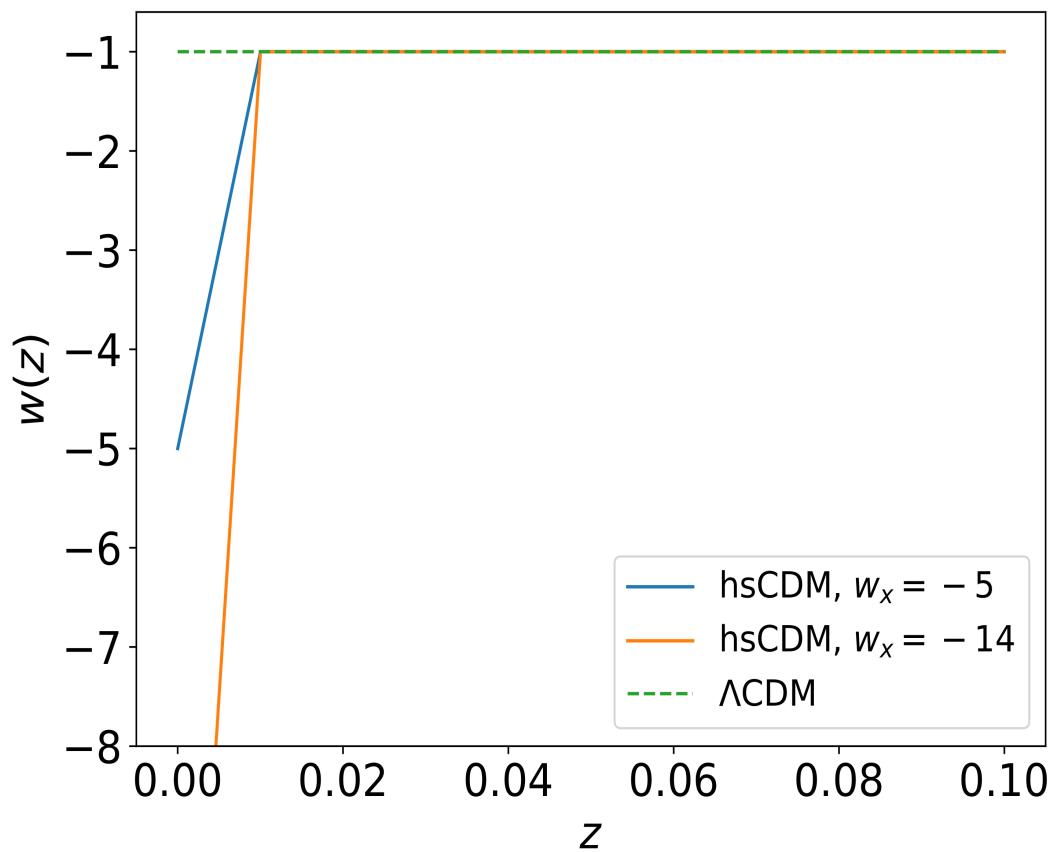


Time to include  $M_B$  on cosmological analysis?  
Are we trying to fit the right high hell on the left foot?

# $M_B$ vs $H_0$ : hockey stick model

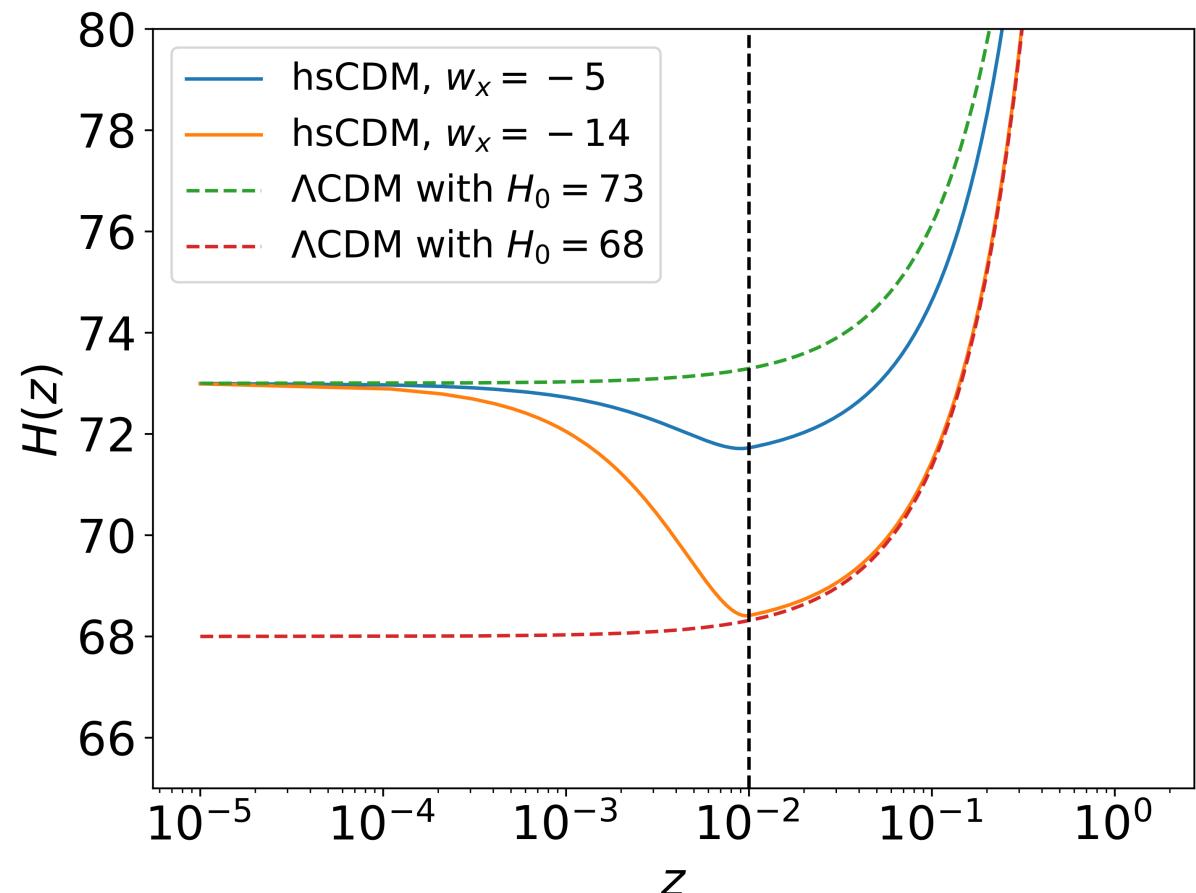


$$w = \begin{cases} w_x - (1 + w_x) z/z_t & \text{if } z \leq z_t \text{ (the blade)} \\ -1 & \text{if } z > z_t \text{ (the shaft)} \end{cases}$$



$$\frac{H^2(z)}{H_0^2} = \Omega_{M0}(1+z)^3 + \Omega_{R0}(1+z)^4 + \Omega_{\Lambda0}(1+z)^{3g(z)}$$

$$g(z) = \frac{1+w_x}{z_t \ln(1+z)} \times \begin{cases} (1+z_t) \ln(1+z) - z & \text{if } z \leq z_t \\ (1+z_t) \ln(1+z_t) - z_t & \text{if } z > z_t \end{cases}$$



# $M_B$ vs $H_0$ : hockey stick model



$$\theta = \{H_0, \Omega_{m0}, \Omega_{b0}, w_x, z_t, M_B, n_s\}$$

$$\chi^2_{\text{tot}, H_0}(\theta) = \chi^2_{\text{cmb}} + \chi^2_{\text{bao}} + \chi^2_{\text{sne}} + \chi^2_{H_0} \quad \chi^2_{\text{tot}, M_B}(\theta) = \chi^2_{\text{cmb}} + \chi^2_{\text{bao}} + \chi^2_{\text{sne}} + \chi^2_{M_B}$$

- CMB: gaussian prior on  $(R, l_a, \Omega_{b0}, h^2, n_s)$
- BAO: 6dFGS, SDSS-MGS and BOSS-DR12 ( $d_V(z)$ ,  $d_A(z)$  and  $H(z)$ )
- Supernovas: Pantheon supernovas ( $0.01 < z < 2.3$ )

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Analysis with prior on $H_0$	$\hat{\chi}_{\text{tot}}^2$	$\Delta\hat{\chi}^2$	best-fit vector $\{H_0, \Omega_{M0}, w_x, z_t, M_B, \Omega_{B0}, n_s\}$	distance from $H_0^{\text{R21}}$	distance from $M_B^{\text{R21}}$
$w\text{CDM}$	1045.8	0	$\{69.6, 0.29, -1.08, \text{---}, -19.39, 0.046, 0.97\}$	2.8	3.8
$hs\text{CDM}$	1035.1	-10.7	$\{72.5, 0.26, -14.4, 0.010, -19.42, 0.043, 0.97\}$	0.5	4.9
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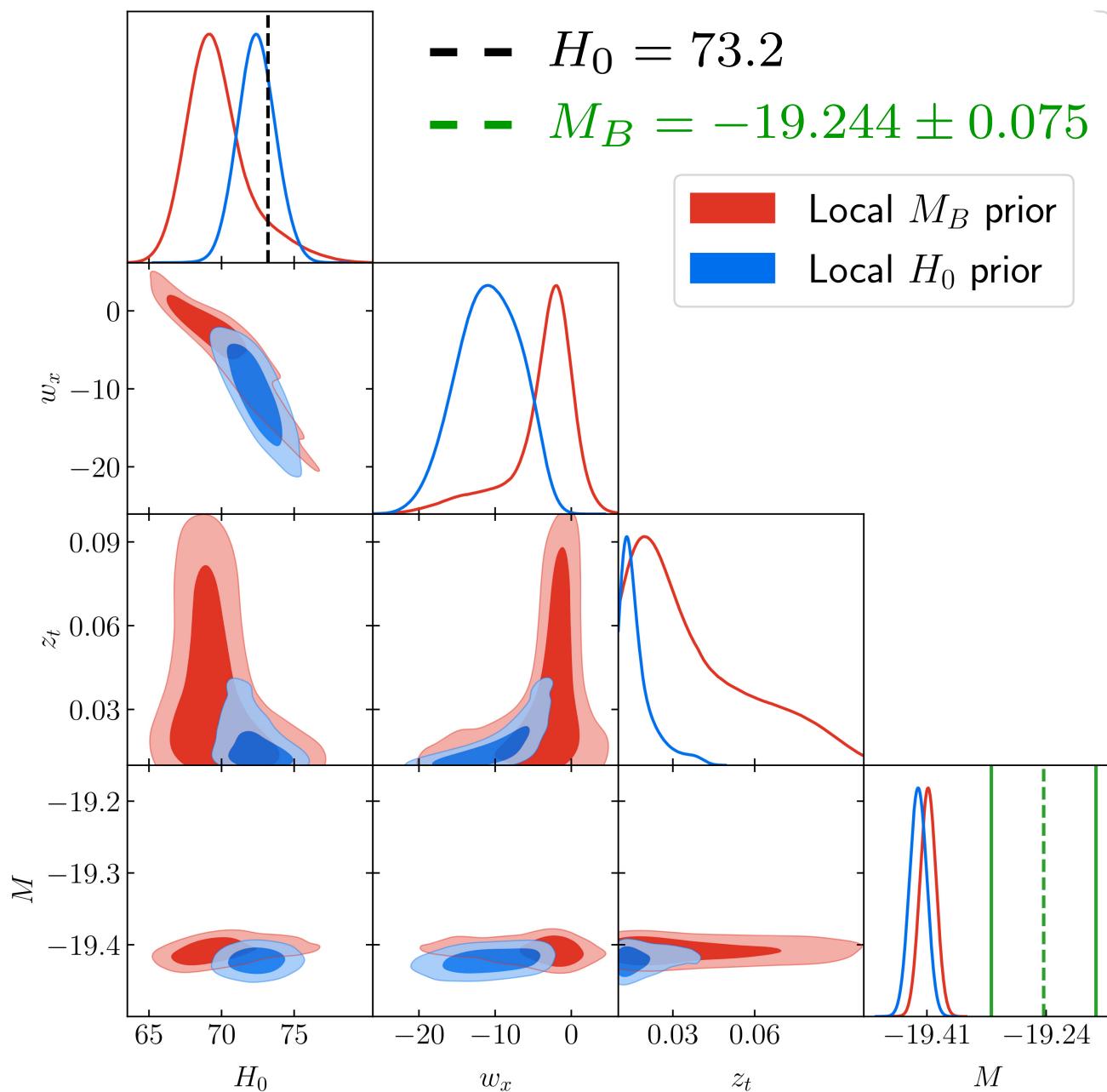


$$\theta = \{H_0, \Omega_{m0}, \Omega_{b0}, w_x, z_t, M_B, n_s\}$$

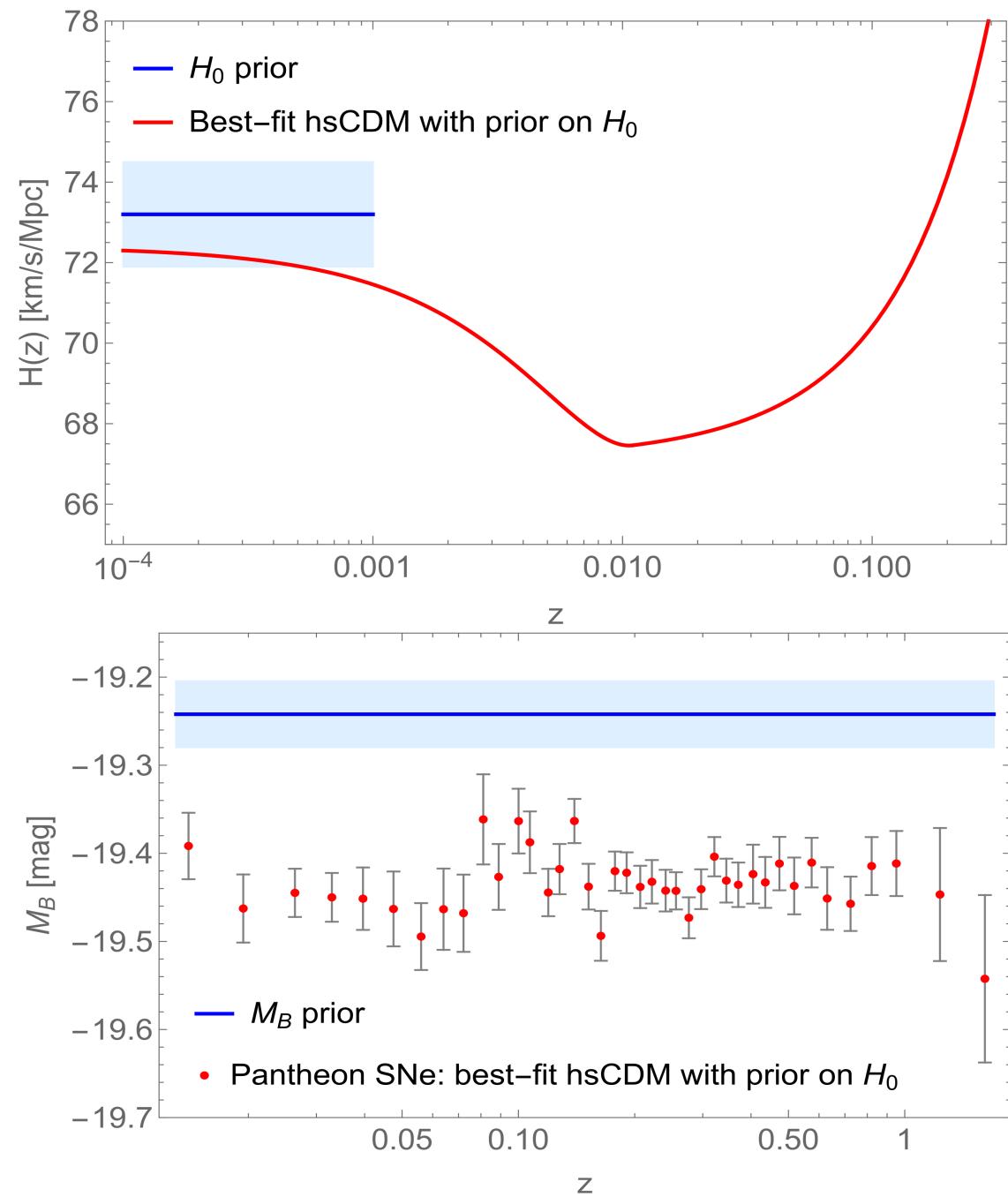
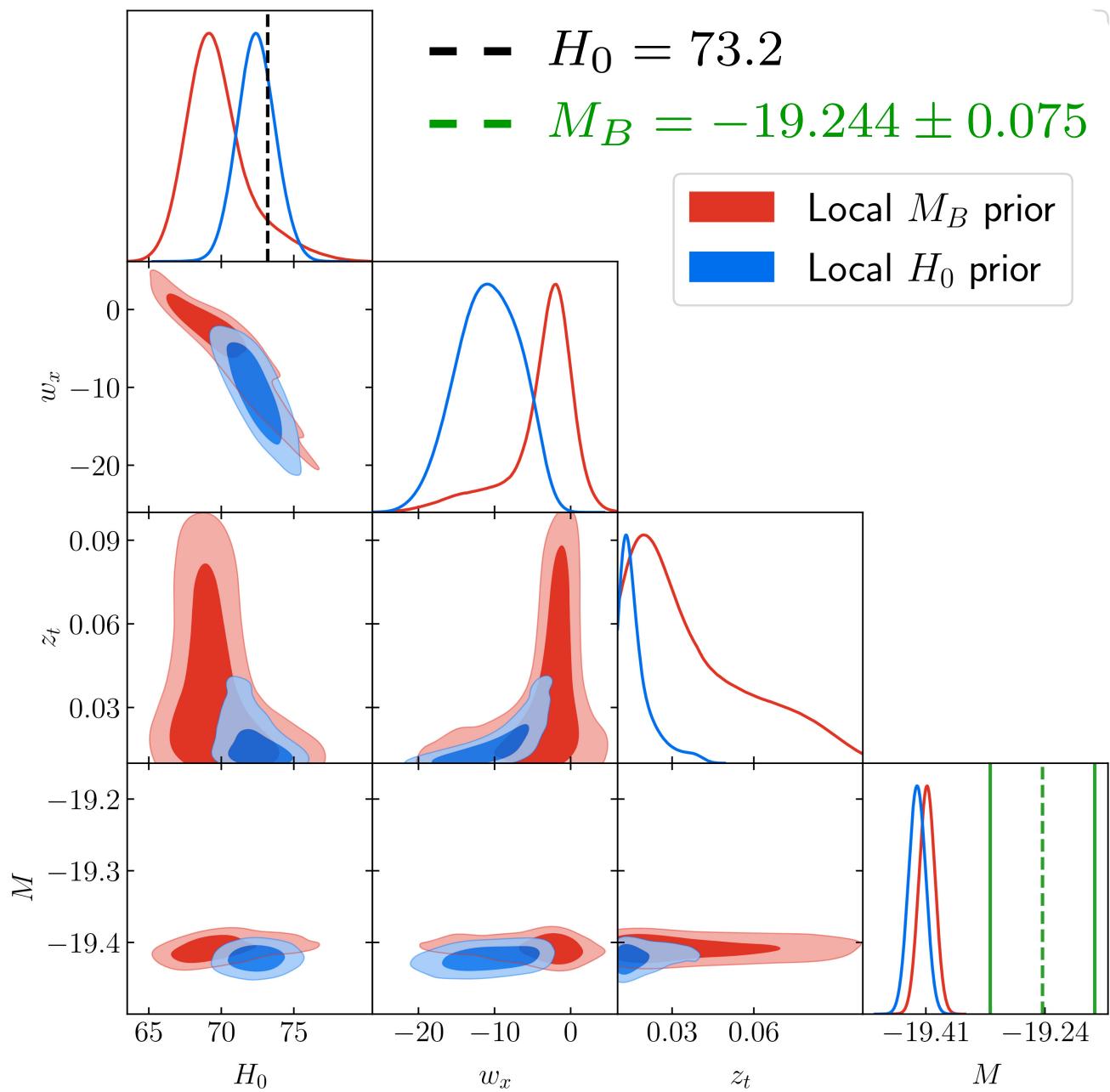
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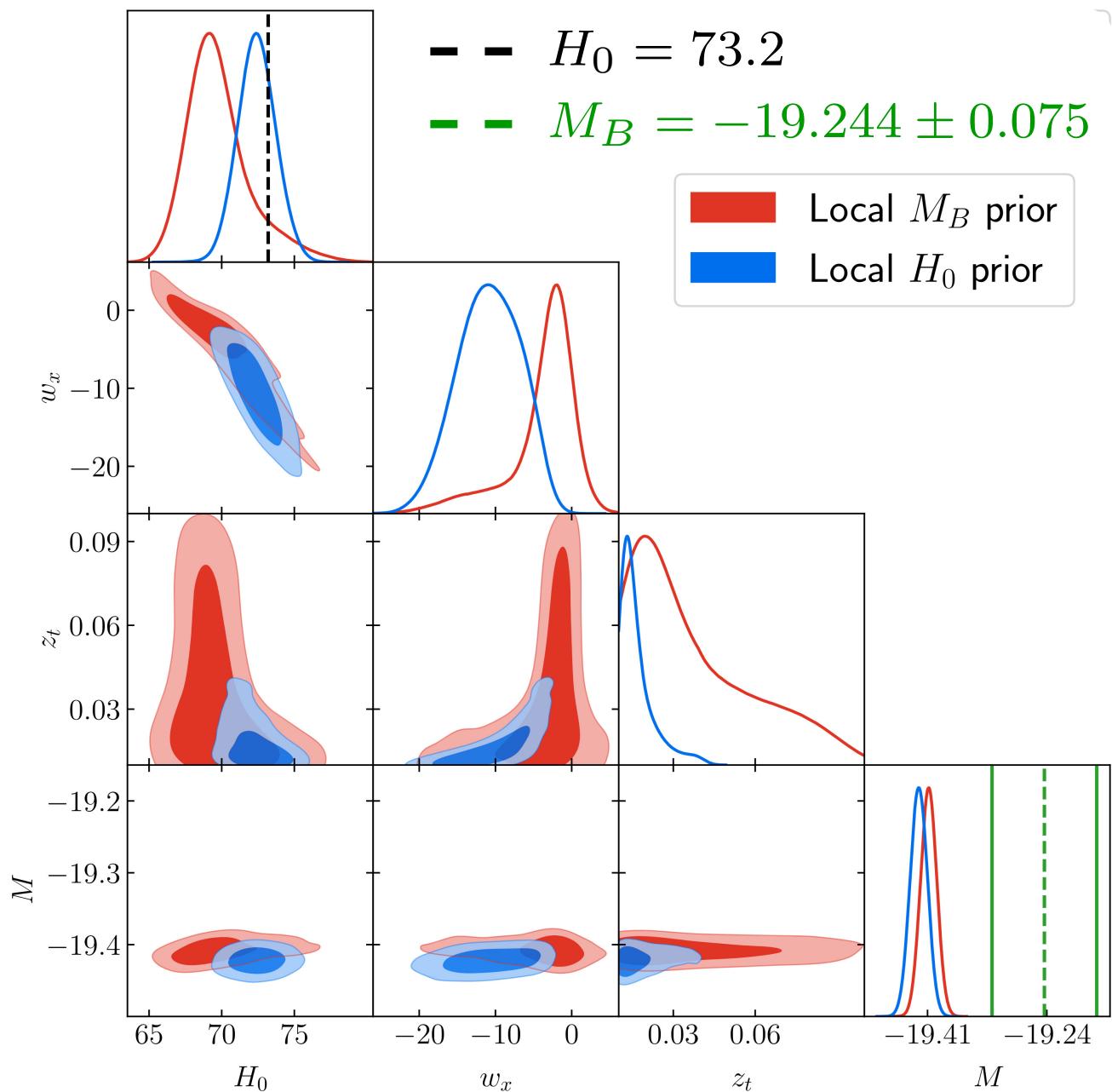
# $M_B$ vs $H_0$ : hockey stick model



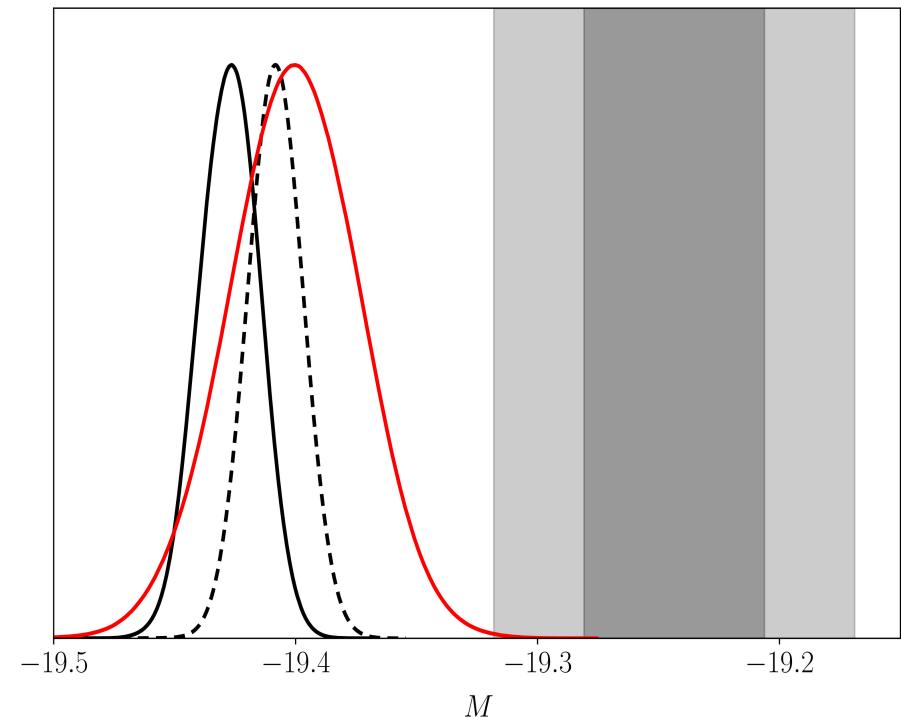
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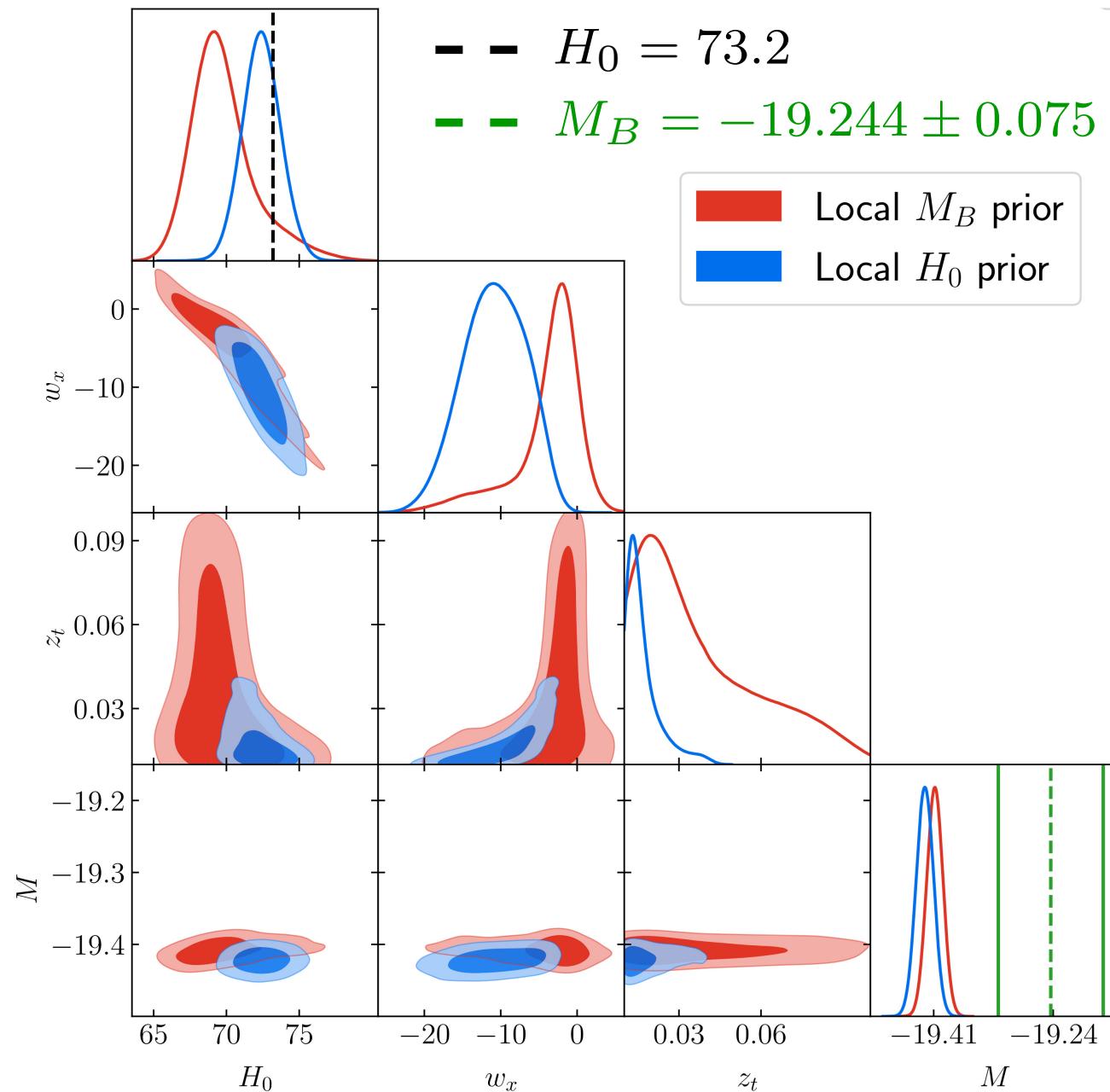
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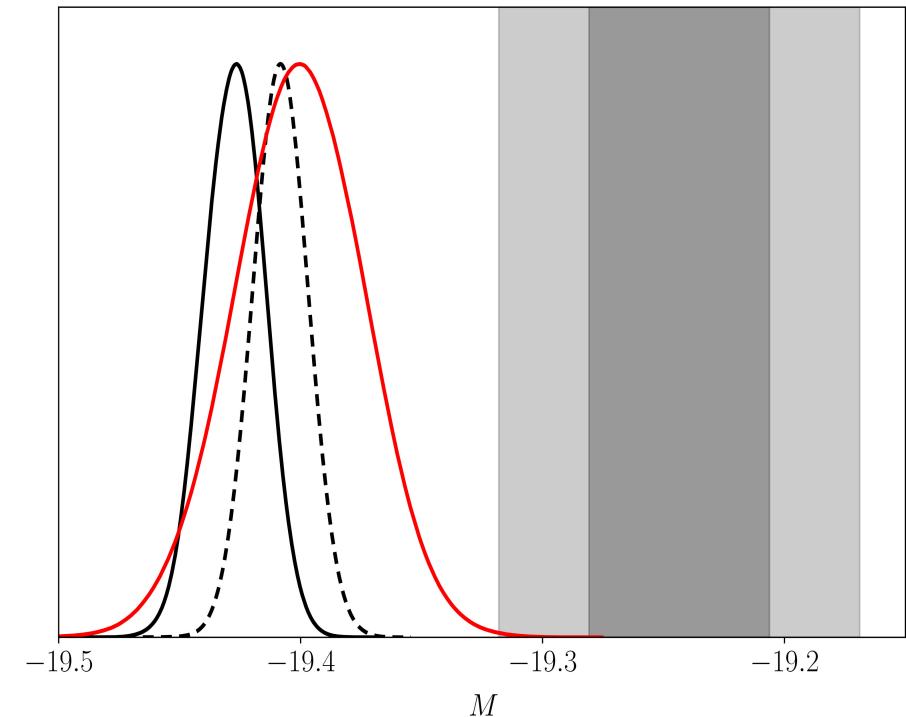
— CMB+BAO+SNe    - - - CMB+BAO+SNe+ $M_B$     — Inverse ladder



# $M_B$ vs $H_0$ : hockey stick model



— CMB+BAO+SNe    - - - CMB+BAO+SNe+ $M_B$     — Inverse ladder



~  $4.3\sigma$  tension on  $M_B$ !

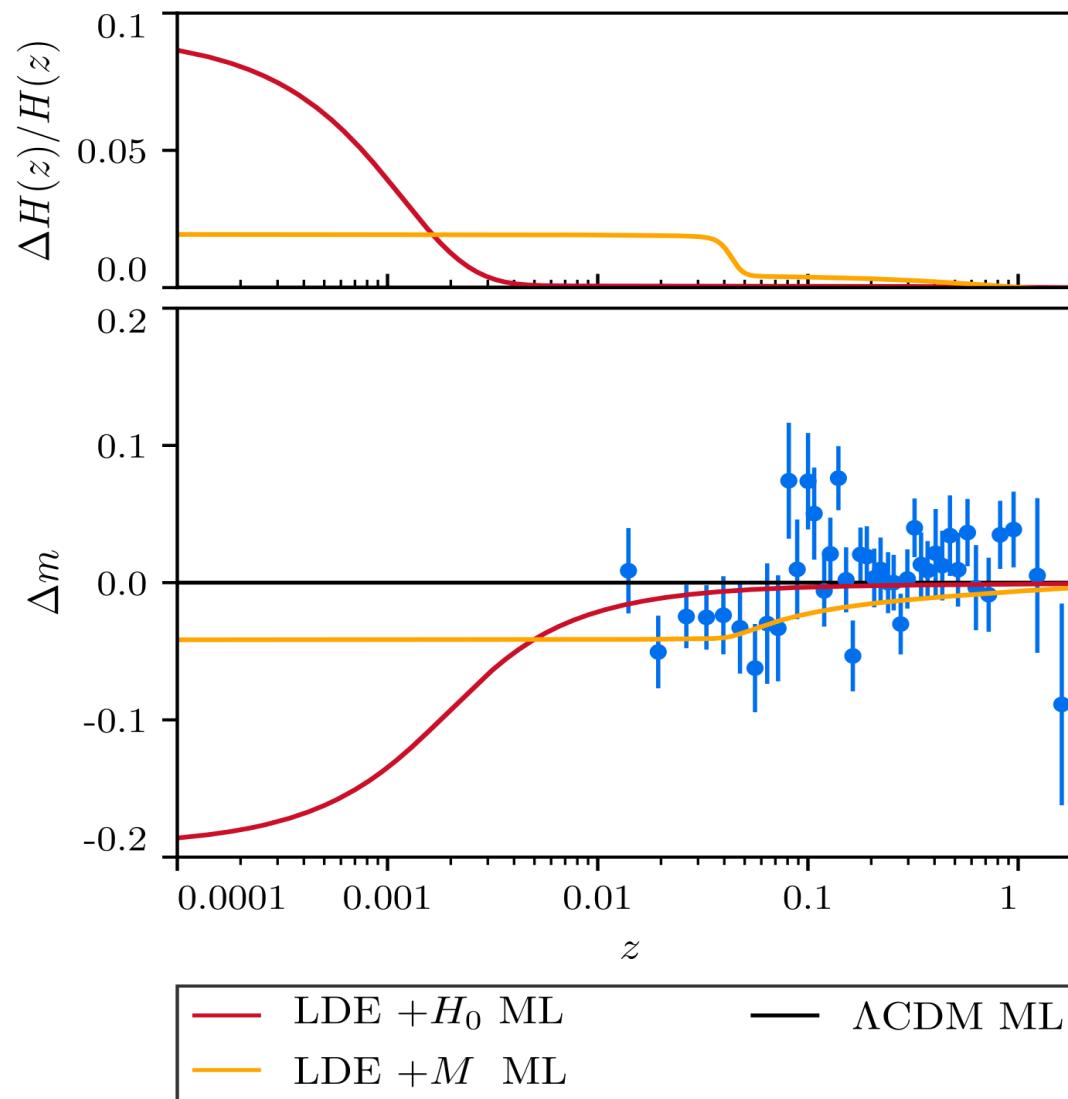
CMB+BAO+SN:  $-19.401 \pm 0.027$

Local constraint:  $-19.244 \pm 0.037$

# $M_B$ and physics beyond $\Lambda$ CDM



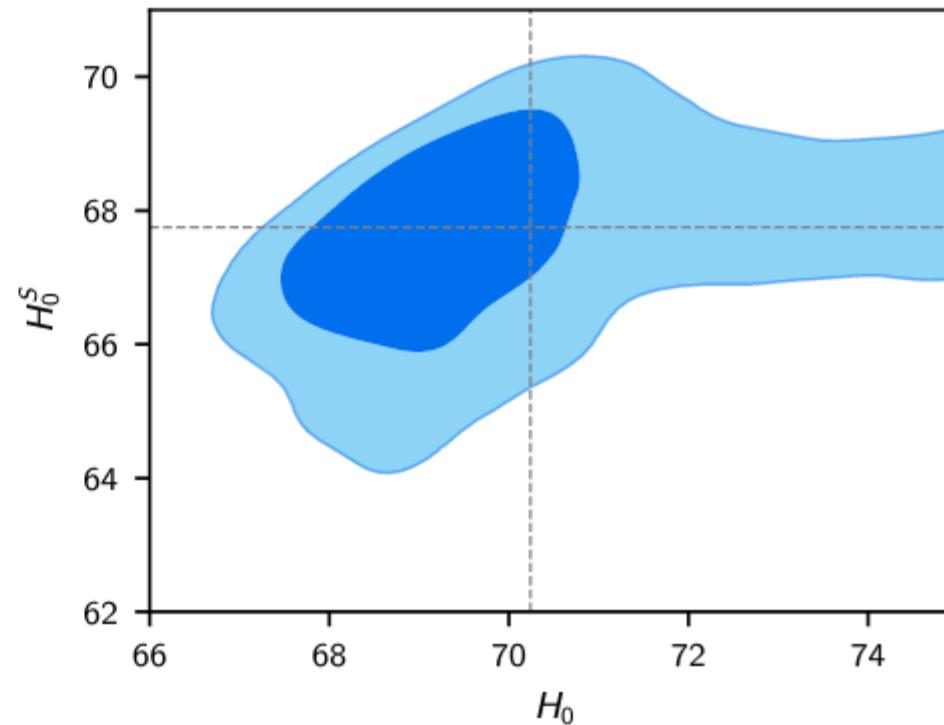
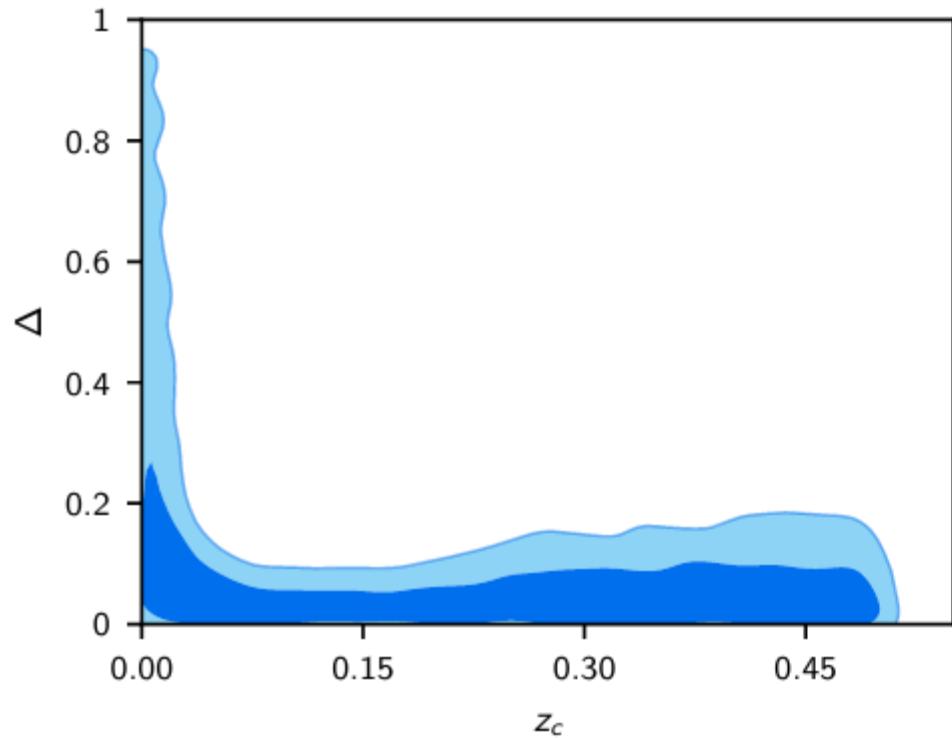
- Late dark energy fails to raise the Hubble constant (G. Benevento et al. arXiv:2002.11707)



# $M_B$ and physics beyond $\Lambda$ CDM



- Late dark energy fails to raise the Hubble constant (G. Benevento et al. arXiv:2002.11707)
- Supernova data are insensitive to late time changes in the dark energy (G. Efstathiou et al. arXiv:2103.08723)



# Conclusions



- No strong evidence systematics error (that can solve the tension).
- Other measurements would be crucial to confirm (or ruled out) new physics/systematics
- Local constraint on  $q_0$  shows a "curious" tension  $2\sigma$  with  $\Lambda$ CDM
- There is a tension between  $\alpha$  and  $\theta$  BAO data set.
- Inverse distance ladder does not agree with the Cepheid calibration  $M_B$  (if  $r_d$  CMB and  $\alpha_{BAO}$  are assumed)
- Use a  $M_B$  prior instead of a  $H_0$  prior: avoid SN double-counting, pure astrophysical and account for the tension with Cepheids.
- late-time modifications to  $\Lambda$ CDM do not solve the Hubble discrepancy!



Obrigado!